Author response to 1st reviewer

We thank the reviewer for their comments and would like to address the questions raised by the reviewer point by point. In this version of the response to the reviewer, we also outline where we made changes in the manuscript in response to the reviewer comments.

“The short-term isotope exchange data is gained in isotope exchange studies that have been conducted in order to estimate the capacity of the soils to sorb P. The experiments typically last for 90 minutes and during this time the 33P activity in the soil solution decreases strongly due to sorption to the soil solid phase. Isotope exchange experiments have been used by Frossard et al. and other working groups to learn about the plant availability of different P pools in soil.”

Isotope exchange kinetic experiments (IEK) were developed to “determine the rate at which phosphate ions in the soil solution are renewed from phosphate ions in the solid phase,” not to measure soil P sorption capacity (Fardeau et al. 1991). Isotopic methods using P radioisotopes date back to the 1940s (McAuliffe et al. 1948). IEK method was then further developed and tested by J.C. Fardeau and colleagues (Fardeau and Marini 1968, Fardeau and Jappe 1988, Fardeau 1985). Unfortunately, these and further key publications validating the IEK method are in French, which explains why they are little known outside of French-speaking regions.

IEK experiments are thus based on, and have done much to further, our understanding of exchange mechanisms. This explains why E-values derived from IEK perform much better at predicting crop response than other soil P tests (Frossard et al. 1994), and why E-values are widely accepted as the gold standard for determining P bioavailability (Hamon et al. 2002, Kruse et al. 2015).

“I have doubts about the validity of the approach proposed here for the following reasons. First, the calculation of MRT is based on the assumption of steady state (inputs=outputs). However, it is highly questionable whether this assumption is correct. In the experiments used by the authors, typically 10 g of sieved soil are oversaturated by 100 ml of water and put on a shaker until the end of the experiment. Being oversaturated with water and kept on a shaker is not a natural condition for soils. Thus, very likely the soils move away from steady state during these experiments due to this disturbance. Thus, the assumption of steady state is very likely violated in the experiments, on which the calculation is based.”

It is true, as the reviewer pointed out, that the soil/water suspension we use in IEK is not similar to soil natural conditions, however several studies comparing E-values extrapolated from IEK and L-values from pot experiments with plants (so under conditions much closer to “natural”) have shown that these two independent estimations of P exchangeability closely overlap. Fardeau and Jappe (1976), showed that measured L-values and extrapolated E-values were very similar. Morel and Plenchette (1994) showed the same for soybean and barley (measuring E-values on soil suspensions in periods from 1 min to several days) and Frossard et al. (1994) for Agrostis on several different soil types. Similarly, Sinaj et al., (2004) demonstrated the same for zinc (different nutrient, but same IEK method) on several different soils and plant species.

The comparisons between E-values extrapolated from IEK experiments and L-values measured in pot experiments with plants suggest that extrapolated E-values are a good approximation for P
exchange between solid phase and soil solution. Although in IEKs soil is suspended in water, the soil/solution transfer is not readily affected, especially compared to other methods using chemical extractions.

Finally, in the discussion section (p. 10 l. 26 to p. 11 l. 9) we validate our estimates against incubation experiments and field measurements.

To state the limitation more clearly of measuring MRTs in simplified laboratory conditions, we added the following sentences to the "limitations" section (p. 12, l. 2-6): “Our approach only considers a simplified system of soil and water in steady-state conditions, and excludes biological activity. In field conditions, P residence times may be different due to non-steady state conditions, microbial interactions with abiotic processes, as well as plant uptake and alterations of the physical and chemical soil environment (Hinsinger, 2001). For example, intensive P uptake by plants may lead to net changes in soil P pools in addition to exchange fluxes (Guo et al., 2000). Also, it is likely that MRTs are affected by temperature and changes in soil moisture.”

“Second, the authors derive MRTs of more than 10,000 years (Fig. 4) from experiments that last only for a much, much shorter period of time, which is problematic since the exchange processes measured over a short period of time are extrapolated by a factor of > 1,000,000.”

We agree that estimates of longer MRTs (i.e. for the HCl-P pool) are more uncertain because extrapolated E-values can only be validated with incubation data for time spans up to several months due to the short half-life of the P radioisotopes. This limitation is clearly stated in the manuscript (p. 1, l. 6-9). However, three independent lines of evidence support our estimates even of the very long MRTs of HCl-P.

Firstly, the strong correlation (following the 1:1 line) of E-values with sequentially extracted pools, also for P not exchangeable in three months and HCl-P (Fig. 2). This shows that these pools are clearly related even though measured by independent methods. The same correlation was found already by Frossard et al (1996) for a sewage sludge in which the HCl-P pool was composed by sparsely soluble (and therefore slowly exchangeable) Ca-P minerals.

Secondly, stable oxygen isotopic ratios of phosphate have been studied in HCl-P pools in soils of known ages, and shown that indeed this pool may remain stable for time spans of years to >> millennia, depending on environmental conditions and soil properties. This range fits with our estimates. See (p. 11, l. 11-19).

Thirdly, the strong relationship between pH and MRT of HCl-P that we observed in our data is supported by empirical observation, or at least make sense given what we know about the composition and stability of HCl-P (p. 10, l. 1-5). Hence, both the order of magnitude and the pattern in our HCl-P estimates make sense given what we know about P species extracted by HCl and their relative stability under different environmental conditions.

“Third, the calculation proposed by the authors (Equation 1) is based on the assumption that the specific 33P activity of the soils solution (33P in solution to total inorganic P in solution) is stable during the 90-minutes experiment. This assumption is not correct. During 90-minutes experiments the specific 33P activity of the decreases exponentially, which means that the ratio of
33P and total inorganic P decreases, which is mostly due to adsorption of 33P to the soil solid phase. This change of the specific 33P activity is problematic because 33P is used as a tracer, and the ratio of the tracer to the inorganic P in the soil solution is changing continuously over the course of a short-term experiment. The proposed approach would require that the ratio of 33P to inorganic P in the solution is stable, but the specific 33P activity of the soil solution approaches a stable value only over longer periods of time.”

We do not understand the reviewer’s concern here: equation 1 is not based on the assumption that specific activity of 33P (or 32P) is constant in the soil solution. Rather, the denominator of Eq. 1 specifically describes the change in specific activity. IEK experiments provide insights on P exchange between the soil solution and the solid phase by measuring the decrease of radioisotope activity in the soil solution. This decrease in specific activity is modelled by

\[
\frac{r(t)}{R} = m \left( t + \frac{1}{m} \right)^{-n} + \frac{r(\infty)}{R}
\]

Where \(r(t)\) is the radioactivity (Bq) measured at time \(t\) (min), \(R\) is the total amount of radioactivity added, and \(m\) and \(n\) are the model parameters that describe the rapid and slow physicochemical processes, respectively (Fardeau et al. 1991, Frossard et al. 2011).

“In addition (and less importantly), the description of the applied calculation is incomplete, and the calculation of the variables \(n\) and \(m\), which are derived from short-term experiments is not explained in the present manuscript.”

We thank the reviewer for pointing out that the description needs to be improved. We added the following sentence “The parameters \(m\) and \(n\) describe the rapid and slow physicochemical exchange processes, respectively, and are determined by fitting a non-linear regression model to measurements of radioisotope concentration in solution (for details see Fardeau et al. 1991 and Frossard et al. 2011).” (p. 5, l. 6-9). Based on the second reviewers’ comments, we also added a file containing all of the primary data (including \(n\) and \(m\) values).

References


Author response to 2nd Reviewer

“The estimate of MRT deserves an encouragement, because it provides a fundamental and quantitative insight into the dynamics of P in soil. In this regard, I would like to support the publication of this work. However, before this, I have some concerns for the authors to address.”

Thank you very much for taking the time to review our manuscript and for your supportive and constructive comments. Below, we have addressed your comments point by point and described our changes to the revised manuscript.

“I am curious about why the MRT of HCl-P can be estimated in the way used by the authors. HCl-P is mainly of apatite P in neutral and alkaline soils. The dynamics of apatite P should be unidirectional, that is apatite P is always depleted without a formation during the experimental duration (90 mins). So, an exchangeable between resin P and HCl P is unreasonable at least for neutral and alkaline soils (Fig. 1), although it’s possible if HCl P is largely of Fe/Al associated P, as in acidic soils.”

Indeed, exchange between HCl-P and the soil solution is often considered to be unidirectional in model formulations, i.e. a slow one-way flow of phosphates from the HCl-P pool to the soil solution via dissolution. This holds effectively true if we consider the net change of this pool over a pedological time scale (e.g. the Walker and Syers model). However, as pointed out by the reviewer, HCl-P may also contain secondary P forms, such as Fe/Al associated P. Even in neutral/alkaline soils, Ca-P forms extracted by HCl may be secondary because phosphate ions easily precipitate with Ca in systems containing carbonates (Frossard et al., 1995).

Analysis of stable oxygen isotopic ratios in phosphate have also confirmed the dynamics of the HCl-P pool. There, on all soils studied except for young/unweathered soils, oxygen in phosphate carried the biological signature, suggesting re-precipitation of phosphate from the soil solution into the HCl-P pool after cycling through the biosphere (Helfenstein et al., 2018; Tamburini et al., 2012). Similarly, radioisotopic tracing shows radioisotope tracer incorporation over time scales of days-weeks into HCl-P (Buehler et al., 2002). Due to the empirical evidence, we propose that future P model formulation should consider bi-directional exchange between HCl-P and the soil solution.

We explain why we propose bi-directional exchange in a new section in the discussion (p. 13, l. 10-18).

“All the estimates of MRT are obtained based on laboratory incubation. The estimates therefore should be much different from those in field, which can be affected by soil moisture and temperature and many other factors. This limitation and their potential effects on the estimates should be noted. Are the estimates comparable to the estimates of Hou et al. (2019) based on greenhouse experiments?”

We agree that MRTs in field situations are likely to be vary from MRT estimates based on
laboratory experiments. Hou et al. 2019 calculated MRTs of P in P pools based on changes in P pool sizes over time with data from a pot experiment growing plants on 8 different soils (Guo et al., 2000). Below we compare the MRT of Hou et al. 2019, calculated as the inverse of the reported turnover rates for the respective pools, to the median MRTs of our study (see Table 3).

<table>
<thead>
<tr>
<th>Pool</th>
<th>MRT in Hou et al. 2019 (means)</th>
<th>MRT in our study (medians)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Labile P</td>
<td>25 days</td>
<td>&lt;&lt; 1 day</td>
</tr>
<tr>
<td>NaOH-P</td>
<td>43.5 days</td>
<td>25 days</td>
</tr>
<tr>
<td>HCl-P</td>
<td>3.1 years</td>
<td>2.6 years</td>
</tr>
</tbody>
</table>

While MRT estimates for NaOH-Pi and HCl-P are similar, the range in MRTs was much larger in our study than in Hou et al. (2019). Also, the MRT for labile P is one order of magnitude lower in Hou et al. (2019) than in our study. These differences are not surprising given the different approaches used to estimate MRT of P in these pools. By measuring changes in P pool sizes, only net P fluxes are considered. The radioisotopic approach on the other hand also measures exchange fluxes not leading to changes in pool sizes. This is important because sorption/desorption fluxes without net changes in P pool sizes are the main process driving P cycling between the soil solution and inorganic P pools, and thus important for P bioavailability (Frossard et al., 2000; Syers et al., 2008).

To address the reviewer’s concerns, we expanded on the discussion of limitations arising from laboratory estimates (p. 11, l. 3-5). Also, we point out how our estimates are different from MRT estimates considering net changes in P pool sizes (p. 3, l. 14-16).

“The Figure 1 and the calculation of MRT of NaOH-P and HCl-P are weird. MRT-NaOHP is estimated based on the sum of labile P and NaOH-P (while not only NaOH alone?). MRT-HClP is estimated on the sum of labile P, NaOH-P, and HCl P (while not on HCl P alone?). This will at least confuse readers, which do MRT-NaOHP and MRT-HCl really measure?”

We realize that the calculation was not properly described, making the understanding of the approach difficult. Hence, we added the following sentence: “The summation of more labile pools to estimate MRT of more recalcitrant pools is necessary because in this model “slow” exchanging pools can only exchange once “faster” exchanging pools have fully exchanged.” (p. 6, l. 2-3). The explanation is followed by the justification of this assumption (p. 6, l. 6-9).

“In Fig. 1 the conceptual diagram differs from many other diagrams, such as Hou et al. JGR
Biogeosciences (2019) and Tiessen et al. (1984). The model structure (conceptual diagram) affects the estimate of MRT. I think this should be discussed to let readers know there are other possible exchange pathways among soil P pools that will affect the estimate of MRTs.”

We realize that one of the difficulties in P modelling is that many empirical studies and also many models are based on slightly different conceptual diagrams of P cycling. In preparing this paper, we had a lot of discussions with Daniel Goll (as a representative of the P modelling community and co-author on this paper) on how our approach relates to existing model formulations. Our approach has been to clearly state the assumptions (p. 6, l. 6-22) and discuss the limitations (p. 11, l. 22- p. 12, l. 9). Also, we made sure that our conclusions go beyond our conceptual model and apply to all P model formulations.

To address the reviewer’s comments, we added an additional sentence to make it explicit that we did not consider exchange between NaOH-Pi and “occluded pools” (p. 6, l. 10-12).

Also, we adapted the concluding paragraphs to make them more appropriate also to other conceptual model formulations of P cycling (see section “implications for land surface modelling”).

“Give units in Figs. 2 and 5. Give Y axis lab (MRT?) in Fig. 4”
Thank you for spotting this. We added units to the x- and y-axes in Fig 2 (in the figure legend because the axes labels are already crowded). Figure 5 already has units (no changes made). In Fig. 4 the y-axis is indeed MRT. We added that.

“In L15, “and call these soil P pools”, I think I understand what you mean, but it reads a bit weird.”
We deleted the sentence fragment because it is unnecessary and can lead to confusion.

“L24-25: which two studies? Does the filled data affect much of the results?”
The two studies that didn’t have information on soil texture were Borda et al. 2014 and Helfenstein et al. 2018. This is listed in supplementary table 1, “Sources for data on soil and other properties for each site”. Additionally, we now referenced the studies in the sentence (p. 4, l. 11).

To test if the “filled data” affects the results, we repeated the analysis while excluding the Borda and Helfenstein samples (Fig 1 below. Compare to supplementary figure 3). The F and p values changed slightly, but the general conclusion is the same: significant regressions for MRT of labile P and NaOH-P, but not for HCl-P, though all models point at the same trend. Because the “filled data” does not affect the results we made no changes in the manuscript.
“I think the data used by the authors are valuable. Why not make the raw data and the fitted m and n values open access?”

Thank you for finding our data valuable. We will provide it as a supplementary csv table in the revision. See “all_data.csv” file.

REFERENCES


Figure 1. Simple regression of calculated mean residence time of P with clay concentration, excluding samples for which soil texture data was taken from SoilGrids. The model values changed slightly, but show the same trend. For labile P (F-statistic = 5.4,  \( p = 0.03 \)) and NaOH-P (F-statistic = 9.8,  \( p < 0.01 \)), but not for HCP (F-statistic = 3.8,  \( p = 0.06 \)).


Estimates of mean residence times of phosphorus in commonly-considered inorganic soil phosphorus pools

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Abstract. Quantification of turnover of inorganic soil phosphorus (P) pools is essential to improve our understanding of P cycling in soil-plant systems and improve representations of the P cycle in land surface models. Turnover can be quantified using mean residence time (MRT), however, to date there is little information on MRT of P in soil P pools. We introduce an approach to quantify MRT of P in sequentially-extracted inorganic soil P pools using data from isotope exchange kinetic experiments. Our analyses of 53 soil samples from the literature showed that MRT of labile P (resin- and bicarbonate-extractable P) was on the order of minutes to hours for most soils, MRT in NaOH-extractable P was in the range of days to months, and MRT in HCl-extractable P was on the order of years to millennia. Multiple regression models were able to capture 54 – 63 % of the variability in MRT among samples, and showed that land use was the most important predictor of MRT of P in labile and NaOH pools. MRT of P in HCl-P was strongly dependent on pH, as high pH soils tended to have longer MRTs. This was interpreted to be related to the composition of HCl-P. Under high pH, HCl-P contains mostly apatite, with a low solubility, whereas under low pH conditions, HCl-P may contain more exchangeable P forms. These results suggest that current land surface models underestimate the dynamics of inorganic soil P pools and could be improved by reducing model MRTs of the labile and NaOH-P pools, considering soil-type dependent MRTs rather than universal exchange rates, and allowing for two-way exchange between HCl-P and the soil solution.

1 Introduction

Since only a small fraction (usually < 1%) of soil phosphorus (P) is present as phosphate in the dissolved state where it can be taken up by plants and microbes, the rate at which this pool is replenished from other soil P pools is critical to assess the bio-
availability of soil P (Syers et al., 2008). The extent and the time scale on which unavailable soil P forms can become gradually bioavailable is an important factor affecting ecosystem productivity under increasing carbon dioxide concentrations (Sun et al., 2017). Estimates of P availability thus directly influence inferences on carbon sequestration. However, currently P availability is poorly constrained in land surface models, which hampers our ability to project future carbon sequestration rates (Goll et al., 2012). Modelling the rate of replenishment from different pools requires knowledge of the mean residence time of P in these pools. While there is growing information on concentrations of soil P pools in soils (Hou et al., 2018b), and how they react to drivers such as crop management, land use change or changing climate (Feng et al., 2016; Negassa and Leinweber, 2009; von Sperber et al., 2017), little is known about the temporal dynamics of these pools (Hou et al., 2019). This knowledge gap not only limits linking data on soil P pools to P availability, it also slows the incorporation of P into global land surface models, and hence estimating the effect of P cycling on long-term ecosystem functioning at large spatial and temporal scales (Reed et al., 2015).

Soil P pools are most commonly measured using sequential extraction, whereby soil P is extracted with increasingly strong reagents to yield experimentally-defined P pools. While different variants of sequential extraction exist, the Hedley extraction and variants thereof are most widespread (Hedley et al., 1982). Here, we analyzed studies that used a resin-extraction, followed by 0.5 M NaHCO₃, 0.1 M NaOH, and finally 1 M HCl extractions. It is assumed that resin and NaHCO₃-extractable P represents loosely-sorbed P, NaOH extracts P associated to Fe and Al (hydr)oxides, and HCl-P contains phosphates associated to Ca and soluble in acids, especially apatites (Moir and Tiessen, 1993). A precise characterization of P mineral forms present in these inorganic pools is difficult since there is a plethora of mixed compounds and not pure crystalline P forms in soils. However, spectroscopic techniques have been used to confirm that soils with more HCl-P tend to contain more Ca-P, and soils with relatively larger NaOH pools P contain more P associated to Fe- and Al (Frossard et al., 2002; Helfenstein et al., 2018a; Kar et al., 2011; Prietzel et al., 2016; Wu et al., 2014). Mean residence time (MRT) of P has been quantified in the soil solution and in soil microbes; however, little is known about the mean residence time of P in Hedley pools. Mean residence time is defined here as the average time required to completely renew the content of a pool at steady state, and is also called turnover time in other studies (Six and Jastrow, 2002). Radioisotopic labeling-experiments have shown that the MRT of P in soil solution is on the order of milliseconds to minutes (Fardeau et al., 1991; Helfenstein et al., 2018b), while MRT of P in soil microbiota tends to be on the order of days to weeks (Gross and Angert, 2017; Oberson and Joner, 2005; Spohn and Widdig, 2017). Isotope exchange kinetic experiments, where the dilution of a radiisotopic tracer (³²P or ³³P) is traced in a soil-water suspension, allow measuring the exchange of P by physicochemical processes as a function of time (Fardeau, 1996; Frossard et al., 2011). While the MRT of P in resin, NaOH, HCl pools has recently been approximated in soils on a Hawaiian climatic gradient (Helfenstein et al., 2018a), it is not clear if these MRTs also pertain to non-volcanic soils.
Land surface models describe the complex interactions governing the cycles of water, energy, carbon, and increasingly incorporate cycles of major soil nutrients (i.e. nitrogen and phosphorus) (e.g. Wang et al. 2010). The representations of inorganic soil phosphorus dynamics are currently very rudimentary in such models: soil inorganic phosphorus is commonly separated into different pools according to differences in residence times (fast, intermediate and slow pools) (Wang et al., 2010). Although the structure, i.e. number of soil P pools and the connection among pools, differs among models, they commonly apply the same concept. In general, the residence time of P in the fastest pool is modelled as a function of multiple, abiotic (chemical weathering, sorption) and biotic (mineralization, immobilization, plant uptake, phosphatase activity) processes (Lloyd et al., 2001), while more recalcitrant pools have prescribed globally uniform decay rates. The decay rates are either derived from calibration to achieve plausible total soil P stocks (Goll et al., 2012; Wang et al., 2010; Yang et al., 2014), or derived from temporal net changes in soil P fraction along a single soil chronosequence (Goll et al., 2017). Such calibration strategies are not able to capture gross exchanges among soil P pools, which do not result in net changes in pools size, but are critical for the bioavailability of soil P. Hence, current model formulations of P cycling are likely underestimating inorganic soil P dynamics and overestimating inorganic P pool MRTs.

The objective of this work was to quantify the MRT of P in inorganic soil P pools in a wide range of soil types and provide much needed information to constrain soil P dynamics in global models. We limited our study to inorganic pools because the isotope exchange kinetic approach can only be used to study physicochemical exchange processes, whereas MRT of P in organic pools is controlled by biological processes. In our analysis, we assume that the time necessary to renew the total amount of P present in a Hedley pool (MRT) can be equated to the time necessary for phosphate ions in solution to exchange with all phosphate ions located in this pool (Fig 1a). This allowed us to calculate MRT using the function for isotopically exchangeable P as determined in isotope exchange kinetic experiments. However, it also means that potentially important processes influencing P MRT, such as biological and solid-state P transformations, were neglected. The second objective of this work was to determine if variation in MRT among soils could be explained by soil properties and climatic variables. To meet these aims, we searched the literature for soil samples for which both P sequential extraction and IEK data were available. We then used a function describing isotopically exchangeable P as a function of time to calculate MRT of P in resin-P, labile-P (resin- and bicarbonate extractable), NaOH-P, and HCl-P.

2 Methods

2.1 Data set

We found 53 soils for which both P sequential extraction and isotope exchange kinetic data were available. Twelve samples were from a Hawaiian climatic gradient (Helfenstein et al., 2018a), five from a long-term field trial in Switzerland (Keller et al., 2012), eleven from a study of different soils throughout New Zealand (Chen et al., 2003), fourteen from a forested geosequence in Germany (Lang et al., 2017), seven from field-experiments on highly-weathered soil in Colombia (Buehler et
al., 2003; Oberson et al., 1999), and four from an agricultural field-trial on Fluvisols in Italy (Borda et al., 2014). Information on soil properties (pH, soil texture, organic C concentration), climate (mean annual temperature and mean annual precipitation), soil P pools (total P, resin-extractable P, NaHCO$_3$-extractable inorganic P, NaOH-extractable inorganic P, HCl-extractable P), and P exchange properties ($P_w$, m, n, $P_{inorg}$, see section 2.2) were retrieved from the original publications, associated publications, or by contacting the authors (Table 1). One study used an ammonium chloride extraction instead of a resin-extraction (Chen et al., 2003). We added the first two extractions (resin or ammonium-chloride and NaHCO$_3$) and called this the “labile pool”. For two studies (Borda et al., 2014; Helfenstein et al., 2018a), soil texture was not reported and had to be estimated from global gridded (250m resolution) soil information based (Hengl et al., 2017) based on geographic information of the sample site. For the full documentation of sources for the soil property information, please see Supplementary Table 1.

Four soils (“Himatangi”, “Hurundi”, “Okarito”, and “Temuka” (Chen et al., 2003)) were excluded because, unlike the rest of the samples, the Hedley pools of these soils were much larger than the pools from isotope exchange kinetics. This yielded unreasonably high MRTs because of the asymptotic behavior of the E(t) equation. In the discussion, we briefly discuss how excluding these soils affected multiple regression models.

Despite only encompassing 53 soils from 20 geographic sites, the dataset included samples from a wide set of climatic conditions (Supplementary Fig. 1), and a variety of soil texture classes (Supplementary Fig. 2). Eleven of the soils samples were from arable land use, 14 from forest, and 28 from grassland. The world reference base soil orders entailed were Acrisol (1), Andosols (17), Cambisols (19), Ferralsols (7), Fluvisols (4), and Luvisols (5) (IUSS Working Group WRB, 2015). While some of the soils are considered to be low in available P (Buehler et al., 2003; Lang et al., 2017; Oberson et al., 1999), the data set also includes soils developed on P rich parent materials (Helfenstein et al., 2018a; Lang et al., 2017) or soils that have been intensively fertilized (Borda et al., 2014).

### 2.2 Estimating mean residence times

Isotopically exchangeable P ($E_{iso}$) [mg kg$^{-1}$] can be modelled as a function of time by Eq. 1 (Fardeau, 1996), where m and n are statistical parameters, $P_w$ [mg kg$^{-1}$] is water-extractable P, $r_{iso}$ is the radioactivity measured in solution after an infinite time and R is the radioactivity [Bq] introduced at t=0.

$$E(t) = P_w \cdot \left(1 \frac{1}{m(n+1)} \frac{e^{-mt}}{n+1} + \frac{t_{iso}}{R} \right)$$

The ratio $\frac{t_{iso}}{R}$ is usually approximated as $\frac{P_{iso}}{P_{inorg}}$, where $P_{inorg}$ is the total amount of inorganic P [mg kg$^{-1}$] (Fardeau, 1993). The parameters m and n describe the rapid and slow physicochemical exchange processes, respectively, and are determined by fitting a non-linear regression model to measurements of radioisotope concentration in solution from an isotope exchange kinetic experiment (for details see Fardeau et al. 1991 and Frossard et al. 2011).
By plugging in different values of $t$ [min], one can calculate the amount of $P$ that is exchangeable within a given time frame. Likewise, it is possible to calculate the amount of $P$ exchangeable between two time points, e.g. between one day and 3 months (Frossard et al., 2011). While isotope exchange kinetic experiments used to fit $m$ and $n$ only last for around 90 minutes, extrapolated $E$-values have been shown to describe $P$ exchange well over a time span of months, accurately describing $P$ available to plants and being considered the gold-standard for measuring $P$ availability (Frossard et al., 1994; Hamon et al., 2002). Furthermore, $E(t_{\text{min}})$ has been shown to correlate with resin-$P$, $E(t_{\text{months}})$ with NaOH-$P$ and $E(t_{>3\text{months}})$ with HCl-$P$ in sewage sludge (Frossard et al., 1996) and for soils from a Hawaiian climatic gradient (Helfenstein et al., 2018a).

To estimate mean residence times of sequential extraction pools, we plugged in $P$ pool values as measured by sequential extraction ($P_{\text{pool}}$) for $E(t)$ (Eq. 2), and then solved for $t$ to determine the amount of time necessary to exchange all the phosphate ions contained in that pool (Eq. 3).

$$P_{\text{pool}} = P_w \cdot \frac{1}{m(t_m^n)} \cdot \frac{P_w}{P_{\text{narg}}}$$  \hspace{1cm} (2)

$$t = \left( \frac{P_w}{P_{\text{pool}}} \cdot \frac{P_w}{P_{\text{narg}}} \right)^{-\frac{1}{n}} \cdot \frac{1}{m} = MRT$$  \hspace{1cm} (3)

MRT of resin-$P$ and labile $P$ was calculated using Eq. (3) and plugging in resin-$P$ or labile-$P$ pool sizes for $P_{\text{pool}}$. To calculate MRT of NaOH-$P$ and HCl-$P$, the $P_{\text{pool}}$ was set equal to the sum of labile-$P$ and NaOH-$P$ or labile-$P$, NaOH-$P$, and HCl-$P$ respectively (Fig. 1b). The summation of more labile pools to estimate MRT of more recalcitrant pools is necessary because in this model “slow” exchanging pools can only exchange once “faster” exchanging pools have fully exchanged.

Estimating MRT using Eq. (3) required making several assumptions. Firstly, we assumed that the labile pool exchanges much faster than NaOH-$P$ pool, which again exchanges much faster than HCl-$P$. This assumption rests on the observation that radioisotope specific activity after labeling is higher in resin-$P >>$ NaOH-$P >>$ HCl-$P$ in a variety of soils (Buehler et al., 2002; Bünemann et al., 2004; Daroub et al., 2000; Pistocchi et al., 2018; Vu et al., 2010). Secondly, we assumed that all $P$ transformations occur via the soil solution, i.e. we neglected potential exchange between pools in the solid phase (such as diffusive penetration, Fig 1a) (Barrow and Debnath, 2014). For example, we did not consider exchange between NaOH-$P$ and “occluded” soil $P$ forms, considered in some modelling approaches (Hou et al., 2019), but which do not involve phosphate release to the soil solution.

Thirdly, our approach carries over all assumptions from an isotope exchange kinetic experiment (Frossard et al., 2011), including that biological activity does not markedly impact $P$ exchange during the duration of an isotope exchange kinetic experiment (usually 90 minutes). The assumption that biological activity is negligible at this time scale can be tested by
applying a microbial inhibitor to the soil suspension (Bünemann et al., 2012). If the microbial inhibitor does not significantly affect radioisotopic recovery compared to the control, biological processes have a negligible effect. Microbial inhibitors did not affect radioisotopic recovery of soils from the Hawaiian climatic gradient or soils from the forested geosequence (only extreme soils tested, including a very low P soil) used in this study (Bünemann et al., 2016; Helfenstein et al., 2018a). However, for the other studies analyzed here, no such tests were undertaken. Hence, our approach can only be used to estimate MRT of P in inorganic P pools turning over by physicochemical processes, but does not account for biological processes. In our analysis, we also do not consider the residual P pool (P remaining in soil after the HCl-extraction), assuming that this pool only plays a negligible role in P exchange.

2.3 Effect of soil properties on mean residence times

To determine the effect of soil properties on MRT we performed multiple regression, in which independent soil properties were the explanatory variables and MRTs the response variables. Multiple regression models were fitted to the three response variables “t_labile”, “t_NaOH”, and “t_HCl”. For each response variable, we derived a maximum scope model including all numerical soil properties (pH, soil texture, and organic C) and climatic data as well as categorical explanatory variables “land use” and “extraction method”. Different studies used slightly different extraction methods, the effect of this on the variability was explored using the “extraction method” variable. Additionally, we tested the correlation of MRTs with oxalate or dithionite-extractable aluminum and iron as a simple regression for the samples (n=41-43) for which this data was available. The R function “step” (R Core Team, 2018) was then used for stepwise selection of explanatory variables by minimizing Akaike’s information criterion (AIC) (Sakamoto et al., 1986). Model size was reduced to reduce collinearity between predictor variables, as assessed using the Variance Inflation Factor (VIF), which was below 5 for each of the explanatory variable (Fox and Monette, 1992). Non-normally-distributed variables were log-transformed to meet the assumption of normality.

3. Results

3.1 P exchange as a function of time

P pools as defined by sequential extraction displayed highly significant correlations with P pools defined by exchangeability, with most points falling close to the 1:1 line (Fig. 2). Pearson’s moment correlation between labile P and P exchangeable within 1 hour was 0.84, between NaOH-P and P exchangeable between 1 hour and 3 months was 0.94, and between HCl-P and P only exchangeable in time spans longer than 3 months was 0.87.

The soils showed a broad range of P exchange as a function of time. P that was exchangeable within 1 min (E1min) ranged from 0.99 – 218 mg kg⁻¹, and P that was exchangeable in three months from 11.7 to 6311 mg kg⁻¹ between the different soils (Table 1). Soils developed on P-rich basalt (Helfenstein et al., 2018a; Lang et al., 2017) had the highest E-values; while Ferralsols had the lowest E-values (Oberson et al., 1999). Half of the soils had < 5 mg P kg⁻¹ exchangeable within one minute, which is
considered a threshold for low P availability (Gallet et al., 2003). Differences in P exchange behavior were either due to different levels of total inorganic P, or to different P forms present in the soil (Fig 3). For example, a soil with high amounts of inorganic P exchanged more within the same time interval than a soil with low amounts of inorganic P. Similarly, soils with large proportions of HCl-P tended to have lower slopes of E-curves than soils with relatively more labile or NaOH-P. This variability is reflected in the proportion of E_{\text{1min}} to total P, which spanned from 0.04 to 6% of total soil P. Similarly, E_{\text{3months}} represented on average 25% of total soil P, spanning from 4 to 64%.

3.2 Estimates of mean residence times

The median MRT of P in the labile pool was around 1 hour (67 min), for NaOH-P around 1 month (3.4 x 10^4 min), and for HCl-P around three years (1.4 x 10^6 min). However, calculated MRTs of individual soils spanned many orders of magnitude. Mean residence time of P in labile P ranged from 0.4 to 4.4 x 10^3 min, with two frequency maxima, one around one hour and one around one day (Fig. 4). Mean residence time of P in NaOH-P ranged from 91 to 3.4 x 10^6 min, and also had two frequency maxima, one at around 1 day and one at around 3 months. Mean residence time of P in HCl-P had the widest spread, from 129 to 1.7 x 10^15 min. While most soils had a MRT of P in HCl-P around 1 year, another frequency maximum occurred at around 10^4 years. The median MRT of P in resin P (n = 42) was 19 minutes, with a range of 10^{-4} to 10^2 min.

3.3 Soil properties affecting mean residence times

Multiple regression models were able to explain between 54 and 63% of the variability in MRT for each pool (Table 2). The MRT of P in labile P was best predicted by a model including clay and land use (adj. R^2 = 0.63, F-statistic = 30.6, p < 0.001). Land use was the most important predictor of t_{\text{labile}}. A model only including land use had an adj. R^2 of 0.52 (F-statistic 29.6, p < 0.001). While most forest and grassland soils had a MRT of P in labile P around 1 h, arable soils tended to have a longer MRT of around 1 day (Fig. 5a). The land use effect on MRT of P in labile P was not a pool size effect (Fig. 5b). In addition, MRT decreased with increasing clay content (adj. R^2 = 0.12, F-statistic = 6.8, p = 0.01) (Supplementary Fig. 3).

The MRT of P in NaOH-P was best predicted by a model with clay, land use and organic C (adj. R^2 = 0.57, F-statistic = 18.4, p < 0.001). Of those three explanatory variables, the relationship was again strongest with land use. A model only including land use had an adj. R^2 of 0.44 (F-statistic 21.6, p < 0.001). In general, forest soils had a shorter MRT of around 1 day and arable soils a longer MRT of around 3 months. Grassland soils spanned the full range in MRT of P in NaOH-P (Fig. 5c). As for MRT in labile P, the land use effect on MRT was not a pool size effect (Fig. 5d). MRT of P in NaOH-P also decreased with increasing clay content (adj. R^2 = 0.13, F-statistic = 7.1, p < 0.01) (Supplementary Fig. 3). While organic C was also a significant predictor in the multiple regression model, a simple regression between organic C and MRT of NaOH-P was not significant (Supplementary Fig. 4).
The MRT of P in HCl-P was best predicted by a model with clay, pH, and mean annual rainfall (adj. $R^2 = 0.54$, $F$-statistic $= 17.8$, $p < 0.001$). The strongest of these predictors was pH (Fig. 6). MRT of P in HCl-P increased with increasing pH following Eq. (4):

$$\log(t_{HCl}) = -7.95 + 4.63 \cdot (pH)$$

where $t_{HCl}$ is in minutes (adj. $R^2 = 0.47$, $F$-statistic $= 37.7$, $p < 0.001$). Like with the models for labile P and NaOH-P, predicted MRT decreased with increasing clay concentration also for MRT of HCl-P; however, this relationship was not significant as a simple regression (Supplementary Fig. 3).

### 4.1 Discussion

Sequential extraction is probably the most common method used to study P pool distribution in soils. However, the residence time of P in these pools and environmental controls remain poorly understood. While earlier works hypothesized that resin and bicarbonate P have a “fast turnover”, and NaOH and HCl a “slow turnover”, data on MRT of P in these pools for a wide range of soils was previously missing (Cross and Schlesinger, 1995; Tiessen et al., 1984). We found that on average resin-P has a MRT on a range of several minutes, labile of one hour (forest and grassland soils) or one day (arable soils), NaOH-P on a range of days (forest and some grassland soils) to months (arable soils), and HCl-P of years to millennia, with a strong pH dependence. The large variability in MRTs could be partially explained by soil properties, especially pH and clay, or land use, but may also be due to unaccounted soil properties as well as methodological limitations of either our approach or the lab techniques used to produce the original data. For instance, some variability in the MRTs estimation might be generated by the different methods used to measure total inorganic P. The accuracy in total inorganic P measurement might affect MRTs as results from Eq. (2).

As a predictor of MRTs of labile and NaOH-P, land use is likely a proxy for soil P balance (fertilizer inputs, outputs with harvest) and biological activity. Arable soils are more likely to receive P fertilizers. Long-term fertilizers inputs may lead to a decrease in surface charge resulting from diffusive penetration of P into the reacting materials, and therefore to a lower phosphate buffering capacity (Barrow and Debnath, 2014). Hence, fertilizer application may lead to larger P pool sizes but longer MRT (Helfenstein et al., 2018b). Biological activity has been shown to accelerate P turnover in the labile pool through the rapid uptake and release by the soil microbial community (Oehl et al., 2001; Pistocchi et al., 2018; Weiner et al., 2018). This holds especially true under grassland or forest and under low P availability. We consider the later explanation less likely, since microbial uptake/release tends to be negligible during the isotopic exchange kinetic experiments (Oehl et al., 2001) or it is suppressed using microbial inhibitors (Bünemann et al., 2012). However, we cannot completely rule out such an influence as in most soil samples included in our data-set this effect was not systematically tested.
The pH dependence of MRT in HCl-P is likely because the composition of the HCl pool varies strongly with pH. Under high pH, the HCl pool tends to contain apatites, Ca-P minerals which are highly stable (Moir and Tiessen, 1993; Nriagu, 1976). Our results predict that under such conditions, MRT of HCl-P may be on the order of millennia or longer, orders of magnitude longer than estimated MRTs of NaOH-P. In acidic soils on the other hand, apatite is much less stable (Guidry and Mackenzie, 2003), and the HCl pool may contain either carry-over from the NaOH pool or other phosphates that are more reactive (Prietzel et al., 2016). Eq. (4) predicts a MRT in HCl-P of ¾ year for a soil with pH 4.5, a range into which also MRT of many NaOH-P pools falls. Hence, our results suggest that the exchange kinetics of NaOH and HCl pools are more similar under low pH conditions, whereas under high pH conditions, there seems to be a clear distinction between availability of NaOH-extractable P and HCl-extractable P. Nevertheless, even under neutral to alkaline conditions, HCl-P pool may be involved in bi-directional exchange of phosphate involving precipitation of phosphate with Ca to form secondary Ca-phosphates (Frossard et al., 1995). Also, using stable oxygen isotopes in phosphate, it was shown that in 150'000 year old soils from arid conditions and neutral pH, roughly half of the HCl-P pool contained secondary phosphates (Helfenstein et al., 2018a). The relationship of pH and other relationships, e.g. land use as a predictor for t_labile and t_NaOH, pertained if the outliers “Himatangi”, “Hurundi”, “Okarito”, and “Temuka” were included in the multiple regression analyses; however, including the outliers reduced overall model adj. R² to around 0.4 for all three models.

Clays are important binding sites for P (Gérard, 2016). Our data seem to show that the clay content influences residence times not only of labile-P, but also of the NaOH and HCl pools. In our analysis, the clay variable includes not only clay minerals but also secondary minerals such Fe and Al oxyhydroxides, as it follows the particles size classification. Fe and Al oxyhydroxides are known to be key in inorganic P exchange behavior (Achat et al., 2016; Syers et al., 2008). For the samples where data on oxalate- and dithionite-extractable Al and Fe was available (n = 41-43), simple regression showed only weak correlations with MRTs, and only significance for MRT of NaOH-P with oxalate-extractable Al, dithionite-extractable Fe and the sum of dithionite-extractable Al and Fe as explanatory variables (adj. R² ≤ 0.16, p < 0.05, data not shown). In general, soil properties controlling P sorption also control P exchangeability and therefore residence time. Indeed, high amounts of P-sorbents might relate to more rapidly exchangeable P (Achat et al., 2016; Demaria et al., 2013). The variety of mechanisms involved in P binding on such soil surfaces (multi-layer sorption, inner-sphere complexes, surface precipitation, see Gérard 2016 and references therein) might explain why the effect of clay is significant for all residence times.

Data from long-term (weeks-months) radioisotope tracer incubation experiments, where both physicochemical and biological processes are considered, support our estimates of MRTs. While such studies have not reported estimates of MRTs, the time by which specific activity of 32P of the NaOH or HCl pool equilibrates with the specific activity of the labile P pool provides an estimate of MRT of the slowest pool, i.e. the time needed to exchange all the phosphate ions located in the slowest pool with the ones in the soil solution. According to this assumption and using the data published by Buehler et al. (2002) from the
same Ferralsols also included in our dataset, we could estimate a MRT of the NaOH pool between 7 and 14 days (soils under savanna and pasture) or longer than two weeks (two soils under rice). These values are similar to MRTs from our study: 1 and 5 days for the soils under savanna and pasture, respectively, and 28 and 88 days for the soils under rice. Generally, specific activity of $^{33}$P in HCl pool did not equilibrate during the duration of the experiment (two weeks to three months, depending on the study), suggesting longer MRTs for this pool (Buehler et al., 2002; Bünemann et al., 2004; Pistocchi et al., 2018; Vu et al., 2010). Nevertheless, for stable pools such as the HCl-P, it is questionable whether our estimates of MRTs are realistic, as the extrapolation of E-values (Eq. 1) has been tested only over time spans of days to months (Bünemann et al., 2007; Frossard et al., 1994) and is impossible to validate for longer time spans due to the short half-lives of both radioactive P isotopes.

**Insights from stable oxygen isotope analysis support our estimates of MRT of HCl-P.** At the beginning of soil development, all soil P has the parent material stable oxygen isotope value ($\delta^{18}$O$_P$) (Roberts et al., 2015; Tamburini et al., 2012). With time, biological activity brings $\delta^{18}$O$_P$ into steady-state with soil water (Blake et al., 2005). By analyzing $\delta^{18}$O$_P$ in sequentially-extracted pools in soils of known age, it is possible to roughly constrain MRT of P in these pools. While $\delta^{18}$O$_P$ of bicarbonate- and NaOH-extractable P tend to be in the soil-water steady-state (Helfenstein et al., 2018a; Roberts et al., 2015), HCl-P may retain parent material signature even in older soils. In a chronosequence on granitic parent material, it was shown that the HCl pool acquired the biological signature after several thousand years (Tamburini et al., 2012), whereas under more arid conditions, where apatite remains stable, HCl-P may not have turned over completely even after 150'000 years of soil development (Helfenstein et al., 2018a). This supports not only our long and variable estimates of MRTs of P in the HCl-P, but also their strong dependence on pH, the main driver of apatite stability.

**4.2 Limitations**

The main limitations of our study concern representativity of the soil samples used and uncertainty introduced due to assumptions taken to calculate MRTs. The 53 soils samples used in our study only came from a small number of studies, and some soils, like Andosols and Cambisols, were overrepresented in our study, while other important soils such as Vertisols, Podzols, or carbonate or organic matter-rich soil orders were not under represented. In addition, soils with large amounts of NaOH- and HCl-P were overrepresented in our study compared to a larger global data set (Supplementary Fig. 5). However, our resin P values closely match resin P frequency distribution of a larger global dataset (Hou et al., 2018a). In terms of P exchange kinetics, our soils covered the full range of reported m and n values, and can thus be considered to reflect the full range of P exchange kinetic properties observed in soils (Supplementary Fig. 6) (Achat et al., 2016; Helfenstein et al., 2018b).

Assumptions taken to calculate MRT of P in soil P pools required making several simplifications. Our approach only considers a simplified system of soil and water in steady-state conditions, and excludes biological activity. In field conditions, P residence times may be different due to non-steady state conditions, microbial interactions with abiotic processes, as well as plant uptake and alterations of the physical and chemical soil environment (Hinsinger, 2001). For example, intensive P uptake by plants
may lead to net changes in soil P pools in addition to exchange fluxes (Guo et al., 2000). Also, it is likely that MRTs are affected by temperature and changes in soil moisture. Continued improvement of tracer experiments is paramount to provide empirical data on mean residence times and magnitudes of biological and physicochemical fluxes (Bünemann, 2015; Wanek et al., 2019). However, for the time being, our ad hoc approach provides preliminary estimates of mean residence times of commonly used P pools, with the potential to improve both interpretation of lab-and field scale results as well as land surface modelling.

### 4.3 Implications for lab- and field-scale research

Mean residence times of P in inorganic soil P pools we report are important for improved understanding of P dynamics in soil. Sequential extraction continues to be widely used to measure soil P status, for example to study effects of land use change and P inputs or environmental drivers on soil P cycling (Blake et al., 2003; Feng et al., 2016; von Sperber et al., 2017). Understanding the residence times of soil P pools will allow fine-tuning hypotheses of expected changes and improve interpretation of observed changes in pool sizes. Furthermore, analysis of stable oxygen isotopes in phosphate, which is gaining importance as a tracer of phosphate transformation and indicator of biological vs. geochemical P cycling, is tightly linked to sequential extraction (Tamburini et al., 2018). Knowledge of mean residence times has the potential to improve interpretation of sequential extractions and derivate methods.

### 4.4 Implications for land surface modelling

Our study allows drawing several conclusions important for future P representations in land surface models. Firstly, we show that current LSM largely overestimate MRTs of P in inorganic soil P pools. As models do not report all information needed to calculate MRT, we approximate modelled P pool MRT (in the following: MRT*) of the intermediate and slow pool as the inverse of the decay rate assuming the pool size and fluxes are in equilibrium (i.e. net losses = net gains). Juxtaposing our estimates of MRTs of P in inorganic soil P pools with values used in existing land surface models shows that existing land surface models underestimate inorganic P turnover by several orders of magnitude (Table 3). While our estimates of the mean residence times of the NaOH pool are on the range of months to years, existing models run with MRT*s of these pools of decades to centuries (Table 3). The discrepancy between our estimates and existing model values is so large and consistent among models that it is unlikely due to slightly different conceptualizations of the P cycle or the approximation of MRT in models by decay rates. Rather, the overestimation of the stability of inorganic P pools in existing LSM is likely due to the calibration of models using net changes to inorganic soil P pools (Goll et al., 2017; Hou et al., 2019). As the P exchange among two given pools is most often two-way, the calibration of residence times on the net exchange must lead to an underestimation of P turnover. The data provided here will allow to better calibrate soil P dynamics and/or evaluate modelled MRT.

4.5 Historical perspectives and future directions

Continued improvement of tracer experiments is paramount to provide empirical data on mean residence times and magnitudes of biological and physicochemical fluxes (Bünemann, 2015; Wanek et al., 2019). The representations of inorganic soil phosphorus dynamics are currently very rudimentary in such models: soil inorganic phosphorus is commonly separated into different pools according to differences in residence times (fast, intermediate and slow pools) (Wang et al., 2010). Although the structure, i.e. number of soil P pools and the connection among pools, differs among models, they commonly apply the same concept. In the considered land surface models, the residence time of P in the fastest pool is modelled as a function of multiple abiotic (chemical weathering, sorption) and biotic (mineralization, immobilization, plant uptake, phosphatase activity) processes (Lloyd et al., 2001), while more recalcitrant pools have prescribed globally uniform decay rates (first order decay). The decay rates are either derived from calibration to achieve plausible total soil P stocks (Goll et al., 2012; Wang et al., 2010; Yang et al., 2014), or derived from observed changes in soil P fraction along a single soil chronosequence (Goll et al., 2017). The representations of inorganic soil phosphorus commonly apply the same concept. In the considered land surface models, the residence time of P in the fastest pool is modelled as a function of multiple abiotic (chemical weathering, sorption) and biotic (mineralization, immobilization, plant uptake, phosphatase activity) processes (Lloyd et al., 2001), while more recalcitrant pools have prescribed globally uniform decay rates (first order decay). The decay rates are either derived from calibration to achieve plausible total soil P stocks (Goll et al., 2012; Wang et al., 2010; Yang et al., 2014), or derived from observed changes in soil P fraction along a single soil chronosequence (Goll et al., 2017).
Secondly, we found that residence times of P in slow inorganic pools varies considerably between soils, suggesting that land surface models should account for existing knowledge of P pool stability under different soil and environment conditions, rather than assuming globally uniform mean residence times. We found variation over several orders of magnitude in mean residence times of the same pool between different soils, and this variation could partly be explained by secondary soil and environment variables.

Thirdly, land surface models should consider that HCl-P pool may have two-way exchange of P. Current model formulations assume the HCl-P pool contains only primary apatite, and the flux between the HCl-P pool and the soil solution is one-way (only dissolution) (Hou et al., 2019; Yang et al., 2014; Yu et al., 2018). From empirical observations it is known that HCl-P does not only contain primary apatite but may also contain secondary P minerals (Frossard et al., 1995; Helfenstein et al., 2018a; Tamburini et al., 2012). Under acidic conditions, this may be Fe- and Al-associated minerals, while under neutral and alkaline pH this may be precipitated Ca-phosphates (Frossard et al., 1995). Also, P radioisotope transfer from the soil solution to the HCl-P pool is well-documented (Buehler et al., 2002; Pistocchi et al., 2018). To take this into account, future P model formulation should consider a two-way flux between the HCl-P pool and the soil solution, with an exchange rate dependent on pH (see Eq. 4). While this change is likely to have limited impact for the modelling of neutral to alkaline soils, where the HCl-P pool is stable, in more acidic soils the HCl-P pool tends to have similar dynamics to the NaOH-P pool, thus having considerable impact on P cycling.

In conclusion, mean residence times for inorganic P pools proposed here and the lessons learned should help improve model formulation of P in land surface models. Our estimates of MRTs suggest that current land surface models overestimate P MRT in inorganic soil P pools and as a consequence might overestimate the importance of biological soil P transformation (e.g. via phosphatases). Also, the temporal dynamics of P pools was found to vary largely between different soil types, which is not captured by models. Finally, model formulations should refrain from equating HCl-P to primary P, as this pool often contains secondary P minerals and is relatively dynamic in low pH soils. More empirical data on soil P pool mean residence times is needed, also from soil-plant systems and field experiments, but our data provides the basis to start building data-constrained soil P models.

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References


Figure 1. Conceptual diagram showing: a) how Hedley P pools exchanges with the soil solution; b) how mean residence time was calculated. E(t) shows the amount of phosphate that has passed through the soil solution as a function of time.
Figure 2. Correlation between chemically extracted pools and isotopically exchangeable P. Resin and NaHCO$_3$-extractable P correlated with P exchangeable in 1 hour (E 1 hour) (a), NaOH-extractable P with P exchangeable between 1 hour and 3 months (b), and HCl-extractable P with P only exchangeable in over three months (c). Units of both axes are log(mg P kg$^{-1}$). Dotted line shows the 1:1 line. Pearson’s product-moment correlation ($r$ value on plot) was highly significant ($p < 0.001$) for all three correlations.
Figure 3. Examples of exchangeable P as a function of time (E-curves). Grey lines show E-curves of each soil in the dataset. Panels (a) and (b) highlight two highly-reactive soils, one with high amounts of P (an Andosol from Helfenstein et al., 2018a) and one with little P (a Ferralsol from Oberson et al., 1999). (a) Shows the E-curves and (b) the corresponding sequential extraction (b). Panels (c) and (d) highlight two soils with similar amounts of total P, but different pH and P exchange behavior. For the high pH Fluvisol (pH = 8.1, from Borda et al., 2014), P-exchange is slow, compared to a Cambisol with much more exchange on the fast-intermediate term (pH = 3.8, from Lang et al., 2016) (c). In the high pH soil most P is HCl-extractable, whereas for the low pH soil more P is found in the NaOH and labile pools (d).
Figure 4. Distribution of mean residence times of P in labile, NaOH and HCl pools for 53 soils. The black bars show a boxplot and the colored area shows the kernel density distribution.
Figure 5. Mean residence time (MRT) of P (a, c) and pool size (b, d) as a function of land use. Both MRT of P in labile P (a) and NaOH-P (c) was significantly affected by land use.
Figure 6. Simple regression of calculated mean residence time of P in HCl-P with pH. $F$-statistic = 37.7, $p < 0.001$. 

$R^2 = 0.47$
Table 1. Selected soil properties, climate conditions, soil phosphorus pools, and phosphorus exchange kinetic properties of soils used in this study.

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<td>32.40</td>
<td>37.47</td>
<td>170.72</td>
<td>53</td>
</tr>
<tr>
<td></td>
<td>NaOH-extractable P [mg kg⁻¹]</td>
<td>1.5</td>
<td>48.0</td>
<td>99.4</td>
<td>744.6</td>
<td>470.4</td>
<td>9547.8</td>
<td>53</td>
</tr>
<tr>
<td>P exchange kinetics</td>
<td>HCl-extractable P [mg kg⁻¹]</td>
<td>1.0</td>
<td>34.5</td>
<td>162.5</td>
<td>433.1</td>
<td>557.5</td>
<td>4040.7</td>
<td>50</td>
</tr>
<tr>
<td></td>
<td>Pw water-extractable P [mg kg⁻¹]</td>
<td>0.013</td>
<td>0.328</td>
<td>1.00</td>
<td>3.782</td>
<td>2.6</td>
<td>42.5</td>
<td>53</td>
</tr>
<tr>
<td></td>
<td>m exchange parameter</td>
<td>0.01</td>
<td>0.06</td>
<td>0.15</td>
<td>0.26</td>
<td>0.38</td>
<td>0.97</td>
<td>53</td>
</tr>
<tr>
<td></td>
<td>n exchange parameter</td>
<td>0.03</td>
<td>0.40</td>
<td>0.46</td>
<td>0.45</td>
<td>0.50</td>
<td>0.76</td>
<td>53</td>
</tr>
</tbody>
</table>
Table 2. Multiple regression models for mean residence times of P in labile P, NaOH-extractable P, and HCl-P. Models were determined by a step-wise selection process that maximizes Akaike’s Information Criterion.

<table>
<thead>
<tr>
<th>response variable</th>
<th>multiple regression model</th>
<th>adjusted $R^2$</th>
<th>$F$-statistic</th>
<th>significance level</th>
</tr>
</thead>
<tbody>
<tr>
<td>t_labile</td>
<td>log(t_labile) = 8.92 - 0.07 (clay) + (land use)(^a)</td>
<td>0.63</td>
<td>30.6</td>
<td>&lt; 0.001</td>
</tr>
<tr>
<td>t_NaOH</td>
<td>log(t_NaOH) = 11.6 - 0.09 (clay) + 0.80 log(Corg) + (land use)(^b)</td>
<td>0.57</td>
<td>18.4</td>
<td>&lt; 0.001</td>
</tr>
<tr>
<td>t_HCl</td>
<td>log(t_HCl) = -12.9 + 5.23 (pH) - 0.21 (clay) + 5.2 x 10(^{-3}) (mean.rainfall)</td>
<td>0.54</td>
<td>17.8</td>
<td>&lt; 0.001</td>
</tr>
</tbody>
</table>

\(^a\) for arable = 0; for forest = -3.08; for grassland = -3.78

\(^b\) for arable = 0; for forest = -5.94; for grassland = -1.81
Table 3. Mean residence times of different soils calculated in this study compared to values used in land surface models. Mean residence times of the resin and labile (resin + bicarbonate) P pools are displayed in minutes, while mean residence times of the NaOH and HCl P pools are displayed in years. Residence times of the listed models were extracted from the literature or by contacting respective authors (Wang et al. 2010; Goll et al. 2012; Yang et al. 2014; Zhu et al. 2016; Goll et al. 2017).

<table>
<thead>
<tr>
<th>Soil order</th>
<th>Resin P [min]</th>
<th>Labile P [min]</th>
<th>NaOH-P [yr]</th>
<th>HCl-P [yr]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mean</td>
<td>sd</td>
<td>median</td>
<td>n</td>
</tr>
<tr>
<td>Acrisols</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Andosols</td>
<td>16.0</td>
<td>19.8</td>
<td>7.1</td>
<td>12</td>
</tr>
<tr>
<td>Cambisols</td>
<td>33.9</td>
<td>42.6</td>
<td>22.4</td>
<td>14</td>
</tr>
<tr>
<td>Ferralsols</td>
<td>6.1</td>
<td>4.5</td>
<td>5.2</td>
<td>7</td>
</tr>
<tr>
<td>Fluvicols</td>
<td>116.6</td>
<td>101.8</td>
<td>85.8</td>
<td>4</td>
</tr>
<tr>
<td>Luvisols</td>
<td>78.7</td>
<td>28.2</td>
<td>63.5</td>
<td>5</td>
</tr>
<tr>
<td>All soils</td>
<td>37.4</td>
<td>51.4</td>
<td>19.0</td>
<td>42</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Models</th>
<th>Plant-available / fast pool [min]</th>
<th>Intermediate pool [yr]</th>
<th>Slow pool [yr]</th>
</tr>
</thead>
<tbody>
<tr>
<td>CABLE</td>
<td>variable, dynamic equilibrium</td>
<td>150</td>
<td>150</td>
</tr>
<tr>
<td>JSBACH</td>
<td>variable, dynamic equilibrium</td>
<td>150</td>
<td>-</td>
</tr>
<tr>
<td>ELM-CTC</td>
<td>variable, dynamic equilibrium</td>
<td>21-83</td>
<td>8.3 x 10^4</td>
</tr>
<tr>
<td>ELM-ECA</td>
<td>variable, dynamic equilibrium</td>
<td>-</td>
<td>8.3 x 10^4</td>
</tr>
<tr>
<td>ORCHIDEE-NP</td>
<td>variable, dynamic equilibrium</td>
<td>25</td>
<td>-</td>
</tr>
</tbody>
</table>

*Resin and bicarbonate extractable P.