Simulating the growth and distribution of planktic foraminifer using an ecophysiological multi-species model

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Received: 6 October 2010 – Accepted: 14 December 2010 – Published: 4 January 2011

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Published by Copernicus Publications on behalf of the European Geosciences Union.
Abstract

We present an eco-physiological model reproducing the growth of eight foraminifer species (Neogloboquadrina pachyderma, Neogloboquadrina incompta, Neogloboquadrina dutertrei, Globigerina bulloides, Globigerinoides ruber, Globigerinoides sacculifer, Globigerinella siphonifera and Orbulina universa). By using the main physiological rates of foraminifers (nutrition, respiration, symbiotic photosynthesis), this model estimates their growth as a function of temperature, light availability, and food concentration. Model parameters are directly derived or calibrated from experimental observations and only the influence of food concentration (estimated via chl-a concentration) was calibrated against field observations. Growth rates estimated from the model show positive correlation with observed abundance from plankton net data suggesting close coupling between individual and assemblage growth rates. This observation was used to directly estimate potential abundance from the model-derived growth. Using satellite data, the model simulate the dominant foraminifer with a 70.5% efficiency when compared to a data set of 576 field observations worldwide. Using outputs of a biogeochemical model of the global ocean (PISCES) instead of satellite images as forcing variables gives also good results, but with lower efficiency (58.9%). The model also correctly reproduces the relative worldwide abundance and the diversity of the eight species when compared to core tops observations both using satellite and PISCES data. This model allows prediction of the season and water depth at which each species has its highest growth potential. This offers promising perspectives for both an improved quantification of paleoceanographic reconstructions and for a better understanding of the foraminiferal role in the marine carbon cycle.

1 Introduction

Planktic foraminifers occur at low abundance in marine waters compared to both protozoans and zooplankton (e.g., Albaina and Irigoien, 2007). After gametogenesis or
death of the organism, their calcite tests sink through the water column with high sinking rates (Takahashi and Bé, 1984), and accumulate at the sea floor, contributing significantly to the marine carbonate flux (Schiebel, 2002). Fossil shells are commonly used in paleoceanography to reconstruct past climatic conditions and variability through the use of different proxies such as species assemblage composition or shell chemistry (e.g., Waelbroeck et al., 2009). However, interpretation of these proxies requires a precise knowledge of the environmental conditions (season and/or depth) of shell calcification. Unfortunately, environmental and biological studies cover only a small geographic range of the world ocean (e.g., Field, 2004; Schiebel et al., 2001) and laboratory observations are scarce (Bijma et al., 1990). The observed composition of the analysed shells is explained on the basis of a statistical comparison between modern surface hydrology and shells extracted from sediment core tops (Imbrie and Kipp, 1971; Kucera et al., 2005b) without consideration of biological mechanisms such as seasonality or potential deeper habitat in the water column (e.g., Cleroux et al., 2007; King and Howard, 2005).

Planktic foraminiferal seasonality and depth preferences in the ocean waters, as well as growth under laboratory conditions, are strongly linked to environmental conditions, mainly temperature, light (for species with symbionts) and food availability (Bijma et al., 1990; Kuroyanagi and Kawahata, 2004; Lombard et al., 2009b; Schiebel et al., 2001; Spero and Parker, 1985). Thus the physiological adaptation of the different species may explain, in part, the environmental range under which each species exhibits an optimal growth (Lombard et al., 2009b), as well as their seasonal and vertical distribution. The environmental control of foraminifer physiology may be described by a model, which takes into account the sensitivity of each physiological process with respect to various environmental factors. In the past years, several models of foraminifers abundance have been developed based on environmental parameters (Fraile et al., 2008; Žarić et al., 2006). Recently, Fraile et al. (2008) presented a model simulating the abundance of six different species, using parameters which have been calibrated empirically together by field measurements.
In this study, we used a physiological formulation to model the growth of foraminifers for the most abundant planktic foraminifer species living in the ocean surface and subsurface waters. The presented FORAMCLIM growth model is based on the assumption that the presence or absence of species is linked to their ability to grow, depending on the environmental conditions. The model reproduces the physiological rates involved in the growth of planktic foraminifers, based on metabolic processes observed under controlled laboratory experiments. The calibration has been made following two steps: first we attempt to reproduce observed growth under laboratory conditions as a function of temperature and light intensity. Second, we attempt to reproduce observed abundance in field conditions, for which hydrological parameters have been measured. The model has been validated against both global plankton tows and sediment core tops observations independent of the dataset used for the calibration. The model reproduces the relative abundances of the different species on a global scale, and the season and depth of the maximal growth potential of each species is estimated.

2 General growth model conception and calibration

In the first part, we will present the model, which describes the growth of an individual foraminifer. Construction of the growth model is based on observed processes during laboratory experiments or observations and is kept as simple as possible by taking in consideration only well calibrated processes. Eight planktic foraminiferal species are considered: Neogloboquadrina pachyderma (sinistral), Neogloboquadrina incompta (N. pachyderma dextral cf. Darling et al., 2006), Neogloboquadrina dutertrei, Globigerina bulloides, Globigerinoides ruber, Globigerinoides sacculifer, Globigerinella siphonifera and Orbulina universa. The species are among the most abundant species in the marine ecosystem and are most used in both laboratory experiments and paleoclimate reconstruction.
2.1 Individual foraminifer growth

The model simulates the growth of the foraminiferal organic component, but does not yet consider test growth. The growth model simulates foraminifer organic weight increase \( \Delta W, \mu g \text{ C d}^{-1} \) as a function of the main physiological processes: nutrition \( (N, \mu g \text{ C d}^{-1}) \), respiration \( (R, \mu g \text{ C d}^{-1}) \) and, for species with symbionts, photosynthesis \( (P, \mu g \text{ C d}^{-1}) \). Those processes depend on variables like temperature \( (T, ^\circ \text{K}) \), light availability \( (L, \mu \text{mole photon m}^{-2} \text{s}^{-1}) \) and food concentration \( (F, \mu g \text{ C l}^{-1}) \). Variables, processes, parameters and units are described in Table 1.

2.1.1 Nutrition

Foraminifers are poikilotherms protozoans and thus do not regulate their temperature. Poikilotherms feeding processes such as the speed of prey capture and digestion generally depend on water temperature (Kooijman, 2000). Moreover, at extreme low or high temperatures, a sharp decrease in the growth rates is observed in foraminifers (Bijma et al., 1990; Lombard et al., 2009b). Moreover, Bé et al. (1981) have shown that the growth rate of \( G. \text{sacculifer} \) is a saturating function of feeding frequency. In the model we assume this saturation of feeding as a function of food availability using Michaelis-Menten kinetics and depend on temperature following a mechanistic formulation derived from Arrhenius rate kinetics. We use the following relationship to describe the nutrition rate \( N \) as a function of temperature \( T \) (in Kelvin) and food concentration \( (F) \):

\[
N(T, F) = N_{\text{max}}(T_1) \frac{\exp\left(\frac{T_A}{T_1} - \frac{T_A}{T}\right)}{1 + \exp\left(\frac{T_{AL}}{T} - \frac{T_{AL}}{T_L}\right) + \exp\left(\frac{T_{AH}}{T} - \frac{T_{AH}}{T_H}\right)} \frac{F}{F + k_n}
\]  

(1)

where \( k_n (\mu g \text{ C l}^{-1}) \) is the half saturation constant for the Michaelis-Menten relationships; \( N_{\text{max}}(T_1) (\mu g \text{ C d}^{-1}) \) is the maximum nutrition rate for an arbitrary chosen temperature \( T_1 (20 ^\circ \text{C or 293 } ^\circ \text{K in this study}) \); \( T_A \) is the Arrhenius temperature for nutrition
rate; $T_L$ and $T_H$ are the lower and upper boundaries of the enzymes tolerance range and $T_{AL}$ and $T_{AH}$ are the Arrhenius temperatures for the rate of decrease at both boundaries. All $T$ are taken to be positive and generally $T_{AH}>T_{AL}>T_A$. By using this relationship the model reproduces simultaneously the nutrition saturation at high food concentration, the nutrition increase with temperature, and a sharp decrease of growth observed for extreme temperatures, which results in an asymmetrical bell shaped curve (Lombard et al., 2009b).

### 2.1.2 Photosynthesis and respiration

Photosynthesis is carried out by symbionts and therefore depends on the number of symbionts hosted by the foraminifer. Thus photosynthesis is calculated on a per symbiont basis multiplied by the symbiont number of a 250 µm sized foraminifer ($s_{nb}$). Photosynthesis also depends on light availability ($L$, µmole photon m$^{-2}$ s$^{-1}$) and reaches saturation for high light intensities (Jørgensen et al., 1985; Köhler-Rink and Kühl, 2005; Spero and Parker, 1985). The model reproduces this process by using a Michaelis-Menten relationship as a function of the light availability. Warming also increases the photosynthesis rate following an Arrhenius kinetics (Lombard et al., 2009a). The combined effect of light intensity and temperature can thus be estimated as:

$$P(T,L) = s_{nb}P_{max}(T_1)\exp\left(\frac{T_{Ap}}{T_1} - \frac{T_{Ap}}{T}\right) \frac{L}{L + k_p}$$  \hspace{1cm} (2)

where $k_p$ (µmole photon m$^{-2}$ s$^{-1}$) is the half saturation constant for the Michaelis-Menten relationships; $P_{max}(T_1)$ (µg C d$^{-1}$) is the maximum photosynthesis rate per symbiont for the arbitrarily chosen temperature $T_1$ and $T_{Ap}$ ($^\circ$K) is the Arrhenius temperature for photosynthesis rate.
In a similar way, foraminifer respiration increases with temperature following an Arrhenius kinetics (Lombard et al., 2009a) and respiration can be defined as:

\[ R(T) = R(T_1) \exp \left( \frac{T_{\text{Ar}}}{T_1} - \frac{T_{\text{Ar}}}{T} \right) \]  

(3)

where \( R(T_1) \) (µg C d\(^{-1}\)) is the respiration rate for a 250 µm sized foraminifer at the arbitrary chosen temperature \( T_1 \) and \( T_{\text{Ar}} (\degree K) \) is the Arrhenius temperature for respiration rate.

### 2.1.3 Foraminifer growth

To simulate the growth rate, all species are defined with the same initial organic weight \( W_i; 0.73 \text{ µg C} \) corresponding to a 250 µm sized foraminifer (Michaels et al., 1995). This foraminifer size was chosen in order to correspond to most growth and physiological rate observations in laboratory experiments. The final organic weight \( W_f \) is then simulated by the model on a daily basis by taking into account the foraminifer ecophysiology (respiration, photosynthesis, and nutrition) for a \( W_i \) weight.

In case of symbiont bearing foraminifers, the model simulates growth of the symbiont/foraminifer complex, without differentiation between symbiont and foraminifer growths.

Photosynthesis only takes place during day length \( (\text{dl}, \text{d}^{-1}) \) and we hypothesise that only a fraction \( (\%_p) \) of the symbiont photosynthesis potentially contributes to the growth of the foraminifer/symbiont complex (Lombard et al., 2009a). The weight increment \( \Delta W \), which serves to calculate \( W_f \) is calculated on a daily basis such as:

\[ \Delta W = N + \%_p \text{dlP} - R \]  

(4)

The growth rate \( (\mu, \text{d}^{-1}) \) is calculated on a daily basis assuming an exponential growth of foraminifer organic content and using the following formulation:

\[ \mu = \ln\left(\frac{W_f}{W_i}\right) \]  

(5)
2.1.4 Data from culture experiments and growth model calibration

Parameters are listed and described in Table 1, and values taken either from bibliography or from calibration are listed in Table 2. Because temperature have a similar effect among species on respiration and photosynthesis, parameters \( R(T_1) \), \( T_{Ap} \) and \( T_{Ar} \) are directly issued from Lombard et al. (2009a) and are assumed to be the same for all species. Symbiont number \((s_{nb})\) for a 250 µm size for *O. universa* and *G. siphonifera* were estimated in Spero and Parker (1985) and Faber et al. (1988), respectively. As *O. universa*, *G. sacculifer* and *G. ruber* have the same symbiont type (Hemleben et al., 1989), they are assumed to produce photosynthesis in the same way. \( s_{nb} \) for *G. sacculifer* was estimated from Jørgensen et al. (1985) (foraminifer size <300 µm) with photosynthesis re-evaluated for comparison at 25°C, and compared to the photosynthesis rate of one individual symbiont observed for *O. universa* at 25°C (Spero and Parker, 1985). The same estimation was done for *G. ruber* by using photosynthesis results from Lombard et al. (2009a), and Gastrich and Bartha (1988). \( P_{max}(T_1) \) and \( k_p \) were estimated by combining results from Jørgensen et al. (1985), Spero and Parker (1985), and Rink et al. (1998) re-evaluated to the reference temperature of 20°C, and on a per symbiont basis.

Parameters \( N_{max}(T_1), T_A, T_L, T_H, T_{AL}, T_{AH}, \) and \( \%_p \) were calibrated by using growth observations from Lombard et al. (2009b). Knowing that these data were obtained for specimens fed every day or every two days, and that foraminifer in natural conditions should obtain one prey every 4–5 days (Hemleben et al., 1989), we assume that these observations correspond to food saturated conditions (i.e., \( F/(F+k_n)\approx 1 \)) and then the parameter \( k_n \) did not need to be calibrated at this step. Because all observations from Lombard et al. (2009b) were conducted within illuminated conditions, we also assume that the mean light intensity corresponding to these observations is near to the saturating light level (200 µmole photon m\(^{-2}\) s\(^{-1}\)). The parameters were then estimated by a least square minimisation (Nelder-Mead simplex method) of the overall model compared to the empiric data on growth.
After calibration, by combining nutrition, respiration, and photosynthesis, the model simulates with a high confidence the individual growth pattern for the eight species observed under laboratory conditions (Fig. 1; all coefficient of determination between model simulations and observations are higher than 0.88, but for *N. dutertrei*; $R^2=0.76$). Except for the half saturation constant for nutrition $k_n$, all the parameters were thus calibrated with culture experiments, and the results for the different parameters are given in Table 2.

### 2.2 Species abundance in natural conditions

#### 2.2.1 Strategy: from individual growth rate to population abundance

Extending individual growth rates to population growth in natural conditions, for the eight different species, using the mechanistic approach used in our study, would require precise biological knowledge on feeding preferences, food availability of the different food types, reproduction, and mortality of foraminifers. That information is currently not available. Planktic foraminifers feed on various types of food including zooplankton, protozoans, and phytoplankton (Hemleben et al., 1989). However, except of limited case in situ observations, the abundance of different prey items is rarely available together with foraminifer observations. The different outputs of a general ecosystem model may be used to solve this issue (e.g. Fraile et al., 2008). However, prey preference of different foraminifer species is only poorly known, and, because of the lack of data, could be calibrated neither with laboratory experiments nor in situ observations. In addition, whereas chlorophyll-a (chl-a) is generally well constrained in ecological models, the other outputs (zooplankton, protozoans, and detritus) are not yet sufficiently constrained. Taking into account these limitations we use the chl-a concentration as a general productivity indicator, and as food concentration available to foraminifers. This is a reasonable hypothesis knowing that copepods, which are prey of spinose tropical foraminifers (*O. universa*, *G. siphonifera*, *G. ruber*, *G. sacculifer*; Hemleben et al., 1989), are generally correlated in abundance with chl-a (Gasol et al., 1997). Non-spinose species are mostly herbivorous or detritivorous (Hemleben et al., 1989).
1989) and feed on prey that contains chl-a. Choosing chl-a as food has different advantages: (1) Plankton net sampling of foraminifers was sometimes conducted together with measurements of chl-a concentration. The model may therefore be calibrated on real observations. (2) chl-a is observed by a large number of satellite, which give a confident estimation of food level in the oceans upper meters on a global scale. (3) chl-a is the best constrained and validated biological variable in global ecosystem models, which gives also confidence in the use of these models. Besides food availability, the other processes necessary to model population growth, mortality, reproduction, and predation, have been studied only in few cases (Schiebel et al., 1997; Schiebel and Hemleben, 2000) and thus are mostly unknown for foraminifers and would need further observations to be calibrated efficiently.

We chose to generalize the model with a progressive adjustment of the half saturation constant for nutrition \( k_n \) to get the best model output fit when compared to observed species abundance in plankton multinet samples collected in known conditions. As already discussed, the parameter \( k_n \) is the only parameter that we could not calibrate using culture experimental data.

### 2.2.2 Calibration data set: multinet data

The calibration data set includes the results from plankton multinet sampling from different studies (Field, 2004; Kuroyanagi and Kawahata, 2004; Schiebel et al., 2001; Schiebel et al., 2004; Watkins et al., 1996, 1998). These data include foraminifer counts (ind m\(^{-3}\)), T °C, and chl-a for each sampled depth. These plankton tows were obtained with mesh size from 63 \( \mu \)m (Kuroyanagi and Kawahata, 2004; Watkins et al., 1996, 1998) to 100 \( \mu \)m (Schiebel et al., 2001, 2004) and 120 \( \mu \)m (Field, 2004). In order to keep the coherence of data, and because juvenile forms of *O. universa* were rarely recognised or counted both in plankton or sediment samples, only adult forms (when indicated) were considered. Only white forms of *G. ruber* were considered because all the laboratory experiments used to calibrate the model were performed on this morphospecies, and, in the Pacific and Indian Ocean, the pink variety is not present.
N. pachyderma needed to be considered separately due to the lack of observations with hydrological constraints. We use data from Schiebel (2002) for this species to increase the observed reference database and outputs from a plankton ecological model PISCES (see below) at the corresponding location, season, and depth as a reasonable forcing for the foraminifer growth model in lack of available direct measurements of environmental variables. Data used as forcing input in the model (\(T^\circ K\), light intensity, and food concentrations) correspond to the same geographical position and same month as the foraminifer collection.

For all data sets, observed chl-a (mg chl-a m\(^{-3}\)) concentration was converted to carbon biomass (mg C m\(^{-3}\)) by using a variable C:chl-a factor that depends on temperature, light, and nutrient availability (Taylor et al., 1997) as successfully modelled by Geider et al. (1997). To apply this conversion we used outputs of the PISCES model (Aumont et al., 2003; Aumont and Bopp, 2006), which implement the Geider et al. (1997) model on a global scale in order to supply a realistic C:chl-a ratio that takes into account the effect of seasons and hydrology.

Light intensity data were obtained from Seawifs satellite data for the corresponding date of sampling. Light intensity at depth \(z\) (PAR\(_z\)) was calculated from intensity measured at the sea surface and taking into account the observed chl-a concentration in seawater assuming the following relationship:

\[
\text{PAR}_z = \text{PAR}_{z-1} \exp(z(-K_{\text{dw}} - K_{\text{dc}}[\text{chl-a}]))
\]

Where \(K_{\text{dw}}\) is the diffuse attenuation coefficient for water alone, estimated around 0.038 m\(^2\) by Lorenzen (1972), and \(K_{\text{dc}}\) is the specific attenuation coefficient due to chl-a estimated around 0.016 m\(^2\) (mg chl-a\(^{-1}\)) (Gallegos and Moore, 2000).

Daylength (dl) was calculated by taking into account latitude and date using the Forsythe et al. (1995) model.
2.2.3 FORAMCLIM model calibration

When using the growth model \( k_n \) unconstrained) to simulate growth under natural conditions, a general positive correlation was observed between the estimated growth rate and the observed abundance of each species. Thus, our results may indicate a close coupling between individual and population growth rates. In the present case, close coupling between individual growth rates and population abundance of foraminifers could have different origins: (1) the low density of the populations (foraminifers generally occur in low abundance compared to other plankton organisms), which means that the environment rarely becomes saturated by foraminifer and competition for resources does not exist and implies no specific predators. (2) The high mortality rate, both during the life cycle and following reproduction (foraminifers decease after liberation of gametes; Hemleben et al., 1989). (3) A low efficiency of reproduction, especially when growth rates are low. These characteristics specific for foraminifers could induce a short resilience time of populations when conditions are unfavourable, and indicate close coupling between growth rates (controlled by environmental factors) and abundance, with only a small lag between the timing of maximum growth rate and maximum abundance (Fig. 2). If the mismatch would be larger, no correlations would have been observed.

This suggests that the growth rate estimated for each foraminifer species can be used as an abundance indicator. Taking into account these considerations, we tested the hypothesis that the correlation between growth rate \( \mu \) and abundance \( \text{Abund} \) follows an exponential relationship with a minimal abundance \( 0.1 \text{ ind m}^{-3} \) for all species when \( \mu \) is null and in the form:

\[
\text{Abund} = a\mu^b - a + 0.1
\]

(7)

In spite of the potential problems, and/or over-simplification of such an approach, we thus decided to use the observed correlation between population density and individual growth rate to model abundance based on food (chl-a) availability, light, and
temperature. It is important to note that the transformation from growth rate to abundance represents only an ideal foraminiferal community with a mean potential abundance. This is the only way presently available to represent foraminifer abundance without simulating their population dynamics which would have dramatically increased the model complexity and introduce many unknown processes (mortality, reproduction, predation).

For each species, the half saturation constant for nutrition (\(k_n\)) was calibrated in order to maximise the correlation between the model individual growth rate \(\mu\) and species abundance \(\text{Abund}\) (i.e., increase \(R^2\) of the correlation) in the multinet data. After calibration, the Eq. (7) relationship for which the correlation was maximised is used to transform model growth rate into abundance data. When \(\mu\) is negative the species abundance is set to zero. The correlation between abundance and growth rate is shown in Fig. 3. The parameters \(k_n\), \(a\), and \(b\) are listed in Table 2 for the different species. Due to the scarcity of data on adult \(O. universa\), the relationship between growth rate and abundance is weak (\(R^2=0.017; F_{\text{stat}}=7.01; 0.05>p>0.01\)). For the other species, the relationships are highly significant (all \(F_{\text{stat}}\) with \(p<0.001\)) despite the large scattering attributed to the small mismatch between the maximum of growth and of abundance (see Fig. 2). The relationship between abundance and modelled growth rate is relatively strong for \(G. sacculifer\) (\(R^2=0.29\)), \(G. siphonifera\) (\(R^2=0.38\)), \(G. ruber\) (\(R^2=0.4\)), \(N. dutertrei\) (\(R^2=0.34\)) and \(N. pachyderma\) (\(R^2=0.42\)), and lower for \(G. bulloides\) and \(N. incompta\) (\(R^2\), respectively 0.19 and 0.12). This is probably attributable to scarce abundance data of these two species under conditions where the modelled growth rate is negative. These observations generally correspond to sub-surface waters where food is scarce and temperature low, and conditions do not allow significant growth of these species. In fact, the observed foraminifers could originate from individuals that grew under near surface conditions, where the model simulates positive growth, and afterward have been transported to depth both by sinking or advection, process the model cannot reproduce so far.
2.2.4 Model evaluation

In order to validate the model, we tested and compared its results with data bases covering large areas, i.e., foraminifer species dominance from sea surface plankton tows, and foraminifer species proportion in sediment core tops.

Foraminifer total abundance and species dominance (i.e., species having the highest abundance in the foraminiferal assemblage) in sea surface plankton tows (0–10 m) were recovered from Bé and Tolderlund (1971). This study covers the entire Atlantic and Indian Oceans. These data correspond to more than 10 multi-station cruises in different years and seasons. In order to simplify the procedure, we did not determined the sampling season of each sampling point but simply assumed that the dataset represents an annual average of species dominance. In order to simulate these observations with the model, annual means from satellite images from MODIS ($T^\circ C$, chl-a) and SeaWifs (Photosynthetically Active Radiations, PAR, $\mu$mol photon m$^{-2}$ s$^{-1}$) were used (http://oceancolor.gsfc.nasa.gov/). Annual means of sea surface results ($T^\circ C$, chl-a, and PAR) of the general ecosystem model (PISCES model; Aumont and Bopp, 2006) were alternatively used to simulate foraminiferal abundance (annual mean, 0–10 m depth). To do so, we used the standard climatological simulation of PISCES as described and evaluated in Aumont and Bopp (2006). By using the mean annual $T^\circ C$, chl-a, and PAR observed by satellites (mean annual sea surface conditions), the growth rates of the different species were calculated and converted to abundance data using the growth rate-abundance relationships (Fig. 3). These results were then used to estimate species dominance (i.e., species with the highest abundance). In order to compare the model simulation to the data of Bé and Tolderlund (1971), we assume that if the dominant species is the same in both model and empirical data, the model result is correct. However, for some observations it was not possible to determine which species dominate the assemblage and a co-dominance was attributed to those observations (Fig. 4a). Because the model results cannot gives such an exact co-dominance, the model was assumed correct if one of the two observed co-dominants species was reproduced.
Results from core tops foraminifer counts (MARGO database; Barrows and Juggins, 2005; Hayes et al., 2005; Kucera et al., 2005a) were also used. This database includes around 3000 samples covering all oceans. Abundance data were converted to relative abundance by considering only the eight species included in the model. Shannon diversity index ($H'$) was calculated from species relative abundances of the eight considered species, ($p_i$), both from the model and from core tops data, by using the following relationship:

$$H' = -\sum p_i \log(p_i)$$  \hspace{2cm} (8)

In order to simulate an equivalence to core tops assemblages, the model was run with two different data sets. Firstly, the model was run using mean monthly chl-a, $T \degree C$, and PAR observations derived from satellite images (monthly averages). The abundance of each species was cumulated over months to produce a mean annual estimate and expressed as a fraction ($p_i$) of the total foraminifer abundance and $H'$ was calculated following Eq. (8). Secondly, the model was forced by outputs from the PISCES model. Monthly $T \degree C$, PAR, and chl-a average were used in a similar way as for satellite data, and their distribution within the upper 200 m of water column simulated by the PISCES model. Abundances of the different species were cumulated with reference to month and water depth.

For all core tops data, deviations between the $n$ observed ($x_o$) and modelled ($x_m$) species relative abundance were calculated using coefficient of determination ($R^2$) and, in order to compare with previous studies, with the root mean squared error (RMSE) which is calculated as follow:

$$\text{RMSE} = \sqrt{\frac{\sum (x_o - x_m)^2}{n}}$$  \hspace{2cm} (9)

These monthly simulations were also used to determine the season and water depth of maximum growth (i.e., season or water depth where the growth rate is maximum) for the different species.
3 Results

3.1 Species dominance

The model successfully reproduces species dominance of foraminifer observed in Atlantic and Indian Oceans by sea surface plankton tows (Bé and Tolderlund, 1971; Fig. 4), with 70.5% of the 576 observations being correctly estimated by the model (Fig. 4). The model reproduces the general biogeography of dominant foraminifers, with *G. ruber* dominating in oligotrophic tropical gyres. *G. sacculifer* dominates in the equatorial area, in the North Indian Ocean and at the limits of temperate regions, except of the Gulf Stream where the assemblage shifts from a *G. ruber* dominance to *G. bulloides* without transition. *G. bulloides* dominates the species assemblage in temperate regions and also in some tropical coastal productive areas such as in the Benguela and Mauritanian upwelling regions. In few locations, *N. incompta* is modelled as the dominant species notably close to the coast in the southern part of the Benguela upwelling system, along the Uruguay coast, and in the northeast of the Atlantic Ocean around 45° N. *N. pachyderma* dominates the ecosystem in polar regions starting from 50° S latitude in the Southern Hemisphere, and from the Canadian coast to Iceland and Norway in the North Atlantic Ocean.

Using the environmental results of the PISCES model (mean annual sea surface conditions), our model simulates a similar geographic distribution in the dominance of the different species, but with lower confidence (58.9% efficiency; Fig. 4). Most of these differences come from the fact that the PISCES model uses a 2° mesh grid, which does not allow reproduction with sufficient confidence of fine scale physical processes such as the Gulf Stream or the equatorial Atlantic upwelling, and most of the discrepancies between observed and modelled dominances are observed here. For example, in the equatorial Atlantic, the food concentration is slightly lower than observed by satellite images, which results in *G. ruber* dominance instead of *G. sacculifer*. The Gulf Stream region is not sufficiently contrasted hydrographically. Then the model simulates a gradual change in dominance from *G. ruber* to *G. sacculifer* and then to *G. bulloides* rather
than the observed direct transition from *G. ruber* to *G. bulloides*. However, excepted for these two locations that were massively sampled, the general pattern of species dominance is correctly reproduced.

### 3.2 Total abundance in surface waters

The general abundance of foraminifers under different sea surface conditions is simulated by combining the abundance of all the species simulated by the model when forced by satellite derived data. This abundance may be compared to observations of Bé and Tolderlund (1971) (Fig. 5), but with caution. Bé and Tolderlund (1971) reported only three classes of abundance, and used a 200 µm mesh sized plankton tow whereas our model abundance has been calibrated for 64–120 µm mesh size multinet sampling. The range of abundance simulated by the model (0–80 ind m\(^{-3}\); Fig. 5) is in the same range as that observed in Atlantic and Indian Oceans (0–100 ind m\(^{-3}\)). The pattern of abundance of foraminifer species is reproduced by the model with a maximum abundance in the equatorial regions, African upwelling, Arabian Sea, off Uruguay and the Brazil coast, and in the Gulf Stream. Considering the Gulf Stream and the southern Indian Ocean, the simulated maximum abundance is less extended to the north than observed.

These differences may have two origins. Firstly, we used mean annual observations to force the model, whereas Bé and Tolderlund (1971) samplings originate from different seasons. Indeed, foraminifer sampling in the subpolar Atlantic and Indian Ocean, correspond generally to summer conditions when the foraminifer abundance is higher than simulated by annual mean conditions. Secondly, the model, derived from available laboratory observations, simulates the abundance of eight of the most abundant species in the world ocean, but misses some of the species which are significant in polar and temperate regions such as *Turborotalita quiveloba*, *Globorotalia inflata* and *Globigerinita glutinata*. Those were included in Bé and Tolderlund (1971) observations and contribute to a significant fraction of foraminifer assemblage in transitional region. This could explain the smaller poleward extension of the modelled maximum
abundance in the Atlantic and Indian than observed by Bé and Tolderlund (1971).

3.3 Relative abundance of the species

Comparison of the simulation data with core tops foraminiferal assemblages from the MARGO data base (Barrows and Juggins, 2005; Hayes et al., 2005; Kucera et al., 2005a), recalculated on the basis of eight species, are shown in Figs. 6 and 7. The model fit is expressed by the coefficient of determination ($R^2$; Table 3) which represent the fraction of data variability explained by the model. The $R^2$ are shown for the standard simulation (i.e., worldwide dataset using satellite data Figs. 6 and 7), and for similar simulations done with the PISCES model considering the effect of water depth and season. We also considered a subset of the data focussing on Atlantic Ocean where the data are more numerous and secure: the deep water $\text{CO}_3^{2-}$ is higher and therefore foraminifer will be less subject to selective dissolution (Takahashi et al., 1981).

The $R^2$ on the standard simulation is comprised between 0.07 and 0.85% for $O. universa$ and $N. pachyderma$, respectively, (Table 3) with variations between species that reflects the $R^2$ variations of the fit between estimated growth rate and abundance in multinet samplings (Fig. 2). The model does not efficiently reproduce $O. universa$ and $N. pachyderma$ spatial variations on a worldwide coverage and only explains 7–9% of the data variability. The model explains between 37% ($G. bulloides$) to 85% ($N. pachyderma$) of species relative abundance variations, with most species in the 40–55% range. When focussing only on the Atlantic Ocean, the $R^2$ for all the species is higher than for worldwide comparison, indicating smaller differences between simulated and sampled relative abundance, except for $N. pachyderma$ for which the $R^2$ remains mostly unchanged. In the Atlantic Ocean, the model better reproduce the spatial variations of $O. universa$ (11% variability explained) and $N. dutertrei$ (20%). Using data that combine seasonal and depths effects, the PISCES model outputs give results in the same range of order, except for $N. dutertrei$, for which the precision is significantly increased (16% of variability explained worldwide; 34% in the Atlantic Ocean).
From a qualitative point of view, the spatial distribution pattern of different species is well represented by the model. As most of the sampling points are concentrated in the Atlantic and Indian Oceans, we focus the description of the spatial distribution patterns to these regions by highlighting the correspondences between the model and observations. *N. pachyderma* is present with high abundance south of 55° S latitude and north of 45° N in the Pacific Ocean, and in the Atlantic Ocean from Labrador Sea to Iceland and Cape North. *N. incompta* is abundant in the Northwestern Atlantic Ocean from a narrow zone in the northern part of the Gulf Stream and in the Northeastern Atlantic Ocean to a zone from Gibraltar to Iceland. Low *N. incompta* abundance is also correctly modelled for the northwestern part of the Mediterranean Sea. *N. incompta* is present in the Southern Hemisphere in a circumpolar belt from 40° S to 50° S, and also in some upwelling zones (Benguela, Argentina and to a lesser extend the Mauritanian upwelling). The spatial distribution of *G. bulloides* is relatively similar to *N. incompta*, but is also present to a larger extent in some tropical upwelling such as Mauritanian, Peru, and the Arabian Sea. *N. dutertrei* shows high relative abundance in tropical-productive areas such as the southern part of the Gulf Stream, the Arabian Sea, and equatorial upwelling. *G. ruber* is present mostly in oligotrophic tropical gyres, and is less abundant in productive areas such as coastal and equatorial upwellings. It is also present in the eastern basin of Mediterranean Sea. *G. siphonifera* has a distribution intermediate between *G. ruber* and *N. dutertrei*. *G. siphonifera* species is present in oligotrophic areas but shows its maximum relative abundance at the limit between oligotrophic areas and tropical upwelling systems. *G. sacculifer* shows maximum abundance in a circum-equatorial belt between 20° N and 20° S. *O. universa* occurs at low abundance from 50° N to 50° S of latitude.

The relative abundance of different species is in general also well reproduced by the model. However, some regional discrepancies can be observed between modelled and observed relative abundance. For *N. incompta*, the model simulates maximum relative abundance around 35% in the North Atlantic Ocean whereas it is higher (∼55%) in observations. For *G. bulloides*, the modelled relative abundance in the South Atlantic
and Indian Oceans is less important than observed. For *N. dutertrei*, the model underestimates the relative abundance in the Arabian Sea, the Bay of Bengal, and in the East Pacific equatorial upwelling whereas it overestimates it in temperate regions. For *G. ruber*, the relative abundance seems to be slightly underestimated by the model in highly oligotrophic regions, which is also the case for *G. sacculifer* and *G. siphonifera*.

To some extent, these discrepancies could be explained by differences between sea surface conditions (observed by satellite images) and favourable conditions in subsurface waters that satellite images can not observe. Some of these discrepancies are reduced by the use of the PISCES model, which integrates both water depths and seasons, rather than satellite images as forcing variables. However, as seen previously, some small scale events are less efficiently reproduced. For example, using PISCES data reduces the bias for the high abundance of *N. dutertrei* in Arabian Sea, Bay of Bengal and East Pacific equatorial upwelling but do not efficiently capture small scale processes.

### 3.4 Diversity

The Shannon Diversity index on both core tops data and model outputs considering only the eight selected species (Fig. 8). The modelled diversity pattern corresponds well to the observations ($R^2 = 0.50$), especially in the Atlantic Ocean ($R^2 = 0.52$) with minimum diversity in polar regions and in the centre of the subtropical oligotrophic gyres. Maximum diversity was calculated at the southern limit of the Gulf Stream, off the west coast of Africa, and in the circumpolar belt around 40° S of latitude, and intermediate diversity in the equatorial part of the Atlantic Ocean. However, some discrepancies can be observed such as the high diversity in the central part of the Indian Ocean, and the low diversity (<1) in the equatorial Eastern Pacific, due to a high abundances of *N. dutertrei*, which are not reproduced by the model (see Fig. 6).

The mean modelled and observed diversity was extracted in a mid Atlantic transect between 25° W and 50° W. The model simulates well the diversity pattern with maximum values at 40° N and S, a sharp decrease in diversity in polar regions around 50° S
and more gradually in the Northern Hemisphere, a minimum diversity in subtropical gyres (20° S and 20° N), and an intermediate diversity around the equator.

However the model seems to smooth the variations in diversity by simulating lower amplitude changes over different regions. In high diversity regions, the model slightly underestimates the diversity whereas it overestimates it in tropical gyres. Using the PISCES model (including species variations with depth) rather than the satellite images as input data for the model gives similar results but with better adequacy with the data (Table 3; $R^2$ 0.58–0.69 for worldwide and Atlantic simulation, respectively).

### 3.5 Model predictions on season and water depth of maximum growth

In order to estimate the season and depth of the maximum growth potential, and consequently abundance, the model was run using PISCES model outputs combining depths and seasons in order to determine in which season and water depth the maximum of growth potential occurs. For *G. sacculifer*, *G. siphonifera*, *G. ruber*, and *O. universa* the simulation indicates that maximum abundance should systematically be observed in surface waters (0–10 m; data not shown). In this case, we used preferentially satellite images to simulate the influence of seasons (Fig. 9). These four species approximately show the same pattern in their seasonal preferences with maximum growth in August in the northern temperate oceans, in May–June in the western part of north tropical oceans, and in August–September in the eastern part north tropical oceans. In equatorial waters, maximum growth is modelled for October, and from February to March in the tropical and temperate southern marine ecosystems.

For the other species (*N. dutertrei*, *G. bulloides*, *N. incompta* and *N. pachyderma*), maximum abundance could occur at depths, and we used PISCES data to determine the combined depth and season of maximum growth (Fig. 10). For *N. dutertrei*, maximum growth rates were modelled in surface waters for summer in the 30–60° latitude (July–August and February–March for the Northern and Southern Hemisphere, respectively). At the 0–30° latitude range *N. dutertrei*, occurs mostly in spring and exhibits maximum growth at sub-surface waters around 60–80 m and deeper (>100 m).
in oligotrophic gyres. *N. incompta* and *N. bulloides* have similar seasonal growth patterns with maximum growth in summer at the 60–40° latitude and maximum in spring in subtropical and tropical areas. Their depth of maximum growth also progressively increases while the waters become more oligotrophic, and *N. incompta* exhibits generally larger depth of maximum growth than *G. bulloides*. *N. pachyderma* has its maximum growth ability in spring in the 40–60° latitude range and in early summer in higher latitudes. The maximum growth potential is always in surface waters in the North Atlantic Ocean whereas a progressive increase in depth is observed in the Northeastern Pacific Ocean. In the Southern Ocean, *N. pachyderma* maximum growth rate is always located in sub-surface waters between 20–30 m in 80–60° S latitudes and at 60–40° S with a progressive increase in depth down to about 100 m.

4 Discussion

4.1 General considerations

After calibration of the model against laboratory experiments (Fig. 1) and multinet data (Fig. 3), our model has been validated by comparing the modelled data with various independent data sets obtained with plankton tows and core tops sampling (Figs. 4–8) and helps to represent generally more than half of the observed variability. Our work suggests that physiological adaptations control to a large degree the species distribution of foraminifers. Our approach is intermediate between trait based models and habitat suitability models. Trait based models are usually concentrated on simulating a whole variety of traits (i.e., physiological abilities) and afterward define a species by analogy between simulated successful combination of traits and existing species or functional groups of organisms presenting these traits (Bruggeman and Kooijman, 2007; Follows et al., 2007; McGill et al., 2006). In contrary, habitat suitability models, also called niche models, use field abundance or presence observations in order to statistically estimate the suitable environmental conditions for each species (Hirzel and Le Lay, 2008). Because habitat suitability models are based on observations that
could not represent all possible combinations of environmental conditions (Guisan and Thuiller, 2005) or biotic interactions (Davis et al., 1998), it is recognized that a statistical approach could be inappropriate when extrapolating to novel situations, for example, using scenarios of climatic changes (Davis et al., 1998; Kearney and Porter, 2004). Indeed, it has been argued that only mechanistic process based models (e.g., Kearney and Porter, 2004; Morin et al., 2008) can approach the fundamental niche (Guisan and Thuiller, 2005), and, if based on laboratory or field observations of processes, could facilitate good extrapolation within changing environments (Davis et al., 1998; Kearney and Porter, 2009). We have attempted to fulfil this goal by constructing a model, as much as possible, on laboratory observations of foraminiferal physiology. Thus the FORAMCLIM model is particularly relevant for paleostudies and future climate change studies.

However, with little information on the foraminifer population biology (i.e., fecundity, reproduction, mortality), it was not realistic to develop a mechanistic model of the species abundance. Our model does only simulate abundances using the positive correlation between observed abundance and the model-simulated growth rates (Fig. 3). This correlation was then used to directly convert the growth rates, simulated by the mechanistic part of the model, to abundance. Although introducing an empirical part in our model, this procedure has several advantages: It allows simplifying the model without introducing population biology, for which a large part of the processes are neither quantified nor demonstrated. Consequently, this empirical relationship (Fig. 3) combines all population biology in a simple assumption, and allows its calibration with regard to observed abundance.

4.2 Potential biases of the approach

The discrepancies observed between observations and model simulations may be explained by many factors including different biases both in the data used to simulate the model, and the data used to validate it, but also potential biases due to the model formulation itself.
4.2.1 Bias from in situ observations

The environmental data used to run the model, i.e., hydrological data originating both from satellite sensors or global ecological model, could lead to biases in the comparison between model results and in situ foraminifer distribution. Only in the case of multinet data used for calibration, all hydrological data (T °C, chl-a, light) have been measured simultaneously with foraminifer sampling. For the foraminifer data base used to validate the model (Bé and Tolderlund, 1971; core tops), the corresponding hydrological data are not available, and we could not take into account the effect of inter-annual variability, favourable conditions in subsurface waters compared to surface waters when using satellite data and climate changes since the observation. For the plankton net data originating from Bé and Tolderlund (1971), the season of the sampling is not known and sea surface conditions, observed by satellite images where not yet available. Core tops samples (MARGO data base) integrate several decades to centuries of sedimentation and hydrology might have changed between present times and the mean age of core tops samples.

The existence of cryptic species (Kucera and Darling, 2002), which while similar in morphology may have slight differences in physiology, could impact the data-model comparison. Most of the morphospecies cover several genetically defined species (Darling et al., 2006; Darling and Wade, 2008; Kucera and Darling, 2002) which could have different physiological adaptations. Those have not been checked in the laboratory studies on which the model is constructed and then were not taken into account. In addition, due to the different sources of data used to both calibrate and validate the model, taxonomic consistency may also be subject to caution. This is particularly relevant concerning intergrade forms between N. incompta and N. dutertrei. In the case of model-data discrepancies affecting N. incompta and N. dutertrei, it is important to note that in the MARGO database, N. incompta data (also called N. pachyderma dextralis) includes N. pachyderma (dex) sensus stricto but also the so called “P/D intergrade” which regroups specimens with intermediate forms between N. pachyderma (dex) and
N. dutertrei. This choice has been made globally over the world ocean but may differ from choices made in other studies, notably multinet samplings used for model calibration. This would explain, the underestimation of N. incompta and overestimation of N. dutertrei by our model (for example in the Northern Atlantic Ocean). Therefore, in future studies, the methods of combining the P/D intergrade with N. dutertrei or N. incompta, or keeping this taxonomical class separated should be compared.

Selective sedimentation and dissolution of the different species could affect the comparison of model results with the core tops MARGO database. Some species have shells prone to dissolution before fossilization and this will affect the species distribution in core tops (Berger, 1970) notably when concentration is low, such as in the deeper part of Indian and Pacific Oceans. For instance, N. dutertrei is known as dissolution resistant and, this may explain why the model does not succeed to reproduce the high proportion of this species observed in core tops from the east equatorial Pacific Ocean (Fig. 6).

The assemblage data originating from core top samples are subject to error propagation because they are expressed in relative abundance: a deviation from observations on one species has an influence on the relative abundance of the other species. This bias also applies to model data expressed in relative abundance. This is particularly true in oligotrophic zones where a small deviation in the absolute abundance of one species may have a large impact on the relative abundances of all other species because of the generally low abundance of each species.

4.2.2 Possible biases from model construction

Several hypotheses on which the FORAMCLIM model is built may affect its efficiency. The model only considers eight foraminifer species among the most abundant ones both in the water column and in sediment core sampling. Considering more species would certainly change the model results. However, due to the lack of knowledge on their physiology, all foraminifer species could not be considered yet. The model only considers three environmental forcing factors (T °C, food concentration, and light...
availability) whereas other parameters can act on foraminifer abundance such as the salinity (Bijma et al., 1990; Siccha et al., 2009), the depth of the mixed layer (Žarić et al., 2005) or the phase in the lunar cycle (Erez et al., 1991; Schiebel et al., 1997).

Our model, like numerous other habitat suitability models, is a static model implying an assemblage is in pseudo-equilibrium with its environment (Guisan and Theurillat, 2000). Accordingly, the model cannot reproduce events controlled by population biology and hydrology, such as the effect of delayed response to a bloom (e.g., Fig. 2) and the effect of transport of assemblages by oceanic currents. Only bottom-up processes are considered meaning that predation and competition are not taken into account. An empirical relationship has been used to relate the simulated growth rates to estimated abundances (Fig. 3). Whereas a good correlation exists between these growth rate and abundance, the variability is high and could potentially lead to large biases when comparing model estimations with discrete observations such as plankton tows or sediment trap data. This means that the model only allows to represent a mean ideal foraminifer community, and to calculate a potential abundance.

Despite all these possible biases, the model seems to reproduce efficiently the general pattern of foraminifer species dominance as well as the relative abundance of species, and the total abundance of specimens.

### 4.3 Comparison with previous foraminifer models

Previous existing models are based on empirical abundance observations, statistical relationships and are constrained by hypothesis on unknown population dynamic parameters (predation, competition, reproduction success) (Fraile et al., 2008; Žarić et al., 2006). In contrast, the FORAMCLIM model calibration is mostly based on parameters derived from physiological laboratory observations, with a model complexity limited to demonstrated processes. For the few comparable results (see below), the FORAMCLIM model reproduces the species relative abundance with higher confidence than previous modelling studies (Fraile et al., 2008; Žarić et al., 2006). For comparison between the FORAMCLIM model outputs, forced by satellite images or the PISCES
model, and core tops, all RMSE are between 5 to 23% (Table 3), a lower deviation than the 22–25% obtained by Fraile et al. (2008). *N. pachyderma* (sin.) is the only species for which our RMSE (12–19%) is larger than that of Fraile et al. (2008) (9%). When compared to the total foraminifer mean abundance from plankton net sampling (Bé and Tolderlund, 1971)(Fig. 5), FORAMCLIM correctly reproduces the observed abundances, with maximum abundance in tropical and equatorial regions, whereas previous modelling studies simulate maximum abundance in temperate zones (Žarić et al., 2006). However, this could be due to the fact that in our model simulations and data correspond to individuals living in surface waters, and the abundance of temperate-polar species such as *Turborotalita quinqueloba, Globorotalia inflata* and *Globigerinita glutinata* is not simulated, whereas the Žarić' et al. (2006) model includes those species and simulates fluxes over the whole surface mixed layer in order to reproduce sediment trap observations. It is therefore possible that, whereas having higher abundance in equatorial zones (Bé and Tolderlund, 1971), maximum flux of shells may be encountered in temperate regions (Žarić et al., 2006) due to possible differences in population dynamics between temperate and tropical conditions.

In addition, whereas previous models estimate the foraminifer assemblages on a 2-D framework reproducing only the mean mixed layer, our model offers the opportunity to estimate foraminifer assemblages over different water depth, when coupled with appropriate data sets of forcing variables (in situ observations or PISCES model). Since some species are known to occur specifically in sub-surface conditions close or below the deep chl-a maximum (e.g., Schiebel et al. 2001; Kuroyanagi and Kawahata, 2004), this can improve the utility of predictions made by the FORAMCLIM model.

### 4.4 Ecological meaning of parameters

Several model parameters are related to the affinities of foraminifer species for their environment. For example, $k_n$ values identified from the calibration allow to describe the affinity for food of different foraminifer species. *G. ruber* is better adapted to oligotrophic conditions ($k_n=0.51 \mu g C I^{-1}$), *O. universa, G. sacculifer, G. siphonifera* and *N. dutertrei*...
are more adapted to intermediate conditions between oligotrophic to mesotrophic waters ($k_n$ between 1 to 1.75 µg C l$^{-1}$), whereas *N. incompta, N. pachyderma,* and especially *G. bulloides* need abundant food condition to growth ($k_n$ about 3.33, 4.7, and 6.84 µg C l$^{-1}$, respectively). *G. ruber* is commonly described as an oligotrophic species (Bé and Tolderlund, 1971; Hemleben et al., 1989). *G. bulloides, N. pachyderma,* and *N. incompta* are more common in temperate to polar productive waters (Bé and Tolderlund, 1971), and seem to react positively to strong bloom events (Schiebel et al., 1995). *N. dutertrei* is commonly described as occurring in tropical-subtropical upwelling or productive areas (Bé and Tolderlund, 1971) has a similar $k_n$ as *O. universa, G. sacculifer* and *G. siphonifera* which are not considered to be related to enhanced production. This difference should originate in the fact that the three latter species bear symbionts that could help to survive and grow in oligotrophic regions whereas we assumed that *N. dutertrei* does not and then, despite a similar $k_n$, need more food to growth efficiently. The assumption that *N. dutertrei* is symbiont-barren whereas it has been described as a facultative symbiont-bearing species (Hemleben et al., 1989) may also explains some model discrepancies when compared to core top data. Such a shift in behaviour was impossible to implement in our model. If the “symbiont-barren” hypothesis succeeded to reproduce *N. dutertrei* distribution pattern in Atlantic Ocean, it seems that on the contrary, it does not reproduce correctly the high abundance in Southern Indian and equatorial Pacific Oceans. If bearing symbionts, *N. dutertrei* would display behaviour intermediate between the current one and *G. sacculifer* (data not shown), which would better agree to observation in Indian and Pacific Oceans, but will not agree with observations in the Atlantic Ocean. This may indicate that in Southern Indian and equatorial Pacific Oceans conditions. *N. dutertrei* may more frequently use symbionts and then potentially explains the model discrepancies when compared to data.

The $\%_p$ parameter gives information on the proportion of material originating from symbiont photosynthesis which is effectively used for growth of the foraminifer-symbiont complex. The $\%_p$ parameter has been freely calibrated in order to reproduce foraminifer growth observed in laboratory experiment (Fig. 1). For all the symbiotic considered
species, this proportion is comprised between 0.3 and 0.46 indicating that more than 50% of the photosynthesis is not used for growth of the foraminifer-symbiont complex. Then the model seems to confirm the hypothesis that photosynthesis produces carbon in excess (Jørgensen et al., 1985), and that only a small fraction effectively serves to growth (Lombard et al., 2009a).

4.5 Current utility and future potential of the model

Due to the fact that our study links foraminifer physiology, growth potential and potential abundance in natural environments, the FORAMCLIM model has different possible applications. First of all, the growth part of the model gives good simulations of the growth rate of different species for given environmental conditions (Fig. 1). This would support future laboratory experiments, and may provide references to estimate the effect of additional environmental parameters when compared to experimental observations. Moreover, the growth model, once integrated in a population dynamics model, and used in combination with temporal surveys such as sediment traps, may also serve in future studies to estimate reproduction and mortality rates. This will potentially allow using the growth model in a more dynamic way, and without using empirical links between growth rate and abundance (Fig. 3). The entire model also provides a good estimation of the distribution of dominant species and relative abundance of the foraminifer assemblage (Figs. 4–8). Therefore, the model can be used as a tool to give a first-order estimate of the distribution of foraminifer species at a given location and to plan samplings of selected species. This can notably offer possibility to target selected locations for sampling, where model and data does not agree, and thus where processes not included in the model (e.g., effect of salinity, presence of cryptic species) may mainly control the foraminifer species assemblage. For instance, two populations may correspond to cryptic species in our study: the abundant G. bulloides population observed in the Arabian upwelling, and the possibly symbiont-bearing N. dutertrei in Southern Indian and equatorial Pacific Oceans, that the model does not succeed to reproduce. A direct potential application of this model is also to give an indication on the potential
season and depth where each species may exhibit their maximal growth rate and then maximal abundance (Figs. 9, 10). This indication can be useful for numerous paleoclimate reconstructions in which depth and season are usually assumed. Our model provides a first-order estimate that may strengthen future climatic reconstructions.

Another potential application of this model could be to provide a new way to validate global ocean models. A recognized way to validate models is to simulate them under significantly different climatic regimes, such as during the last glacial maximum (LGM) (Le Quéré et al., 2005). However, available data to validate the LGM simulations cover only a small spatial range, and are often hardly comparable (Bopp et al., 2003), whereas large datasets are available on foraminifer composition during LGM (Waelbroeck et al., 2009).

Finally, if the calcification (Lombard et al., 2010) and dissolution processes that take place during sedimentation (Schiebel et al., 2007) could be integrated in our model, the latter associated with global-scale models may provide first-order estimates of foraminifer impact on calcite fluxes in present, past (LGM) and future conditions in the context of the current global warming.

Acknowledgements. We greatly thank the members of the Forclim Team for constructive discussions and their improvements of the manuscript, the French program ANR05-BLAN0275-01 Forclim, CEA and CNRS for their support to LSCE and the Marie Curie Intra-European Fellowship No. 221696 for funding.

The publication of this article is financed by CNRS-INSU.
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Modeling planktic foraminifer growth and distribution

F. Lombard et al.


Table 1. Symbols, description and units of the different variables and parameter used in the model.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Unit</th>
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<tr>
<td></td>
<td><strong>Forcing variables</strong></td>
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<tr>
<td>$T$</td>
<td>Temperature</td>
<td>°K</td>
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<tr>
<td>$L$</td>
<td>Light availability</td>
<td>µmole photon m$^{-2}$ s$^{-1}$</td>
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<td>$F$</td>
<td>Food concentration</td>
<td>µg C l$^{-1}$</td>
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<td>$dl$</td>
<td>Day length</td>
<td>d$^{-1}$</td>
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<td><strong>State variables</strong></td>
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<td>$W_f$</td>
<td>Final foraminifer weight</td>
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<td>$\Delta W$</td>
<td>Weight increase</td>
<td>µg C d$^{-1}$</td>
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<tr>
<td>$\mu$</td>
<td>grow rate</td>
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<td><strong>Fluxes</strong></td>
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<td>$N$</td>
<td>Nutrition</td>
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<td>$R$</td>
<td>Respiration</td>
<td>µg C d$^{-1}$</td>
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<td>$P$</td>
<td>Symbiont photosynthesis</td>
<td>µg C d$^{-1}$</td>
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<td>$W_i$</td>
<td>Initial foraminifer weight (size 250 µm)</td>
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<td><strong>Nutrition</strong></td>
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<td>$N_{max}(T_1)$</td>
<td>Maximum nutrition rate at $T_1$</td>
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<td>$k_n$</td>
<td>Half saturation constant for nutrition</td>
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<td>$T_{AH}$</td>
<td>Arrhenius temperatures for the rate of decrease at upper boundary</td>
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<td>$T_{HL}$</td>
<td>Upper boundary of the enzymes tolerance range</td>
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<td>Lower boundary of the enzymes tolerance range</td>
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<td>Arrhenius temperature for nutrition rate</td>
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<td>Arrhenius temperature for respiration rate</td>
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<td>$P_{max}(T_1)$</td>
<td>Maximum photosynthesis rate per symbiont at $T_1</td>
<td>µg C d$^{-1}$</td>
</tr>
<tr>
<td>$k_p$</td>
<td>Half saturation constant for photosynthesis</td>
<td>µmole photon m$^{-2}$ s$^{-1}$</td>
</tr>
<tr>
<td>$T_{Ap}$</td>
<td>Arrhenius temperature for photosynthesis rate</td>
<td>°K</td>
</tr>
<tr>
<td>$s_{nb}$</td>
<td>Symbiont number for a 250 µm sized foraminferan</td>
<td>nb ind$^{-1}$</td>
</tr>
<tr>
<td>$%_p$</td>
<td>Photosynthesis fraction used for the foraminifera-symbiont complex growth</td>
<td>–</td>
</tr>
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</table>
### Table 2. Parameters values for the different foraminifer species.

<table>
<thead>
<tr>
<th></th>
<th>O. universa</th>
<th>G. sacculifer</th>
<th>G. siphonifera</th>
<th>G. ruber</th>
<th>N. dutertrei</th>
<th>G. bulloides</th>
<th>N. incompta</th>
<th>N. pachyderma</th>
<th>Units</th>
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<tr>
<td>Nutrition</td>
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<tr>
<td>$N_{\text{max}}(T_c)$</td>
<td>0.21</td>
<td>0.29</td>
<td>0.19</td>
<td>0.19</td>
<td>0.17</td>
<td>0.31</td>
<td>0.18</td>
<td>0.19</td>
<td>µg C d⁻¹</td>
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<tr>
<td>$k_n$</td>
<td>1.73</td>
<td>1.32</td>
<td>1.19</td>
<td>0.51</td>
<td>1.00</td>
<td>6.84</td>
<td>3.33</td>
<td>4.70</td>
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<tr>
<td>$T_{\text{NH}}$</td>
<td>74.313</td>
<td>102.000</td>
<td>39.284</td>
<td>47.496</td>
<td>32.319</td>
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<td>51.836</td>
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<tr>
<td>$T_{\text{k}}$</td>
<td>305</td>
<td>305</td>
<td>303</td>
<td>304</td>
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<td>296</td>
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<td></td>
<td>°K</td>
</tr>
<tr>
<td>$T_{\text{AL}}$</td>
<td>31.002</td>
<td>51.870</td>
<td>270.000</td>
<td>44.807</td>
<td>103.000</td>
<td>202.000</td>
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<td>$T_{\text{L}}$</td>
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<td>289</td>
<td>285</td>
<td>291</td>
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<td>277</td>
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<tr>
<td>$T_{\text{A}}$</td>
<td>5598</td>
<td>3523</td>
<td>10427</td>
<td>7852</td>
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<td>$T_{\text{Ar}}$</td>
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<td>10.293</td>
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<td>10.293</td>
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<td>$R_{\text{max}}$</td>
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<td>0.0822</td>
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<td>µg C d⁻¹</td>
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<td>$P_{\text{max}}$</td>
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<td>0.00054</td>
<td>0.00054</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>µg C d⁻¹</td>
</tr>
<tr>
<td>$k_p$</td>
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<td>120</td>
<td>120</td>
<td>120</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>µmole photon m⁻² s⁻¹</td>
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<tr>
<td>$T_{\text{Ap}}$</td>
<td>9026</td>
<td>9026</td>
<td>9026</td>
<td>9026</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>°K</td>
</tr>
<tr>
<td>$s_{\text{np}}$</td>
<td>716</td>
<td>1160</td>
<td>720</td>
<td>1104</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>nb (250 µm) ind⁻¹</td>
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<tr>
<td>$p_{\text{c}}$</td>
<td>0.46</td>
<td>0.40</td>
<td>0.30</td>
<td>0.37</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>fraction</td>
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<tr>
<td>Abundance</td>
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<tr>
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<td>1.40</td>
<td>0.37</td>
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<td>0.57</td>
<td>0.07</td>
<td>1.65</td>
<td>scaling factor</td>
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<tr>
<td>$b$</td>
<td>1.63</td>
<td>5.89</td>
<td>11.20</td>
<td>2.79</td>
<td>34.99</td>
<td>15.85</td>
<td>55.36</td>
<td>32.13</td>
<td>scaling factor</td>
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</table>
Table 3. Coefficient of determination ($R^2$) and in parenthesis, root mean squared error (RMSE) obtained between observed core tops relative abundance of the different foraminifer species and results of the models. Different subsets were used: the whole – worldwide dataset or a subset focused on the Atlantic Ocean. Both results originating from model simulation using satellites subsurface data, that take only seasonality in consideration, or the PISCES model results (data not showed), that take both seasonality and depth in consideration, as forcing variables for the simulation are indicated.

<table>
<thead>
<tr>
<th>Species</th>
<th>Satellite images (Seasons)</th>
<th></th>
<th>PISCES (Seasons and depth)</th>
<th></th>
</tr>
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<tbody>
<tr>
<td></td>
<td>Worldwide</td>
<td>Atlantic</td>
<td>Worldwide</td>
<td>Atlantic</td>
</tr>
<tr>
<td>O. universa</td>
<td>0.07 (3.28)</td>
<td>0.11 (2.78)</td>
<td>0.07 (3.24)</td>
<td>0.12 (2.64)</td>
</tr>
<tr>
<td>G. sacculifer</td>
<td>0.56 (17.46)</td>
<td>0.65 (12.61)</td>
<td>0.56 (12.38)</td>
<td>0.58 (9.94)</td>
</tr>
<tr>
<td>G. siphonifera</td>
<td>0.43 (6.00)</td>
<td>0.55 (5.11)</td>
<td>0.42 (5.29)</td>
<td>0.54 (4.61)</td>
</tr>
<tr>
<td>G. ruber</td>
<td>0.46 (17.76)</td>
<td>0.52 (16.49)</td>
<td>0.37 (23.14)</td>
<td>0.39 (21.78)</td>
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<tr>
<td>N. dutertrei</td>
<td>0.09 (17.23)</td>
<td>0.21 (11.82)</td>
<td>0.16 (17.53)</td>
<td>0.34 (13.64)</td>
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<tr>
<td>G. bulloides</td>
<td>0.37 (18.97)</td>
<td>0.57 (13.16)</td>
<td>0.28 (21.02)</td>
<td>0.37 (16.47)</td>
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<tr>
<td>N. incompta</td>
<td>0.39 (14.85)</td>
<td>0.40 (17.95)</td>
<td>0.31 (15.85)</td>
<td>0.28 (19.97)</td>
</tr>
<tr>
<td>N. pachyderma</td>
<td>0.85 (12.32)</td>
<td>0.84 (13.70)</td>
<td>0.81 (17.04)</td>
<td>0.80 (19.37)</td>
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<tr>
<td>Diversity</td>
<td>0.50 (0.52)</td>
<td>0.59 (0.43)</td>
<td>0.58 (0.48)</td>
<td>0.69 (0.45)</td>
</tr>
</tbody>
</table>
Fig. 1. Observed growth rate in laboratory experiments (Lombard et al., 2009b) for the different species (dots) compared to model outputs (line) after calibration under saturating food and light conditions. Resulting model parameters are listed in Table 2.
**Fig. 2.** Schematic explanation of the potential reasons of the growth rate-abundance coupling.  
**A** When prey abundance is high, individual growth rate is maximal (grey arrow) but there is a time lag between maximum individual growth rate and observed population abundance maximum (black arrow). When this time lag between maximum growth rate and maximum abundance is small, then a potential coupling between growth rate and abundance thus may be observed **B** in which the variability is due to the time lag. The small black arrows represent the time course of an assemblage development.
Fig. 3. Observed coupling between observed abundance in multinets samples and model-estimated growth rate ($\mu$) after calibration of the parameter $k_n$. The fit of each relationship between growth rate and abundance (black line) is indicated (see Table 2 for parameters) as well as the 95% confidence limits (dashed line).
Fig. 4. (Upper panel) Dominant species observed by Bé and Tolderlund (1971) within sea surface conditions (upper 10 m). Each colour represents a different dominant species assemblage (see key for the colour code). Dominant species simulated by the model (background colours) in surface conditions (annual average) by using satellite images (middle panel) or PISCES model (lower panel) as inputs. The model reproduces 70.5% of the 576 observations when using satellite images and 58.9% using PISCES model.
Fig. 5. Total >200 µm foraminifer abundance (ind m$^{-3}$) observed within sea surface conditions (Bé and Tolderlund, 1971; left panel) and simulated by the model (right panel) under sea surface condition by using satellite images (annual average).
Fig. 6. Relative foraminifer abundance (%) of the different species observed in core tops samples (left panel) calculated on the basis of the eight selected species and estimated by the model (right panel) using satellite images (monthly averages). Root mean squared error (RMSE) calculated between model simulation and estimations are given in Table 3.
Fig. 7. same as Fig. 6.
Fig. 8. Shannon diversity index calculated from core tops data using the eight selected species (upper panel) and simulated by the model (middle panel) by using satellite images. Mean model results (lower panel, line) and observations (dots) in the 40°–20° W (Mid Atlantic Ocean) where extracted for a better comparison. Root mean squared error (RMSE) calculated between model simulation and estimations are given in Table 3.
Fig. 9. Season when the modelled maximum growth rate occurs for *G. sacculifer*, *G. siphonifera*, *G. ruber* and *O. universa*. These species have been estimated to mainly live within the 0–10 m depth layer (simulation using PISCES data; data not showed) and then monthly average satellite images where used for a better simulation.
Fig. 10. Season (upper part) and depth (lower part) where the modelled maximum growth rate occurs for *N. dutertrei*, *G. bulloides*, *N. incompta* and *N. pachyderma*. These estimations originate from a simulation using PISCES data.