Dear reviewer,

We appreciate your constructive comments for our manuscript. We address your comments point-by-point in the following response.

The manuscript presents results from a modelling exercise to study how the delivery of annual rainfall impacts ecosystems. The Authors used scenarios of given annual rainfall amounts occurring at different rates (and thus different amounts per event) and with different durations of the rainy season; the scenarios are applied to Africa, focusing on biomass productivity (GPP) and soil moisture, which, as I understood, is interpreted to be the key driver of GPP. Even though the manuscript addresses a topic that is likely of interest to the audience of Biogeosciences, it is not well written; there are several grammatical errors and some parts (especially the methods) were not very clear. I have listed below specific comments as they appeared in the text.

Response: Thank you very much for your positive assessment and constructive comments. As this work aims to study the impact of intra-seasonal rainfall variability on ecosystem function (e.g. GPP) and biome distribution, we did use soil moisture pattern to explain the shifts in GPP and biome distribution.

In the revised manuscript, all the coauthors have helped improving the language and presentation. Please refer to the updated manuscript attached at the end of this reply.

- Page 7577, Line 11: it is not clear what the Author meant with ‘second-order climate statistics’.
Response: We change it to “intra-seasonal climate variabilities”.

- P7580, L10-15: the Authors mention here that MAP is given by the product of 3 rainfall characteristics, but in reality they define MAP as a product of 4 parameters, α, λ, Tw, and fw. I do not think that the term ‘normalized’ used in the context of ‘fw’ is correct here. I think it should also be said here that the rainfall statistics in the wet and dry season are not different (now, this is said at P7592). This part should be better explained.
Response: We realize that the writing in the previous manuscript causes the confusion, and we have clarified this point in the revised manuscript. Please see the following revised text:

“We manipulate rainfall changes through a stochastic weather generator based on a parsimonious model of rainfall processes (Rodriguez-Iturbe et al., 1984). We model the total amount of rainfall during wet season as a product of the three intra-seasonal rainfall characteristics for the wet season, rainfall frequency (λ, event/day), rainfall intensity (α, mm/event), and rainy season length (T_w, days) (More details in section 2.3).”

We actually treat wet and dry season separately for their frequency and intensity, which has been explained in detail in section 2.3. We also revised that section to make it clearer to follow:

“The stochastic rainfall model can be expressed as MAP=α λ T_w / f_w, and we set f_w to be 0.9, i.e. the period including 90% of total annual rainfall is defined as “rainy season” (exchangeable with “wet season” hereafter). In particular, we first use Markham (1970)’s...
approach to find the center of the rainy season, and then extend the same length to both sides of the center until the total rainfall amount in this temporal window (i.e. “rainy season”) is equal to 90% of the total annual rainfall. Rainy season and dry season have their own rainfall frequency and intensity. Two seasons are separately modeled based on the Market Poisson Process. Here we only focus on and manipulate rainy-season rainfall characteristics in our study, as rainy-season rainfall accounts for almost all the meaningful rainfall inputs for plant use. Thus in the following paper, whenever we mention $\alpha$ or $\lambda$, we refer to the rainy season.”

- P7580, L19: this line repeats exactly what said 3 lines before.
Response: We revised this part as follows:
“The SEIB-DGVM also allows the development of annual and perennial grasses as well as multiple life cycles of grass at one year based on environmental conditions. Multiple life cycles of tree growth per year are possible in theory but rarely happen in simulations (Sato and Ise, 2012). Soil moisture status is a predominant factor to determine the optimum LAI of the grass layer, which influences maximum daily production and leaf phenology.”

- P7581, L12: what is the rooting depth adopted in the model. Did it vary spatially?
Response: Each plant-functional-type (PFT) in the SEIB-DGVM model has its own inherent rooting depth. Thus rooting depths vary explicitly in space based on the biome distribution, resulted from vegetation dynamics and competition. Different rooting depth also means that each plant simulated in the SEIB-DGVM has different capacity to use soil moisture at different layers of soil. We clarify this point in the revised manuscript.

- P7581, L17: the Authors mention here that ‘other environmental conditions’ affect Lai and so NPP. What are these other conditions? The Authors focus on soil moisture, which is considered the main variable and it is used to interpret the data. However, I think it would be better to report also other variables and explain why their role is not as important as soil moisture.
Response: We tended to be more inclusive and that is why we wrote “other environmental conditions”. In reality, the soil moisture pattern can explain most changes of GPP in woodlands and savannas (Figure 5). The only divergence happens in the tropical forests (Figure 5a and 5b), which is mostly due to the reason that tropical forests in SEIB-DGVM are not water-limited but radiation-limited. Thus, though soil moisture increases with increased rainfall frequency in tropical forests (Figure 5a), GPP instead decreases due to increased cloudiness (Figure 5b), as we have already discussed in Section 3.1 (specifically Pattern 1.3).

For the relevant text, we have changed it as follows:
“Soil moisture status is the predominant factor to determine LAI of the grass layer, which influences maximum daily productivity and leaf phenology. When LAI exceeds 0 for 7 continuous days, dormant phase of perennial grass layer changes into growth phase. While when LAI falls below 0 for 7 continuous days, growth phase switches to dormant phase (Sato et al, 2007).”
Response: This part has been revised as follows:

“Two plant function types (PFTs) of tropical woody species are simulated by the SEIB-DGVM in Africa: tropical evergreen trees and tropical deciduous trees. The distribution of these two woody types is largely determined by hydro-climatic environments in the model. Tropical evergreen trees only develop in regions where water resources are sufficient all year around, so they can maintain leaves for all seasons; otherwise, tropical deciduous trees could survive and dominate the landscape as they can shed leaves if there is no sufficient water supply in its root zone during the dry season (Sato and Ise, 2012).”

Response: We repeatedly use the 30-year climate forcing for 2000 years for the spin-up period. We have clarified this point in the revised manuscript.

Response: We recognize the reviewer’s concern, though we are afraid that there is a misunderstanding here. Figure 1 provides the spatial patterns of rainfall frequency, intensity and rainy season length, and these spatial patterns do not reflect the temporal feature of the rainfall distribution at a single point.

The Market Poisson process has been validated and widely used as a stochastic rainfall model in the past (see the following references [1]-[4] have been cited in the manuscript too). Thus, we feel that citing these references may be sufficient here for the methods, and we have also clarified the text to make it easier to follow.

References:

Response: We recognize the reviewer’s concern, though we are afraid that there is a misunderstanding here. Figure 1 provides the spatial patterns of rainfall frequency, intensity and rainy season length, and these spatial patterns do not reflect the temporal feature of the rainfall distribution at a single point.

The Market Poisson process has been validated and widely used as a stochastic rainfall model in the past (see the following references [1]-[4] have been cited in the manuscript too). Thus, we feel that citing these references may be sufficient here for the methods, and we have also clarified the text to make it easier to follow.

References:
order to understand the results.

Response: Thanks for pointing this out. We have revised the relevant text as follows:

“The stochastic rainfall model can be expressed as MAP = α λ Tw / fw, and we set fw to be 0.9, i.e. the period including 90% of total annual rainfall is defined as “rainy season” (exchangeable with “wet season” hereafter). In particular, we first use Markham (1970)'s approach to find the center of the rainy season, and then extend the same length to both sides of the center until the total rainfall amount in this temporal window (i.e. “rainy season”) is equal to 90% of the total annual rainfall. Rainy season and dry season have their own rainfall frequency and intensity. Two seasons are separately modeled based on the Market Poisson Process. Here we only focus on and manipulate rainy-season rainfall characteristics in our study, as rainy-season rainfall accounts for almost all the meaningful rainfall inputs for plant use. Thus in the following paper, whenever we mention α or λ, we refer to the rainy season.”

Also see:

“All the necessary parameters to fit for the stochastic rainfall (including the mean and variance of rainfall frequency, intensity and length of wet and dry seasons) were derived from the satellite-gauge-merged rainfall measurement from TRMM 3b42V7 (Huffman et al., 2007) for the period of 1998 to 2012, based on the above assumptions for the rainfall process. Specifically, we applied our definition of “rainy season” to each year of the TRMM rainfall data for per pixel, and calculated the mean and variance of the “rainy season length”, using which we fitted the beta distribution for Tw. For rainfall frequency and intensity, we lumped all the wet or dry season rainfall record together to derive their parameters.”

- P7586, L6-7: rainfall intensity is defined as 1 mm, which is a depth. It should be 1mm day-1 or it should be referred to as rainfall depth per event.

Response: We revised the unit for rainfall intensity as: mm/event; the unit for rainfall frequency as: events/day. Thanks for pointing this out.

- P7587, L13-16: this phrase was not clear to me. Please, re-phrase.

Response: We revised the text as follows:

“The relationship of GPP sensitivity to MAP and rainfall intensity (Fig. 6c) is complex and has no clear patterns as previous ones, mostly because the GPP sensitivity space that most pixels cluster (Fig. A4c) also contains large uncertainties (Fig. A4d, shown as large variance in the data). Thus we will not over-interpret the pattern in Fig. 6c.”

- P7588, L3: how is s* defined?

Response: We put the following text under the Equation (2) in the revised manuscript:

“Figure 2 provides a schematic diagram of “water stress factor” from the SEIB-DGVM, and we also include an approximated linear model that has been widely adopted elsewhere (e.g. Milly, 1992; Porporato et al., 2001). The linear model uses an extra variable S*, so called “critical point” of soil moisture: when S>S*, there is no water stress (water stress factor =1); and when S<S*, water stress factor linearly decreases with the decrease of S. Though SEIB-DGVM adopts a quadratic form for “water stress factor”, it essentially functions
similarly as the linear model, such that \( S^* \) distinguishes two soil moisture regimes that below which there is a large sensitivity of water stress to soil moisture status, and above which there is little water stress. Understanding how this “water stress factor” functions is the key to explain the following results.”

- P7591, L24: I do not think that the term ‘understand’ is correct here. Considering the limitations of the model, the model is used for interpretation more than understanding.
Response: We accept the reviewer’s suggestion, and change “understand” to be “interpret”.

- P7592, L11-12: I would erase the word ‘still’ (‘: : in reality they have seasonal variations’).
Response: We accept the reviewer’s suggestion and have made the corresponding revision.

- P7593, L12: a rainfall frequency of 0.35 day-1 is not very low.
Response: We change to the following text:
“We identify that negative GPP sensitivity with increased rainfall frequency is possible at very low MAP range (\(~400 \text{ mm year}^{-1}\) with relatively low rainfall frequency (<0.35 events/day) (Fig. 6a)”.

- P7594, L15-16: I thought \( \alpha \) and \( \lambda \) also described the dry season. This is confusing.
Response: We agree that our text is confusing and we made the changes to clarify it.

In the rainfall model, we have wet season (including 90\% of the total annual rainfall) and dry season (having 10\% of the total annual rainfall). Wet season and dry season have their own rainfall frequency and intensity, derived from the TRMM rainfall data. In the experiments we only apply the changes of rainfall frequency/intensity for wet season, while always use the climatological value for dry season. For example, if we need to increase rainfall frequency by 10\% in one experiment, we only apply the change to the wet-season rainfall frequency, and keep the dry-season rainfall frequency unchanged, and then we use the Market Poisson Process to simulate the daily rainfall for wet and dry season separately.

Thus when we use “rainfall frequency” and “rainfall intensity” in the manuscript, we refer to the values during wet-season, as dry-season rainfall characteristics are fixed at the climatological values. Besides, dry-season also only accounts for 10\% of the total rainfall, and has little importance for the ecosystem changes.

We have clarified this point in the revised manuscript as follows:
“We identify that negative GPP sensitivity with increased rainfall frequency is possible at very low MAP range (\(~400 \text{ mm year}^{-1}\) with relatively low rainfall frequency (<0.35 events/day) (Fig. 6a)”.

Thus when we use “rainfall frequency” and “rainfall intensity” in the manuscript, we refer to the values during wet-season, as dry-season rainfall characteristics are fixed at the climatological values. Besides, dry-season also only accounts for 10\% of the total rainfall, and has little importance for the ecosystem changes.

We have clarified this point in the revised manuscript as follows:
“\( \text{The stochastic rainfall model can be expressed as MAP} = \alpha \lambda Tw / fw, \text{ and we set } fw \text{ to be } 0.9, \) i.e. the period including 90\% of total annual rainfall is defined as “rainy season” (exchangeable with “wet season” hereafter). In particular, we first use Markham (1970)’s approach to find the center of the rainy season, and then extend the same length to both sides of the center until the total rainfall amount in this temporal window (i.e. “rainy season”) is equal to 90\% of the total annual rainfall. Rainy season and dry season have their own rainfall frequency and intensity. Two seasons are separately modeled based on the Market Poisson Process. Here we only focus on and manipulate rainy-season rainfall
characteristics in our study, as rainy-season rainfall accounts for almost all the meaningful rainfall inputs for plant use. Thus in the following paper, whenever we mention $\alpha$ or $\lambda$, we refer to the rainy season.”

- Fig. 1: panel b: rainfall intensity should be depth. Panels e-h do not look like histograms; how were they normalized?
  Response: Thanks for pointing this out. They are normalized histogram that the areas of the histogram should be added up to 1, but we forgot to provide the bins of x-axis for each data in the figure caption. We attached the bins for the histogram in the revised manuscript:
  “e-f: Normalized histograms of the rainfall characteristics in two savanna regions of West and Southwest Africa. e-MAP (bin width for the x-axis: 100 mm/year); f-rainfall intensity (bin width for the x-axis: 1 mm/event); g-rainfall frequency (bin width for the x-axis: 0.1 event/day); h-rainy season length (bin width for the x-axis: 20 days).”

- Fig. 2: I would remove this figure.
  Response: We accept the reviewer’s suggestion and have removed this figure in the revised manuscript.

- Fig. 3: this figure is not very useful. The linearized model and $S^*$ are not used here.
  Response: We decide to keep this figure as it helps the explanations of the hydrological mechanism. We also added the explanation of $S^*$ under the Equation (2):
  “Figure 2 provides a schematic diagram of “water stress factor” from the SEIB-DGVM, and we also include an approximated linear model that has been widely adopted elsewhere (e.g. Milly, 1992; Porporato et al., 2001). The linear model uses an extra variable $S^*$, so called “critical point” of soil moisture: when $S>S^*$, there is no water stress (water stress factor =1); and when $S<S^*$, water stress factor linearly decreases with the decrease of $S$. Though SEIB-DGVM adopts a quadratic form for “water stress factor”, it essentially functions similarly as the linear model, such that $S^*$ distinguishes two soil moisture regimes that below which there is a large sensitivity of water stress to soil moisture status, and above which there is little water stress. Understanding how this “water stress factor” functions is the key to explain the following results.”

Also, I believe that this is not a water stress factor as defined in Porporato et al. (2001), but is more a reduction function for transpiration. The water stress is lower at high soil moisture and increases as soil moisture decreases.
  Response: The reviewer’s assessment is correct that Equation (1) and (2) provide a reduction function for transpiration; what we are saying here is that this concept is similar as Porporato et al. (2001), which is basically the reversed form of Equation (2).
  We clarified this point in the revised manuscript.

Fig. 6: it would be nice to have more explanation in the text on how this figure is generated.
  Response: We have added the following text in the revised manuscript:
  “Figure 6 further shows the difference of simulated GPP as a function of MAP and a perturbed rainfall characteristic in the corresponding experiment, to explore how MAP and
these rainfall characteristics affect the simulated GPP. We term Figure 6 as “GPP sensitivity space”, and “positive GPP sensitivity” means that GPP changes at the same direction with MAP or rainfall characteristics, and vise versa for “negative GPP response”. These “GPP sensitivity spaces” are generated based on the aggregated mean GPP in each bin of the rainfall properties. The bin size for MAP, rainfall frequency, rainfall intensity and rainy season length are 100 mm/year, 0.05 event/day, 1 mm/event and 15 days respectively. We also provide the standard error (SE) of GPP in each bin to assess the uncertainties of the “GPP sensitivity spaces”, with higher SE meaning larger uncertainties.

Again, thank you very much for taking your precious time in reviewing our manuscript and providing constructive comments! Please let us know whether you are satisfied with our responses, and we will try our best to address any extra concerns and suggestions.

Best wishes,
Kaiyu Guan, on behalf of all the authors

The attached files:
1) revised manuscript with all the editing marks
2) final revised manuscript without any marks
Continental-scale impacts of intra-seasonal rainfall variability
on simulated ecosystem responses in Africa

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Running title: Ecological Impacts of Intra-Seasonal Rainfall Variability
Submitted to Biogeosciences
Abstract:

Climate change is expected to result in an increase of intra-seasonal rainfall variability, which has arisen from concurrent shifts in rainfall frequency, intensity and seasonality. These changes in intra-seasonal rainfall variability are likely to have important ecological impacts for terrestrial ecosystems. Yet, quantifying these impacts across biomes and large climate gradients is largely missing. This gap hinders our ability to predict ecosystem services and their responses to climate change, especially for arid and semi-arid ecosystems. Here we use a synthetic weather generator and an independently validated advanced vegetation dynamic model (SEIB-DGVM) to virtually conduct a series of “rainfall manipulation experiments” to study how changes in the intra-seasonal rainfall variability affect continent-scale ecosystem responses across Africa. We generated different rainfall scenarios with fixed total annual rainfall but shifts in: i) frequency vs. intensity, ii) rainy season length vs. frequency, iii) intensity vs. rainy season length. These scenarios were fed into the SEIB-DGVM to investigate changes in biome distributions and ecosystem productivity. We find a loss of ecosystem productivity with increased rainfall frequency and decreased intensity at very low rainfall regimes (<400 mm/year) and low frequency (<0.3 day-1 event/day); beyond these very dry regimes, most ecosystems benefit from increasing frequency and decreasing intensity, except in the wet tropics (>1800 mm/year) where radiation limitation prevents further productivity gains. This finding reconciles seemingly contradictory findings in previous field studies on the direction of rainfall frequency/intensity impacts on ecosystem productivity. We also find that changes in rainy season length can yield more dramatic ecosystem responses compared with similar percentage changes in rainfall frequency or intensity, with the largest impacts in semi-arid woodlands. This study demonstrates that not all rainfall regimes are ecologically equivalent, and that intra-seasonal rainfall characteristics play a significant role in influencing ecosystem function and structure through controls on ecohydrological processes. Our results also suggest that shifts in rainfall seasonality have potentially large impacts on terrestrial ecosystems,
something that and these understudied impacts should be explicitly examined in future studies of climate impacts.

Keywords: rainfall frequency, rainfall intensity, rainfall seasonality, biome distribution, Gross Primary Production (GPP), Africa
1. Introduction

Due to increased water holding capacity in the atmosphere as a consequence of global warming (O’Gorman and Schneider, 2009), rainfall is projected to vary in intensity and frequency across much of the world (Easterling et al., 2000; Trenberth et al., 2003; Chou et al., 2013), in conjunction with complex shifts in rainfall seasonality (Feng et al., 2013; Seth et al., 2013). These changes possibly indicate a large increase in the frequency of extreme events and variability in rainfall (Easterling et al., 2000; Allan and Soden, 2008), and many of these changes may be accompanied with little changes in total annual rainfall (Knapp et al., 2002; Franz et al., 2010). Meanwhile, regions sharing similar mean climate state may have very different intra-seasonal dynamics, and the ecological significance of intra-seasonal climate variabilities, second order climate statistics has been largely overlooked previously in terrestrial biogeography (Good and Caylor, 2011). For example, ecosystems in West Africa and Southwest Africa (Figure 1) share similar total annual rainfall, but West Africa has much more intense rainfall events within a much shorter rainy season, while Southwest Africa has a longer and less intense rainy season. The same amount of total rainfall can come in very different ways, which may cause distinctive ecological-ecosystem responses and landscape structure. Understanding the impacts of these regional differences in intra-seasonal rainfall variability and their possible future changes on terrestrial ecosystems is critical for maintaining ecosystem services and planning adaptation and mitigation strategies for ecological and social benefits (Anderegg et al., 2013).

[insert Figure 1]

The changes in intra-seasonal rainfall characteristics, specifically frequency, intensity and seasonality, have critical significance to ecosystem productivity and structure (Porporato et al., 2001; Weltzin et al., 2003; Williams and Albertson, 2006; Good and Caylor, 2011; Guan et al., 2014), but previous studies on this topic (summarized in Table 1) have their limitations in the following aspects. First, existing...
relevant field studies on this topic mostly focus on a single ecosystem, i.e. grasslands, and subsequently only low rainfall regimes have been examined to date (mostly below 800 mm/year, see Table 1). Grasslands have the largest sensitivity to hydrological variabilities among all natural ecosystems (Scanlon et al., 2005; Guan et al., 2012), however inferences drawn from a single ecosystem are limited in scope and difficult to apply to other ecosystems and rainfall regimes. Second, even within grasslands, different studies have seemingly contradictory findings (see Table 1), and there is a lack of a comprehensive framework to resolve these inconsistencies. Specifically, whether increased rainfall intensity with decreased rainfall frequency has positive (Knapp et al., 2002; Fay et al., 2003; Robertson et al., 2009; Heisler-White et al., 2009) or negative impacts (Heisler-White et al., 2009; Thomey et al., 2011) on grassland productivity is still under debate. Third, previous relevant studies mostly focus on the impacts of rainfall frequency and intensity (Table 1 and Rodríguez-Iturbe and Porporato, 2004), and largely neglect the possible changes in rainfall seasonality. Rainfall frequency and intensity mostly describe rainfall characteristics within the rainy season, but do not account for the impacts of interplay between rainy season length and dry season length (Guan et al., 2014). For ecosystems predominately controlled by water availability, rainy season length constrains the temporal niche for active plant physiological activities (van Schaik et al., 1993; Scholes and Archer, 1997), and large variations in rainfall seasonality can lead to significant shifts in biome distribution found from paleoclimate pollen records (e.g. Vincens et al., 2007). Given changes in rainfall seasonality have been found in various tropical regions (Feng et al., 2013) and have been projected in future climate (Biasutti and Sobel, 2009; Shongwe et al., 2009; Seth et al., 2013), studies investigating their impacts on terrestrial ecosystems are relatively rare, and very few field studies are designed to address this aspect (Table 1, Bates et al., 2006; Svejcar et al., 2003; Chou et al., 2008). Finally, there is an increasing trend of large-scale studies addressing rainfall variability and ecological responses using satellite remote sensing (Fang et al., 2005; Zhang et al., 2005; Good and Caylor, 2011; Zhang et al., 2013; Holmgren et al., 2013) and flux network data (Ross et al., 2012). These large-scale studies are able to
expand analyses to more types of ecosystems and different climate conditions, and provide valuable observation-based insights. However there are very few theoretical modeling works to corroborate this effort. All these above issues call for a comprehensive modeling study to investigate different aspects of intra-seasonal rainfall variability on terrestrial ecosystems spanning large environmental gradients and various biomes.

In this paper, we aim to study ecological impacts of intra-seasonal rainfall variability on terrestrial ecosystems. In particular, we design virtual “rainfall manipulation experiments” to concurrently shift intra-seasonal rainfall characteristics without changing total annual rainfall. We focus on the impacts of these different rainfall scenarios on ecosystem productivity (e.g. Gross Primary Production, GPP) and biome distributions in the African continent, simulated by an advanced independently validated dynamic vegetation model SEIB-DGVM (Sato and Ise, 2012). Previous modeling approaches in this topic (Gerten et al., 2008; Hély et al., 2006) designed various rainfall scenarios by rearranging (halving, doubling or shifting) the rainfall amount based on the existing rainfall observations. In contrast to these approaches, we design a weather generator based on a stochastic rainfall model (Rodríguez-Iturbe et al., 1999), which allows us to implement a series of experiments by synthetically varying two of the three rainfall characteristics (rainfall intensity, rainfall frequency, and rainy season length) while fixing total annual rainfall at the current climatology. We choose Africa as our test-bed mostly because the following two reasons: (1) the rainfall regimes and biomes have large gradients varying from extremely dry grasslands to highly humid tropical evergreen forests, and thereby provide a large pool of different biomes; (2) Africa is a continent usually assumed to have few temperature constrains (Nemani et al., 2003), which will help to isolate the impacts of precipitation from temperature, as one challenge in attributing climatic controls on temperate ecosystems or Mediterranean ecosystems is the superimposed influences from both temperature and precipitation. The overarching science question we will address is: How do African ecosystems respond to possible changes in intra-seasonal rainfall variability (i.e. rainfall frequency, intensity and rainy
2. Materials and Methods:

2.1 Methodology overview

Table 1 summarizes previous field-based rainfall manipulation experiments, such as the one that Knapp et al. (2002) did in a grassland that concurrently increasing rainfall frequency and decreasing rainfall intensity while fixing total rainfall for a grassland. The central idea of our study is to design similar rainfall manipulation experiments but test them virtually in the model domain across large environment gradients. We manipulate rainfall changes through a weather generator based on a parsimonious stochastic rainfall model (Rodriguez-Iturbe et al., 1984). We model the total amount of rainfall during rainy season as a product of the three intra-seasonal rainfall characteristics for the rainy season, rainfall frequency (λ, event/day), rainfall intensity (α, mm/event), and rainy season length (T_w, days). (More details in section 2.3) We manipulate rainfall changes through a stochastic weather generator based on a parsimonious model of rainfall processes: statistically for the daily rainfall record, the mean annual precipitation (MAP) is a product of the three rainfall characteristics for the wet season, rainfall frequency (λ, day^-1), rainfall intensity (α, mm), and rainy season length (T_w, days), normalized by f_w (the fraction of wet season rainfall to the MAP) to account for the contribution from dry season rainfall (MAP=α λ T_w / f_w). Thus it is possible to simultaneously perturb two of the rainfall characteristics away from their climatological values while preserving the mean annual precipitation (MAP) unchanged. (Figure 2). We then feed these different rainfall scenarios into a well-validated dynamic vegetation model (SEIB-DGVM, section 2.2) to study simulated ecosystem responses. Detailed experiments design is described in section 2.5.

[insert Figure 2]
2.2 SEIB-DGVM model and its performances in Africa

We use a well-validated vegetation dynamic model SEIB-DGVM (Sato et al., 2007) as the tool to study ecosystem responses to different rainfall variabilities. This model follows the traditional “gap model” concept (Shugart, 1998) to explicitly simulate the dynamics of ecosystem structure and function for individual plants the dynamics of fine scale ecosystem structure and function for a set of virtual vegetation patches, and uses results at these virtual patches as a surrogate to represent large-scale ecosystem states. Thus individual trees are simulated from establishment, having competition with other plants, to death—which creates “gaps” in which different plant function types (PFTs) to other plants to occupy and develop. The SEIB-DGVM includes mechanical-based and empirical-based algorithms for land physical processes, plant physiological processes, and plant dynamic processes. The SEIB-DGVM contains algorithms that explicitly involve the mechanisms of plant-related water stress (Figure 2; Sato and Ise, 2012). With similar concepts to previous studies (e.g. Milly, 1992; Porporato et al., 2001), the current SEIB model SEIB-DGVM implements a continuous “water stress factor” (Equation 2) based on the soil moisture status (Equation 1), scaling from 0 (most stressful) to 1 (with no stress), which then acts to scale the stomatal conductance for plant transpiration and carbon assimilation.

\[
\text{stat}_{\text{water}} = \frac{(S - S_w)}{(S_f - S_w)} \quad \text{(Equation 1)}
\]

\[
\text{Water stress factor} = 2 * \text{stat}_{\text{water}} - \text{stat}_{\text{water}}^2 \quad \text{(Equation 2)}
\]

where S, S_w and S_f refer to the fraction of volumetric soil water content within the rooting depth, at the wilting point, and at field capacity, respectively. Figure 2 provides a schematic diagram of “water stress factor” from the SEIB-DGVM, and we also include an approximated linear model that has been widely adopted elsewhere (e.g. Milly, 1992; Porporato et al., 2001). The linear model uses an extra variable S*, so called “critical point” of soil moisture: when S>S*, there is no water stress (water stress factor = 1); and when S<S*, water stress factor linearly decreases with the decrease of S. Though SEIB-DGVM adopts a quadratic form for “water stress factor”,...
it essentially functions similarly as the linear model, such that $S^*$ distinguishes two soil moisture regimes that below which there is a large sensitivity of water stress to soil moisture status, and above which there is little water stress. Understanding how this “water stress factor” functions is the key to explain the following results.

[insert Figure 2]

The SEIB-DGVM also allows the development of annual and perennial grasses as well as multiple life cycles of grass at one year based on environmental conditions, and multiple life cycles of tree growth per year are possible in theory but rarely happen in simulations (Sato and Ise, 2012). Soil moisture status is the predominant factor to determine LAI of the vegetation layer, which influences maximum daily productivity and leaf phenology. In particular, life cycles of grass are under prominent control of soil moisture status. The previously defined “water stress factor” and other environmental conditions co-determine the optimum LAI of the grass layer, which influences maximum daily NPP and the leaf phenology. When optimum LAI exceeds 0 for preceding 7 continuous days, the dormant phase of perennial vegetation layer changes into the growth phase. While when optimum LAI falls below 0 for preceding 7 continuous days, the growth phase changes into the dormant phase (Sato et al, 2007). SEIB-DGVM also explicitly simulates the light conditions and light competions among different PFTs in the landscape based on its simulated 3D canopy structure and radiative transfer scheme (Sato et al, 2007).

[insert Figure 3]

The SEIB-DGVM has been tested both globally (Sato et al., 2007) and regionally for various ecosystems (Sato et al., 2010; Sato, 2009; Sato and Ise, 2012), whose simulated results compared favorably with ground observations and satellite remote sensing measurements in terms of ecosystem composition, structure and function. In particular, the SEIB-DGVM has been successfully validated and
demonstrated its ability in simulating ecosystem structure and function in the African continent (Sato and Ise, 2012). Two plant function types (PFTs) of tropical woody species are simulated by SEIB-DGVM in Africa: tropical evergreen trees and tropical deciduous trees. The distribution of these two woody types in the simulation is largely determined by hydro-climatic environments. Tropical evergreen trees only develop leaves for all seasons; otherwise, tropical deciduous trees could survive and dominate the landscape as they can shed leaves if there is no sufficient water supply in its root zone during the dry season (Sato and Ise, 2012). For woody species, two plant function types (PFTs) of tropical woody species are modeled in Africa: tropical evergreen trees and tropical deciduous trees, which distinguish in their phenology, with the former having leaves all year around, and the latter shedding leaves during dry season, which is mostly controlled by root-zone moisture status (Sato and Ise, 2012). Trees and grasses coexist in a cell, with the floor of a virtual forest monopolized by one of the two grass PFTs, C₃ or C₄ grass. The dominating grass type of which type is determined at the end of each year by air temperature, precipitation, and CO₂ partial pressure (Sato and Ise, 2012).

The SEIB model SEIB-DGVM was run at a one degree spatial resolution and at a daily temporal resolution step. It was spun-up for 2000 years driven by the observed climate (1970-2000) repeatedly for the soil carbon pool to reach steady state, followed by 200 years simulation driven by the forcings based on the experiment design in Section 2.4. Because our purpose is to understand the direct impacts of intra-seasonal rainfall variability, we turned off the fire component of the SEIB model SEIB-DGVM to exclude fire-mediated feedbacks in the results. Though we are fully aware of the important role of fire in interacting with rainfall seasonality and thus in their influencing on African ecosystems' productivity and structures (Bond et al., 2005; Lehmann et al., 2011; Staver et al., 2012), studying these interactions is beyond the scope of this work. For the similar reason, we fixed the atmospheric CO₂ concentration at 380 ppmv to exclude possible impacts of CO₂ fertilization effects.
2.3 Synthetic weather generator

The synthetic weather generator used here consists of two major components: i) to stochastically generate daily rainfall based on a stochastic rainfall model, and ii) to conditionally sample all other environmental variables from historical records to preserve the covariance among climate forcing inputs variables.

The stochastic rainfall model can be statistically expressed as \( \text{MAP} = \alpha \lambda T_w / f_w \), and we set \( f_w \) to be 0.9, i.e. the period including 90% of total annual rainfall is defined as “wet rainy season” (exchangeable with “rainy wet season” hereafter). In particular, we first use Markham (1970)’s approach to find the center of the rainy season, and then extend the same length to both sides of the center until the total rainfall amount in this temporal window (i.e. “rainy season”) is equal to 90% of the total annual rainfall. Rainy season and dry season have their own rainfall frequency and intensity. Two seasons are separately modeled based on the Market Poisson Process. Here we only focus on and manipulate rainy-season rainfall characteristics in our study, as rainy-season rainfall accounts for almost all the meaningful rainfall inputs for plant use. Thus in the following paper, whenever we mention \( \alpha \) or \( \lambda \), we refer to those during the rainy season.

The “wet season” and “dry season” rainfall time series are respectively modeled using the Marked Poisson Process. In this rainfall model, any day can be either rainy or not, and a rainy day is counted as one rainy event; rainfall events occur as a Poisson Process, with the parameter \( 1/\lambda \) (unit: days/event) being the mean intervals between rainfall events, and rainfall intensity \( \alpha \) for each rainfall event following an exponential distribution, with \( \alpha \) being the mean rainfall intensity per event (Rodríguez-Iturbe et al., 1999). The wet season length is modeled as a beta distribution bounded from 0 to 1, scaled by 365 days. All the necessary parameters to fit for the stochastic rainfall model climatological values of these rainfall characteristics (including the mean and variance of rainfall frequency, intensity and length of wet and dry seasons) were derived from the satellite-gauge-merged rainfall measurement from TRMM 3b42V7 (Huffman et al., 2007) for the period of 1998 to 2012, based on the above assumptions for the rainfall process. Specifically, we...
applied our definition of “rainy season” to each year of the TRMM rainfall data for
per pixel, and calculated the mean and variance of the “rainy season length”, using
which we fitted the beta distribution for $T_r$. For rainfall frequency and intensity, we
lumped all the wet or dry season rainfall record together to derive their parameters.
The two steps of the synthetic weather generator are described as below:

**Step 1:** Model the daily rainfall following the Marked Poisson process described
above. In particular, for a specific year, we first stochastically generate the wet season
length by sampling from the beta distribution, and the dry season length is determined
accordingly. Then we generate the daily rainfall for wet and dry season respectively.

**Step 2:** Based on the simulated daily rainfall time series in Step 1, we conditionally
sample temperature, wind, and humidity from the Global Meteorological Forcing
Dataset (GMFD, Sheffield et al., 2006), as well as cloud fraction and soil temperature
from the Climate Forecast System Reanalysis (CFSR) from National Centers for
Environmental Prediction (NCEP) (Saha et al., 2010). To sample for a specific day, all
the historical record within a 21-day time window centered at that specific day makes
up a sampling pool. For each day, a sample is randomly drawn from a pool that covers
all the historical record within a 21-day time window centered at the sampling day.

From the sampling pool, we find choose the day such that the historical rainfall
amount of the chosen day is within (100-30)% to (100+30)% of the simulated daily
rainfall amount. We then draw all other environmental variables (except rainfall)
on that sampled day to the new climate forcing. If we can find a sample from the pool
based on the above rule, this sampling is called “successful”. When there is more than
one suitable sample, we randomly select one. When there is no suitable sample, we
randomly select one day within the pool. The mean “successful” rate for all the
experiments and ensembles and all the experiments across Africa is 83%.

The GMFD data (Sheffield et al., 2006) blends reanalysis data with observations
and disaggregates in time and space, and is available from 1948 to 2008, with
1.0-degree spatial resolution and daily temporal resolution. The CFSR data (Saha et
al., 2010) provides cloud fraction and simulated soil temperature from three soil
layers for the SEIB model. The CFSR version that we used is from 1979 to 2010, and
the original 0.3-degree spatial resolution and 6-hourly temporal resolution are aggregated to 1.0 degree and daily.

To test the validity of the synthetic weather generator, we ran the SEIB model SEIB-DGVM using the historical climate record (S_climatology) and the synthetic forcing (S_control), with the latter generated using the weather generator based on the rainfall characteristics derived from the former. Figure S1 shows that the SEIB model SEIB-DGVM simulations driven by these two different forcings generate similar biome distributions with a Cohen’s Kappa coefficient of 0.78 (Cohen, 1960), and similar GPP patterns in Africa, with the linear fits of annual GPP as:

\[
GPP(S_{\text{control}}) = 1.03 \times GPP(S_{\text{climatology}}) + 0.215 \quad (R^2 = 0.89, \ P < 0.0001). 
\]

Both biome and GPP patterns are consistent with observations (Sato and Ise, 2012). These results provide confidence in using the synthetic weather generator and SEIB-DGVM to conduct the further study.

2.4 Experiment design

Three experiments are designed as follows, and are shown in the conceptual diagram (Figure 2):

**Exp 1** (Perturbation of rainfall frequency and intensity, and the experiment is termed as S_\lambda hereafter, with S referring “Scenario”) Simulations forced by the synthetic forcings with varying \( \lambda \) and \( \alpha \) simultaneously for wet season (20% increases of \( \lambda \) and corresponding decreases of \( \alpha \) to make MAP unchanged; 20% decreases of \( \lambda \) and corresponding increases of \( \alpha \) to make MAP unchanged; no change for dry season rainfall characteristics), while fixing \( T_w \) at the current climatology;

**Exp 2** (Perturbation of rainfall frequency and rainy season length, termed as S_Tw_\lambda) Simulations forced by the synthetic forcing with varying \( T_w \) and \( \lambda \) simultaneously for wet season (20% increases of \( T_w \) and corresponding decreases of \( \lambda \) to make MAP unchanged; 20% decreases of \( T_w \) and corresponding increases of \( \lambda \) to make MAP unchanged; no change for dry season characteristics), while fixing \( \alpha \) at the current climatology;

**Exp 3** (Perturbation of rainy season length and intensity, termed as S_Tw_\alpha) Simulations
forced by the synthetic forcing with varying $T_w$ and $\alpha$ simultaneously for wet season
(20% increases of $T_w$ and corresponding decreases of $\alpha$ to make MAP unchanged;
20% decreases of $T_w$ and corresponding increases of $\alpha$ to make MAP unchanged; no
change for dry season characteristics), while fixing $\lambda$ at the current climatology.

Because $\lambda$ and $T_w$ have bounded ranges ($\lambda \sim [0, 1]$ and $T_w \sim [0, 365]$), if these two
variables after perturbation—updated value exceeds the range, we would force the
new updated value to be the lower or upper bound, and rearrange the other
corresponding variable—rainfall characteristic to ensure MAP unchanged. Each rainfall
scenario has six ensemble realizations of synthetic climate forcings to account for the
stochasticity of our synthetic weather generator.

For example in Exp 1, if after 10% increase the updated $\lambda$ is larger than 1, we would
force the updated $\lambda$ to be 1, and recalculate the changes in $\alpha$ to keep MAP the same as
before. All the scenarios have six ensemble runs differentiated in their synthetic
forcings to account for the stochasticity of the synthetic weather generator.

3. Results

We present the differences in simulated biome distributions of the three experiments
(i.e. $S_{\lambda} - \lambda$, $S_{T_w} - \lambda$, $S_{T_w} - \alpha$) in Figure 4 and Figure 3, and Figure S2 and S3 for their spatial
patterns are shown in Figure S2 and S3, and the differences in simulated annually
averaged soil moisture and GPP for each experiment are shown in Figure S5 and S4.
These differences indicate that the simulated ecosystem sensitivity to the
slight perturbation away from the current climatology of intra-seasonal rainfall
characteristics deviating from the current climatology. We present the differences
between +20% and -20% changes in each experiment. We also assessed shifts of +/−
10%, and found that these responses are similar with only smaller magnitudes and
thus not shown here. To further explore how MAP and these rainfall characteristics
affect the simulated GPP, Figure 5 shows plots of the difference in simulated
GPP as a function of mean annual precipitation (MAP) and the climatological value of a
perturbed rainfall characteristic in the corresponding experiment. We term Figure 5 as
“GPP sensitivity space”, and “positive GPP sensitivity” means that GPP changes at
the same direction with MAP or rainfall characteristics, and vice versa for “negative
GPP response”. These “GPP sensitivity spaces” are generated based on the aggregated
mean GPP in each bin of the rainfall properties. The bin size for MAP, rainfall
frequency, rainfall intensity and rainy season length are 100 mm/year, 0.05 event/day,
1 mm/event and 15 days respectively. We also provide the standard error (SE) of the
“GPP sensitivity spaces” in each bin to assess their uncertainties, with higher SE
meaning larger uncertainties. The standard error (SE) between simulations to indicate the uncertainty of the result, as $SE = \frac{\sigma}{\sqrt{n}}$, where $\sigma$ and n refer to the standard deviation of GPP values and the sample size in each bin respectively. Thus changes in GPP and their associated standard errors are calculated for each climatological bin; where the bin size for MAP, rainfall frequency, rainfall intensity and rainy season length are 100 mm/year, 0.05 event/day, 1 mm and 15 days respectively. We recognize that there are large heterogeneity in soil texture, altitude and other factors which can influence simulation results at local scale, and using the current approach essentially lumps these factors and highlights the impacts from our interested variables (i.e. rainfall characteristics). A series of illustrations in Figure 4 were generalized from the simulated time series, and will be used to explain the underlying mechanisms.

3.1 Ecosystem sensitivity to rainfall frequency and intensity (Experiment $S_{\lambda \alpha}$)

Experiment $S_{\lambda \alpha}$ assesses ecosystem responses after increasing rainfall frequency $\lambda$ and decreasing rainfall intensity $\alpha$ ($\lambda \uparrow, \alpha \downarrow$) under a fixed total annual rainfall. The experiment $S_{\lambda \alpha}$ shows that the simulated biome distributions, after increasing rainfall frequency $\lambda$ and decreasing its intensity $\alpha$ ($\lambda \uparrow, \alpha \downarrow$) under a fixed total annual rainfall, have small differences in the low rainfall regime (around 500 mm/year, Figure 4a), with show that a small portion of regions are converted from woodland to grassland at low rainfall regime (~500 mm/year), corresponding to a decrease of GPP

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in these regions indicating a negative impact of increasing rainfall frequency when total rainfall is very low. In the high rainfall regime (around 1500 mm/year, Figure 3a), increasing rainfall frequency significantly converts tropical evergreen forests into woodlands. In the intermediate rainfall regime (600-1000 mm/year), there are little changes in biome distributions. We further check the spatial patterns of differences in annual mean soil moisture and annual total GPP (Figure 4 and 5b). We find that GPP increases with increasing rainfall frequency across most of the Africa continent, except in the very dry end (in the southern and eastern Africa) as well as the very wet regions (in central Africa and northeastern Madagascar). This GPP pattern mostly mirrors the soil moisture change in woodlands and grasslands (Figure 5a), except the wet tropics, where the changes of soil moisture and GPP are in the reversed signs.

Figure 6a shows the GPP sensitivity as a function of MAP and the climatological rainfall frequency, and we find three major patterns stand out.

**Pattern 1.1**: Negative GPP sensitivity shows up in the very dry end of MAP regime (MAP<400 mm/year) and with very low rainfall frequency (<0.3 day^-1 event/day), i.e. GPP decreases with more frequent but less intense rainfall in this low rainfall regime, without changes in the total rainfall amount.

**Pattern 1.2**: Across most rainfall regimes (MAP from 400 mm/year to 1600 mm/year), increasing frequency of rainfall (and simultaneously decreasing rainfall intensity) lead to positive GPP sensitivity. This positive GPP sensitivity peaks at the low range of rainfall frequency (~0.35 day^-1 event/day) and around the MAP of 1000 mm/year.

**Pattern 1.3**: At the high range of MAP (>1800 mm/year) with low rainfall frequency (~0.4 day^-1 event/day), GPP decreases with increased rainfall frequency.

The relationship of GPP sensitivity to MAP and rainfall intensity (Fig. 6c) has no clear patterns as previous ones, mostly because the GPP sensitivity space (Fig. A4c) contains large uncertainties (Fig. A4d, shown as large variance in the data). Thus we will not over-interpret the pattern in Fig. 6c: The GPP sensitivity with respect to MAP and rainfall intensity (Figure 6c) contains more uncertainties and shows more
complex patterns, mostly because the space that most pixels cluster (Figure S4c) also has large variance (Figure S4d). Thus we will not over interpret the pattern in Figure 6c.

Illustrative time series in Figure 7a and 7b explain the above Pattern 1.1 and Pattern 1.2 can be explained by the illustrative time series in Figure 6a and 6b, respectively. Figure 3a and 3b shows that when rainfall events are small and very infrequent, increasing rainfall frequency while decreasing intensity would cause more frequent downcrossings of soil moisture at the wilting point $S_w$, which subsequently would reduce the effective time of carbon assimilation and plant growth (i.e. when soil moisture is below $S_w$, plants would be in the extreme water stress and slow down or stop physiological activity). It is worth noting that in this case only happens where MAP is very low with low frequency and the biome is predominantly grasslands—which explains why negative changes in soil moisture and GPP in Figure 4a and 4b are distributed in those regions. The spatial patterns of negative soil moisture and GPP sensitivity in Figure 5a and 5b. This result also corroborates the field findings of the negative impacts from increasing rainfall frequency in Heisler-White et al.(2009) and Thomey et al. (2011) at low rainfall regimes.

Figure 2a and 2b explains provides the hydrological mechanism for the positive sensitivity of soil moisture and GPP with increasing rainfall frequency over the most African continent (Pattern 1.2). Once individual rainfall event has enough intensity and rainfall events are frequent enough, downcrossings of $S_w$ would not easily happen. Instead, the accumulative rainy-season soil moisture becomes the dominant control of plant growth, and water stress (shaded areas between $S_w$ and $S^*$, Porporato et al., 2001) becomes the dominant source of growth stress for plants; and increasing rainfall frequency has can lead to a significant decrease in this type of plant water stress increase of soil moisture for plant water use (Figure 4a and 4b). This conclusion drawn from our numerical modeling is consistent with previous findings in Rodríguez-Iturbe and Porporato (2004) based on stochastic modeling. We also find that this positive impact GPP sensitivity reaches to its maximum in the intermediate total rainfall (~1000 mm/year) and relatively low rainfall frequency (~0.35
day$^{-1}$event/day), indicating that in these regimes increasing rainfall frequency could most effectively decrease plant water stress, soil moisture for plant water use, and create marginal benefits of GPP to the increased rainfall frequency. Further increase in rainfall frequency may also increase plant water use and create marginal benefits of GPP to the increased rainfall frequency.

Pattern 1.3 also shows a negative GPP sensitivity, but its mechanism is different from the previous case of Pattern 1.1. There is another negative GPP sensitivity shown in Pattern 1.3, but the mechanism is different from the previous negative GPP sensitivity. In regions with total rainfall usually more than 1800 mm/year, SEIB-simulated tropical forests exhibit radiation-limitation rather than water-limitation during wet season. Increase of rainfall frequency at daily scale would enhance cloud fraction and suppress plant productivity in these regions (Graham et al., 2003). Thus even though soil moisture still increases (Figure 5), GPP decreases with increased rainfall frequency. This mechanism also explains why tropical evergreen forests shrink its area with increased rainfall frequency (Figure 4).

It is worth noting that the magnitude of GPP changes due to rainfall frequency and intensity is relatively small in most of the woodlands, but can be relatively large for drylands with MAP below 600 mm/year (up to 10-20% of annual GPP). This pattern also explains why only modest changes in biome distribution happen for the transitional area between woodlands and grasslands in $S_{TS}$ (Figure 4).

3.2 Ecosystem sensitivity to rainfall seasonality and frequency (Experiment $S_{TS}\lambda$)

The experiment $S_{TS}\lambda$ assesses ecosystem responses after increasing rainy season length and decreasing rainfall frequency (i.e. $T_w$, $\lambda$) under a fixed total annual rainfall. $T$ shows that the simulated biome distribution, after increasing rainy season length and decreasing rainfall frequency...
length and decreasing rainfall frequency (i.e. $T_w$, $\lambda$) under a fixed total annual rainfall, shows a gain of area in tropical evergreen forests, which are converted from woodlands. The northern Africa has an area increase of woodlands converted from grasslands in the northern Africa, and African Horn region has a small expansion of grasslands into woodlands in the African Horn region (Figure 4, Figure 3b). Figure 5c and 4d show that increasing rainy season length $T_w$ and decreasing frequency $\lambda$ would significantly increase annual mean soil moisture and GPP (up to 30%) in most woodland areas, Meanwhile decreased soil moisture and GPP are found in the southern and eastern Africa, Tropical evergreen forests show regions have little response. We further explore the GPP sensitivity space in Figure 6 Figure 5e and 5g, and find the following interesting robust patterns (based on small standard errors shown in Figure 5f and 5h):

Pattern 2.1: The negative GPP sensitivity tends to happen where MAP is mostly below 1000 mm/year with long rainy season length ($T_w$ > 150 days) and low rainfall frequency ($\lambda$ < 0.35\ day^{-1}\ event/day), which is a unique rainfall regime that sporadically spread rain events for a long rainy season.

Pattern 2.2: When MAP and rainfall frequency are both larger than certain ranges (MAP > 1000 mm/year and $\lambda$ > 0.4\ day^{-1}\ event/day), decreasing $\lambda$ while increasing $T_w$ would significantly increase GPP. The maximum positive GPP sensitivity happens in the rainfall regime with the intermediate MAP range (1100-1500 mm/year) and the high rainfall frequency ($\lambda$ < 0.7\ day^{-1}\ event/day).

Pattern 2.3: There exists an “optimal rainy season length” for relative changes in ecosystem productivity at across large different MAP ranges (the white area between the red and blue space in Figure 6 Figure 5e). For the same MAP, any deviation of $T_w$ from the “optimal rainy season length” would reduce GPP; longer than this length, rainy season lengthening would decrease GPP; while shorter than this length, rainy season lengthening would increase GPP. This “optimal rainy season length” follows an increasing trend with MAP until 1400 mm/year.
Figure 7 explains the hydrological mechanism for the negative GPP sensitivity in Pattern 2.1. In the situation with low MAP and infrequent rainfall events, decreasing rainfall frequency and expanding rainy season length (i.e. $T_w$↑, $\lambda$↓) would lead to longer intervals between rainfall events and possibly longer excursions below $S_w$, which would restrain continuous plant growth and have detrimental effects on ecosystem productivity. It is worth noting that long rainy season in dryland (Figure 6) is usually accompanied with low rainfall frequency (Figure 5). The southern African dry grasslands (south of 15°S) typically fall in this category, and these regions thus have negative GPP sensitivity (Figure 5c and 5d), accompanied by a small biome conversion from woodlands to grasslands in the low range of MAP (~300 mm/year) as shown in Figure 3b.

Figure 6d explains the hydrological mechanisms for the positive GPP sensitivity in Pattern 2.2, which shows that when rainfall is ample enough to maintain little or no water stress during rainy season, increasing the interval of rainfall events may introduce little additional water stress but can significantly extend the growing season. This situation mostly happens in woodlands, where limited water stress exists during growing rainy season, and dry season length is the major constraint for plant growth. Thus the increase of rainy season length extends the temporal niche for plant growth, and significantly modifies the biome distribution, which leads to a significant woodland expansion large wood encroachment to grasslands and as well as a larger expansion of tropical evergreen forests conversion of woodlands to tropical evergreen forests, as shown into woodlands (Figure 4).

The little GPP sensitivity in tropical evergreen forest regions is mostly attributed to the long rainy season length already existing in this type of ecosystem. Thus further increasing $T_w$ may reach to its saturation (365 days) and has thus little impact to ecosystem productivity. This also explains why the magnitude of GPP sensitivity is much smaller at high MAP range than at the intermediate MAP range. Similar reason also explains why the GPP sensitivity has the maximum response in the intermediate
MAP range rather than the high MAP range, at which GPP sensitivity has been saturated.

The finding of “optimal rainy season length” across different rainfall regimes (Figure 6) is consistent with our previous empirical finding about the similar pattern of “optimal rainy season length” for tree fractional cover in Africa derived based on a satellite remote sensing product (Guan et al., 2014). The existence of “optimal rainy season length” Two distinctive GPP sensitivities separated by the “optimal rainy season length”, with this optimal length increasing with MAP, fully demonstrates the importance to explicitly consider the non-linear impacts of rainy season length on ecosystem productivity under climate change, which has been largely overlooked before.

3.3 Ecosystem sensitivity to rainfall seasonality and intensity ($S_{T_w-\alpha}$)

The results of the experiment $S_{T_w-\alpha}$ have many similarities with those of $S_{T_w-\lambda}$, including the similar changes in biome distributions (Figure 4), soil moisture and GPP patterns (Figure 5). We further find that the GPP sensitivity space with MAP and rainy season length for $S_{T_w-\alpha}$ (Figure 6) is also similar with that of for $S_{T_w-\lambda}$ (Figure 6). One new pattern finding is that rainfall intensity has little impact on the GPP sensitivity, as the contour lines in Figure 6 are mostly parallel with y-axis (i.e. rainfall intensity). In other words, the trade-off between $T_w$ and $\alpha$ is mostly a function of MAP and $T_w$, but not $\alpha$, and the largest marginal effects happen in the intermediate range of MAP, similar as in $S_{T_w-\lambda}$.

Figure 2, Figure 6e and 5f explain the governing hydrological mechanisms for the patterns of $S_{T_w-\alpha}$, which also have many similarities with $S_{T_w-\lambda}$. For the negative case (Figure 2, Figure 6e), decreasing rainfall intensity to extend and increasing rainy season length in the very low MAP regime may possibly lead to more downcrossings of $S_a$ and interrupt continuous plant growth. The positive case (Figure 2, Figure 6e) is similar as that in Figure 2, i.e. the repartitioning of excessive rainy season rainfall to the dry season for an extended growing period would significantly benefit plant growth and possible increase tree fraction cover.
4. Discussion

In this paper we provide a new modeling approach to systematically understand the ecological impacts from changes in intra-seasonal rainfall characteristics (i.e. rainfall frequency, rainfall intensity and rainy season length) across biomes and climate gradients in the African continent.

4.1 Limitation of the methodology

Though the modeling framework that we used is able to characterize the diverse ecosystem responses to the shifts in different rainfall characteristics, it nevertheless has its limitations. The current rainfall model only deals with the case of single rainy season per year, and approximates the case of double rainy seasons per year to be the single rainy season case. This assumption may induce unrealistic synthetic rainfall patterns in the equatorial dryland regions, in particular the Horn of Africa, thus the resulting simulated sensitivity of these regions may be less reliable. We also assume that rainfall frequency and intensity are homogenous throughout wet and dry seasons (or dry seasons), but in reality they still have seasonal variations. We only consider rainy season length for rainfall seasonality, and neglect the possible temporal phase change; actually in reality, rainfall seasonality change usually has length and phase shifts in concert. These rainfall-model-related limitations can be possibly overcame by simulating smaller intervals of rainfall processes (e.g. each month has their own $\alpha$ and $\lambda$) rather than simulating the whole wet or dry season using one fixed set of $\alpha$ and $\lambda$.

Besides, only using one ecosystem model also means that the simulated ecosystem sensitivity can be model-specific. Though magnitudes or thresholds for the corresponding patterns may vary depending on different models, we argue that, though we believe the qualitative results for the GPP sensitivity patterns (e.g. Figure 5 and Figure 6) should mostly hold as the necessary ecohydrological processes have been incorporated in the SEIB-DGVM, magnitudes or thresholds in these patterns may vary depending on different models. For example, GPP in tropical evergreen forests (Figure 5b and Figure 6a) is less sensitive to radiation limitation as
shown in satellite-based observation than in the SEIB simulation in Africa (Guan et al., 2013). We also recognize that to exclude fire impacts in the current simulation may bring some caveats limitation in interpreting the results for this study, as evidence shows that many savanna regions can be bistable due to fire effects (Staver et al. 2011; Hirotá et al 2011; Higgins and Scheiter 2012; also see for a possible rebuttal in Hanan et al, 2013), and Changes in rainfall regimes may not only have direct effects on vegetation productivity, but can also indirectly affect ecosystems through influencing its interactions with fire regimes, and rapid biome shifts may being a possible consequence. These feedbacks can be important in situations where the changes in the growing season length changes, which are related to fuel loads, fuel moisture dynamics and hence fire intensity (Lehmann et al., 2011). Quantifying these fire-rainfall feedbacks will be the important future direction to pursue.

4.2 Clarifying the impacts of rainfall frequency and intensity on ecosystem productivity

In this modeling study, we provide a plausible answer to possibly resolve the previous debate about whether increasing rainfall intensity (or equivalently decreasing rainfall frequency, i.e. $\lambda_{\downarrow}$, $\alpha_{\uparrow}$) has positive or negative impacts on above-ground primary productivity with a fixed annual rainfall total. We identify that negative GPP sensitivity with increased rainfall frequency is possible at very low MAP range (~400 mm/year) with very relatively low rainfall frequency (<0.35 day$^{-1}$ event/day) (Figure 6/Figure 5a), due to the increased downcrossings of soil moisture wilting point, which restricts plant growth (Figure 2/Figure 6a). Our This derived MAP threshold (~400 mm/year) to distinguish different GPP sensitivities with rainfall frequency is consistent with our meta-analysis based on the previous field studies (Table 1), which shows a threshold of MAP at 340 mm/year separates positive and negative impacts of more intense rainfall on ANPP (aboveground net primary production). Our findings are also consistent with another study about increased tree encroachments with increased rainfall intensity in very low rainfall regime (<544 mm/year, Kulmatiski and Beard, 2013), which essentially follows the
same mechanism as identified in Figure 7a. In addition, we thoroughly investigated the ecosystem responses across all the wide ranges of annual rainfall in Africa. We find that beyond the very low rainfall range (below 400 mm/year), most grasslands and woodlands would benefit from increasing rainfall frequency, which also corroborate the previous large-scale findings about the positive effects of increased rainfall frequency (and decreased rainfall intensity) for tree fractions across the African continent (Good and Caylor, 2011). The only exception happens at the very wet end of MAP (~1800 mm/year) where cloud-induced radiation-limitation may suppress ecosystem productivity with increased rainfall frequency. We also find that changes in rainfall frequency and intensity mostly affect grassland-dominated savannas (changes of GPP up to 20%), and the corresponding effects are much smaller in woodlands and have little impact on woodland distribution. Though this work is only based on a single model, it provides a primary assessment for understanding of interactive changes between $\lambda$ and $\alpha$ in ecosystem functioning, which and expands the analysis to the full spectra of wide range of annual rainfall ranges-conditions compared with previous studies (e.g. Porporato et al., 2004).

4.3 Ecological importance of rainy season length

The results involving rainy season length (i.e. $S_{T_w-\lambda}$ and $S_{T_w-\alpha}$) have fully demonstrated provide evidence for the ecological importance of rainfall seasonality. The magnitudes of changes in soil moisture, GPP and biome distribution in $S_{T_w-\lambda}$ and $S_{T_w-\alpha}$ are much larger than those of $S_{\lambda-\alpha}$, with almost one order of magnitude difference. These disproportional impacts of $T_w$ indicate that slight changes in rainy season length could modify biome distribution and ecosystem function more dramatically compared with the same percentage changes in rainfall frequency and intensity. We also notice that $S_{T_w-\lambda}$ and $S_{T_w-\alpha}$ have similar results, which is because that both $\lambda$ and $\alpha$ describe rainfall characteristics within wet season, while $T_w$ describes rainfall characteristics of both dry season and wet season. Cautions are required that our simplified treatment rainy season length may overestimate its importance, and we did
not consider the rainfall phase information here.   

Given the importance of rainy season length, its ecological impacts under climate change are largely understudied, though substantial shifts in rainfall seasonality have been projected in both Sahel and South Africa (Biasutti and Sobel, 2009; Shongwe et al., 2009; Seth et al., 2013). Here we only address the rainfall seasonality in terms of its length, and future changes in rainfall seasonality may modify their phase and magnitude in concert. The climate community has focused on the increase of extreme rainfall events (Field et al., 2012), which could be captured by the changes in $\lambda$ or $\alpha$ towards heavier tails in their distribution. However, explicit and systematic assessments and projection on rainfall seasonality changes (including both phase and magnitude) are still limited even in the latest Intergovernmental Panel on Climate Change (IPCC) synthesis reports (Field et al., 2012; Stocker et al., 2013). More detailed studies related to these changes and their ecological implications are required for future hydroclimate-ecosystem research.

4.4 Not all rainfall regimes are ecologically equivalent

As Figure 1 gives a convincing example that the same total annual rainfall may arrive in a very different way, our results further demonstrate that ecosystems respond differently to the changes in these intra-seasonal rainfall variability. For example, with similar MAP, drylands in West Africa and Southwest Africa can have reversed responses to the same changes in intra-seasonal rainfall variability. As shown in the experiments of $S_{Tw}$ and $S_{Ta-o}$. increasing $T_w$ while decreasing $\lambda$ or $\alpha$ generates slightly positive soil moisture and GPP sensitivity in West Africa (Figure 5 and 4d), but would cause relatively large GPP decrease in Southwest Africa. The prior hydroclimate conditions of these two regions can explain these differences: West Africa has much shorter rainy season with more intense rainfall events, which is totally contrary to in contrast, Southwest Africa, which has a long rainy season but many small and sporadic rainfall events. As a result, under a fixed annual rainfall total, slightly increasing rainy season and meanwhile decreasing rainfall intensity would benefit plant growth in West Africa, but the same change would lengthen dry spells in
Southwest Africa and bring negative effects to the ecosystem productivity. We further deduce that the rainfall use efficiency (RUE, defined as the ratio of plant net primary production to total rainfall amount) in these two drylands could be different: West Africa may have lower RUE, and the intense rainfall could lead to more infiltration-excess runoff, and thus less water would be used by plants; while Southwest Africa can have higher RUE, because its sporadic and feeble rainfall events would favor grass to fully take the advantage of the ephemerally existed water resources. This conclusion is partly supported by Martiny et al. (2007) based on satellite remote sensing. We further hypothesize that landscape geomorphology in these two drylands may be different and therefore reflect distinctive rainfall characteristics. More bare soil may exist in West Africa grasslands due to intense-rainfall-induced erosion, while Southwest Africa may have more grass fraction and less bare soil fraction. Testing these interesting hypotheses is beyond the scope of this paper, but is worthy the further exploration.

Acknowledgements:

K. Guan and E. F. Wood acknowledge the financial supports from the NASA NESSF fellowship. S.P. Good and K. K. Caylor acknowledge the financial supports from the National Science Foundation through the Grant EAR-0847368. The authors thank Ignacio Rodríguez-Iturbe for his valuable inputs and discussion.
References:


Porporato, A.; Laio, F.; Ridolfi, L. & Rodríguez-Iturbe, I. (2001), 'Plants in


Table 1. Summary of previous representative studies on assessing the impacts of rainfall characteristics (i.e. rainfall frequency, intensity and seasonality) on the structure and function of terrestrial ecosystem.

**Focus**: frequency (freq); intensity (int); seasonality (sea); variation (CV).

**Methods**: Field Experiments (Field); Remote Sensing (RS); Flux Tower (Flux).

**Major Conclusion**: increasing rainfall intensity (or decreasing frequency) has positive impacts (int+); increasing intensity (or decreasing frequency) has negative impacts (int-); increasing rainfall CV has positive impacts (CV+); increasing rainfall CV has negative impacts (CV-).

<table>
<thead>
<tr>
<th>Focus</th>
<th>Methods</th>
<th>Spatial Scale</th>
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<th>MAP (mm/year)</th>
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<tr>
<td>freq; int</td>
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<td>Africa continent</td>
<td>intra-annual climatology</td>
<td>[0,3000]</td>
<td>Africa all</td>
<td>(int-) woody cover</td>
<td>Good and Caylor, 2011</td>
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<td>freq; int</td>
<td>RS</td>
<td>US</td>
<td></td>
<td>[163,1227]</td>
<td>US</td>
<td>(int-) ANPP greatest in arid grassland (16%) and Mediterranean forest (20%) and less for mesic grassland and temperate forest (3%)</td>
<td>Zhang et al., 2013</td>
</tr>
<tr>
<td>freq; int</td>
<td>RS</td>
<td>Pan-tropics (35°N to 15°S)</td>
<td>inter-annual</td>
<td>[0,3000]</td>
<td>Tropical ecosystems</td>
<td>(CV+) wood cover in dry tropics; (CV-) wood cover in wet tropics</td>
<td>Holmgren et al., 2013</td>
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<tr>
<td>freq; int</td>
<td>RS</td>
<td>Northern China</td>
<td>intra-annual</td>
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<td>(int-) NDVI for temperate grassland and broadleaf forests, not for coniferous forest</td>
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<td>intra-annual</td>
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</tr>
<tr>
<td>seas</td>
<td>RS</td>
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<td>climatology</td>
<td>[0,3000]</td>
<td>Africa all</td>
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<td>615</td>
<td>grassland</td>
<td>(int-) ANPP</td>
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<td>Climate</td>
<td>ANPP Type</td>
<td>ANPP Value</td>
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<td>(int+) ANPP</td>
<td></td>
<td>Thorne et al., 2011</td>
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<td>grassland</td>
<td>(int-) soil CO2 flux</td>
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<td>Harper et al., 2005</td>
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<td>Field plot (Spain)</td>
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<td>grassland</td>
<td>Mediterranean dryland ecosystem has more resilience for intra- and inter-annual changes in rainfall</td>
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Figure 1. a-b: Spatial pattern of the rainfall characteristics in Africa: a-MAP; b-rainfall intensity; c-rainfall frequency; d-rainy season length. The black-line identified areas refer to two savanna regions in West and Southwest Africa. e-f: Normalized histograms of the rainfall characteristics in two savanna regions of West and Southwest Africa. e-MAP (bin width for the x-axis: 100 mm/year); f-rainfall intensity (bin width for the x-axis: 1 mm/event); g-rainfall frequency (bin width for the x-axis: 0.1 event/day); h-rainy season length (bin width for the x-axis: 20 days).
Figure 2. Conceptual diagram of the experiment designs for three experiments ($S_{\lambda-\alpha}$, $S_{Tw-\lambda}$, $S_{Tw-\alpha}$).
Figure 2. Schematic diagram of water stress factor ranging from 0 (most stressful) to 1 (no stress), which acts to reduce transpiration and carbon assimilation. The red dotted line is based on Porporato et al. (2001) with a reversed sign, and the SEIB model (SEIB-DGVM) has a nonlinear implementation (blue solid line, Sato and Ise, 2012).
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Figure 5 Figure 4. Simulated changes in annual mean soil moisture (0-500mm, first column) and annual mean GPP (second column) for different experiments. Please note that the scales of $S_{λ-α}$ is much smaller than those of $S_{Tw-λ}$ and $S_{Tw-α}$. The two areas with black boundaries in each panel are West African grassland and Southwest African grassland associated with Figure 1. The spatial patterns shown here are smoothed by 3*3 smoothing window from the raw data.
Figure 6: Differences in simulated annual GPP as a function of mean annual precipitation and one of the perturbed rainfall characteristics in all the three experiments (i.e. $S_{\lambda\alpha}$, $S_{T_w\lambda}$, $S_{T_w\alpha}$) in the left column. The right column shows the correspondent standard errors (SE, calculated as $SE = \sigma / \sqrt{n}$, where $\sigma$ refers to the standard deviation within each bin, $n$ is the sample size in each bin, and $n$ and $\sigma$ are shown in Figure S4), with larger values associated with more uncertainties and requires more caution in interpretation. The contours are based on the binned values, with for each 100 mm/year in MAP, each 0.05 day$^{-1}$ event/day in rainfall frequency, each 1 mm/event in rainfall intensity and each 15 day in rainy season length.
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<th>Negative Cases</th>
<th>Positive Cases</th>
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<td>After alteration</td>
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**Figure 7**. Illustrative time series for hydrological controls on plant root-zone soil moisture dynamics for all the experiments, and these illustrations are generalized based on the simulated time series from the experiments. Both negative and positive cases are shown, and cases with directly hydrological controls are shown (i.e. cloud-induced negative impacts in tropical forests are not shown). The cumulative shaded areas refer to “plant water stress” defined by Porporato et al. (2001).
Supplementary materials:

Figure S1. Comparison of biomes and annual GPP between S_{climatology} and S_{control} to test the validity of the synthetic weather generator. The biome definition follows Sato and Ise (2012).
Figure S2. Simulated biomes for different experiments.
Figure S3. Normalized histograms of three simulated dominating biomes in the three experiments.
Figure S4. The sample size ($n$) in each bin (left column) and standard deviation ($\sigma$) in each bin (right column), corresponding to Figure 6 and Figure 5. In Figure 6, right column, standard deviation (SE) is calculated as $SE = \frac{\sigma}{\sqrt{n}}$. 
Continental-scale impacts of intra-seasonal rainfall variability
on simulated ecosystem responses in Africa

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Running title: Ecological Impacts of Intra-Seasonal Rainfall Variability

Submitted to \textit{Biogeosciences}
Abstract:

Climate change is expected to change intra-seasonal rainfall variability, arising from shifts in rainfall frequency, intensity and seasonality. These intra-seasonal changes are likely to have important ecological impacts on terrestrial ecosystems. Yet, quantifying these impacts across biomes and large climate gradients is largely missing. This gap hinders our ability to better predict ecosystem services and their responses to climate change, esp. for arid and semi-arid ecosystems. Here we use a synthetic weather generator and an independently validated vegetation dynamic model (SEIB-DGVM) to virtually conduct a series of “rainfall manipulation experiments” to study how changes in the intra-seasonal rainfall variability affect continent-scale ecosystem responses across Africa. We generated different rainfall scenarios with fixed total annual rainfall but shifts in: i) frequency vs. intensity, ii) rainy season length vs. frequency, iii) intensity vs. rainy season length. These scenarios were fed into SEIB-DGVM to investigate changes in biome distributions and ecosystem productivity. We find a loss of ecosystem productivity with increased rainfall frequency and decreased intensity at very low rainfall regimes (<400 mm/year) and low frequency (<0.3 event/day); beyond these very dry regimes, most ecosystems benefit from increasing frequency and decreasing intensity, except in the wet tropics (>1800 mm/year) where radiation limitation prevents further productivity gains. This result reconciles seemingly contradictory findings in previous field studies on rainfall frequency/intensity impacts on ecosystem productivity. We also find that changes in rainy season length can yield more dramatic ecosystem responses compared with similar percentage changes in rainfall frequency or intensity, with the largest impacts in semi-arid woodlands. This study demonstrates that not all rainfall regimes are ecologically equivalent, and that intra-seasonal rainfall characteristics play a significant role in influencing ecosystem function and structure through controls on ecohydrological processes. Our results also suggest that shifts in rainfall seasonality have potentially large impacts on terrestrial ecosystems, and these understudied impacts should be explicitly examined in future studies of climate impacts.

Keywords: rainfall frequency, rainfall intensity, rainfall seasonality, biome
distribution, Gross Primary Production (GPP), Africa

1. Introduction

Due to increased water holding capacity in the atmosphere as a consequence of global warming (O’Gorman and Schneider, 2009), rainfall is projected to change in intensity and frequency across much of the world (Easterling et al., 2000; Trenberth et al., 2003; Chou et al., 2013), in conjunction with complex shifts in rainfall seasonality (Feng et al., 2013; Seth et al., 2013). These changes possibly indicate a large increase in the frequency of extreme events and variability in rainfall (Easterling et al., 2000; Allan and Soden, 2008), and many of these changes may be accompanied with little changes in total annual rainfall (Knapp et al., 2002; Franz et al., 2010). Meanwhile, regions sharing similar mean climate state may have very different intra-seasonal variabilities, and the ecological significance of intra-seasonal climate variabilities has been largely overlooked previously in terrestrial biogeography (Good and Caylor, 2011). For example, ecosystems in West Africa and Southwest Africa (Figure 1) share similar total annual rainfall, but West Africa has much more intense rainfall events within a much shorter rainy season, while Southwest Africa has a longer and less intense rainy season. The same amount of total rainfall can come in very different ways, which may cause distinctive ecosystem responses and structure. Understanding the impacts of these regional differences in intra-seasonal rainfall variability and their possible future changes on terrestrial ecosystems is critical for maintaining ecosystem services and planning adaptation and mitigation strategies for ecological and social benefits (Anderegg et al., 2013).

[insert Figure 1]

The changes in intra-seasonal rainfall characteristics, specifically frequency, intensity and seasonality, have critical significance to ecosystem productivity and structure (Porporato et al., 2001; Weltzin et al., 2003; Williams and Albertson, 2006; Good and Caylor, 2011; Guan et al., 2014), but previous studies on this topic
(summarized in Table 1) have their limitations in the following aspects. First, existing relevant field studies mostly focus on a single ecosystem, i.e. grasslands, and subsequently only low rainfall regimes have been examined to date (mostly below 800mm/year, see Table 1). Grasslands have the largest sensitivity to hydrological variabilities among all natural ecosystems (Scanlon et al., 2005; Guan et al., 2012), however inferences drawn from a single ecosystem are limited in scope and difficult to apply to other ecosystems. Second, even within grasslands, different studies have seemingly contradictory findings (see Table 1), and there is a lack of a comprehensive framework to resolve these inconsistencies. Specifically, whether increased rainfall intensity with decreased rainfall frequency has positive (Knapp et al., 2002; Fay et al., 2003; Robertson et al., 2009; Heisler-White et al., 2009) or negative impacts (Heisler-White et al., 2009; Thomey et al., 2011) on grassland productivity is still under debate. Third, previous relevant studies mostly focus on the impacts of rainfall frequency and intensity (Table 1 and Rodríguez-Iturbe and Porporato, 2004), and largely overlook the possible changes in rainfall seasonality. Rainfall frequency and intensity mostly describe rainfall characteristics within the rainy season, but do not account for the impacts of interplay between rainy season length and dry season length (Guan et al., 2014). For ecosystems predominately controlled by water availability, rainy season length constrains the temporal niche for active plant physiological activities (van Schaik et al., 1993; Scholes and Archer, 1997), and large variations in rainfall seasonality can lead to significant shifts in biome distribution found from paleoclimate pollen records (e.g. Vincens et al., 2007). Given changes in rainfall seasonality have been found in various tropical regions (Feng et al., 2013) and have been projected in future climate (Biasutti and Sobel, 2009; Shongwe et al., 2009; Seth et al., 2013), studies investigating their impacts on terrestrial ecosystems are relatively rare, and very few field studies are designed to address this aspect (Table 1, Bates et al., 2006; Svejcar et al., 2003; Chou et al., 2008). Finally, there is an increasing trend of large-scale studies addressing rainfall variability and ecological responses using satellite remote sensing (Fang et al., 2005; Zhang et al., 2005; Good and Caylor, 2011; Zhang et al., 2013; Holmgren et al., 2013) and flux network data
(Ross et al., 2012). These large-scale studies are able to expand analyses to more types of ecosystems and different climate conditions, and provide valuable observation-based insights. However there are very few theoretical modeling works to corroborate this effort. All these above issues call for a comprehensive modeling study to investigate different aspects of intra-seasonal rainfall variability on terrestrial ecosystems spanning large environmental gradients and various biomes.

In this paper, we aim to study ecological impacts of intra-seasonal rainfall variability on terrestrial ecosystems. In particular, we design virtual “rainfall manipulation experiments” to concurrently shift intra-seasonal rainfall characteristics without changing total annual rainfall. We focus on the impacts of these different rainfall scenarios on ecosystem productivity (e.g. Gross Primary Production, GPP) and biome distributions in the African continent, simulated by an independently validated dynamic vegetation model SEIB-DGVM (Sato and Ise, 2012). Previous modeling approaches in this topic (Gerten et al., 2008; Hély et al., 2006) designed various rainfall scenarios by rearranging (halving, doubling or shifting) the rainfall amount based on the existing rainfall observations. In contrast to these approaches, we design a weather generator based on a stochastic rainfall model (Rodríguez-Iturbe et al., 1999), which allows us to implement a series of experiments by synthetically varying two of the three rainfall characteristics (rainfall intensity, rainfall frequency, and rainy season length) while fixing total annual rainfall at the current climatology.

We choose Africa as our test-bed mostly because the following two reasons: (1) the rainfall regimes and biomes have large gradients varying from extremely dry grasslands to highly humid tropical evergreen forests; (2) Africa is a continent usually assumed to have few temperature constrains (Nemani et al., 2003), which will help to isolate the impacts of precipitation from temperature, as one challenge in attributing climatic controls on temperate ecosystems or Mediterranean ecosystems is the superimposed influences from both temperature and precipitation. The overarching science question we will address is: How do African ecosystems respond to possible changes in intra-seasonal rainfall variability (i.e. rainfall frequency, intensity and rainy season length)?
2. Materials and Methods

2.1 Methodology overview

Table 1 summarizes previous field-based rainfall manipulation experiments, such as the one that Knapp et al. (2002) did in a grassland that concurrently increasing rainfall frequency and decreasing rainfall intensity while fixing total rainfall. The central idea of our study is to design similar rainfall manipulation experiments but test them virtually in the model domain across large environment gradients. We manipulate rainfall changes through a weather generator based on a parsimonious stochastic rainfall model (Rodriguez-Iturbe et al., 1984). We model the total amount of rainfall during rainy season as a product of the three intra-seasonal rainfall characteristics for the rainy season, rainfall frequency ($\lambda$, event/day), rainfall intensity ($\alpha$, mm/event), and rainy season length ($T_w$, days) (More details in section 2.3). Thus it is possible to simultaneously perturb two of the rainfall characteristics away from their climatological values while preserving the mean annual precipitation (MAP) unchanged. We then feed these different rainfall scenarios into a well-validated dynamic vegetation model (SEIB-DGVM, section 2.2) to study simulated ecosystem responses. Detailed experiments design is described in section 2.5.

2.2 SEIB-DGVM model and its performances in Africa

We use a well-validated vegetation dynamic model SEIB-DGVM (Sato et al., 2007) as the tool to study ecosystem responses to different rainfall variabilities. This model follows the traditional “gap model” concept (Shugart, 1998) to explicitly simulate the dynamics of ecosystem structure and function for individual plants at a set of virtual vegetation patches, and uses results at these virtual patches as a surrogate to represent large-scale ecosystem states. Thus individual trees are simulated from establishment, competition with other plants, to death, which creates “gaps” for other plants to occupy and develop. SEIB-DGVM includes mechanical-based and empirical-based
algorithms for land physical processes, plant physiological processes, and plant dynamic processes. SEIB-DGVM contains algorithms that explicitly involve the mechanisms of plant-related water stress (Figure 2; Sato and Ise, 2012). With similar concepts to previous studies (e.g. Milly, 1992; Porporato et al., 2001), the current SEIB-DGVM implements a continuous “water stress factor” (Equation 2) based on the soil moisture status (Equation 1), scaling from 0 (most stressful) to 1 (with no stress), which then acts to scale the stomatal conductance for plant transpiration and carbon assimilation.

\[ stat_{\text{water}} = \frac{(S - S_w)}{(S_f - S_w)} \quad \text{(Equation 1)} \]

\[ \text{Water stress factor} = 2*stat_{\text{water}} - stat_{\text{water}}^2 \quad \text{(Equation 2)} \]

where S, S_w and S_f refer to the fraction of volumetric soil water content within the rooting depth, at the wilting point, and at field capacity, respectively. Figure 2 provides a schematic diagram of “water stress factor” from the SEIB-DGVM, and we also include an approximated linear model that has been widely adopted elsewhere (e.g. Milly, 1992; Porporato et al., 2001). The linear model uses an extra variable S*, so called “critical point” of soil moisture: when S>S*, there is no water stress (water stress factor =1); and when S<S*, water stress factor linearly decreases with the decrease of S. Though SEIB-DGVM adopts a quadratic form for “water stress factor”, it essentially functions similarly as the linear model, such that S* distinguishes two soil moisture regimes that below which there is a large sensitivity of water stress to soil moisture status, and above which there is little water stress. Understanding how this “water stress factor” functions is the key to explain the following results.

[insert Figure 2]

SEIB-DGVM allows development of annual and perennial grasses as well as multiple life cycles of grass at one year based on environmental conditions. Multiple life cycles of tree growth per year are possible in theory but rarely happen in simulations (Sato and Ise, 2012). Soil moisture status is the predominant factor to determine LAI of the vegetation layer, which influences maximum daily productivity and leaf phenology.
When LAI exceeds 0 for 7 continuous days, dormant phase of perennial vegetation layer changes into growth phase. While when LAI falls below 0 for 7 continuous days, growth phase switches to dormant phase (Sato et al., 2007). SEIB-DGVM also explicitly simulates light conditions and light competition among different PFTs in the landscape based on its simulated 3D canopy structure and radiative transfer scheme (Sato et al., 2007).

SEIB-DGVM has been tested both globally (Sato et al., 2007) and regionally for various ecosystems (Sato et al., 2010; Sato, 2009; Sato and Ise, 2012), whose simulated results compare favorably with ground observations and satellite remote sensing measures for ecosystem composition, structure and function. In particular, SEIB-DGVM has been successfully validated and demonstrated its ability in simulating ecosystem structure and function in the African continent (Sato and Ise, 2012). Two plant function types (PFTs) of tropical woody species are simulated by SEIB-DGVM in Africa: tropical evergreen trees and tropical deciduous trees. The distribution of these two woody types in the simulation is largely determined by hydro-climatic environments. Tropical evergreen trees only develop in regions where water resources are sufficient all year around, so they can maintain leaves for all seasons; otherwise, tropical deciduous trees could survive and dominate the landscape as they can shed leaves if there is no sufficient water supply in its root zone during the dry season (Sato and Ise, 2012). Trees and grasses coexist in a cell, with the floor of a virtual forest monopolized by one of the two grass PFTs, C$_3$ or C$_4$ grass. The dominating grass type is determined at the end of each year by air temperature, precipitation, and CO$_2$ partial pressure (Sato and Ise, 2012).

SEIB-DGVM was run at 1° spatial resolution and at the daily step. It was spun-up for 2000 years driven by the observed climate (1970-2000) repeatedly for the soil carbon pool to reach steady state, followed by 200 years simulation driven by the forcings based on the experiment design in Section 2.4. Because our purpose is to understand the direct impacts of intra-seasonal rainfall variability, we turned off the fire component of SEIB-DGVM to exclude fire-mediated feedbacks in the results. Though we are fully aware of the important role of fire in interacting with rainfall
seasonality and their influence on African ecosystems (Bond et al., 2005; Lehmann et al., 2011; Staver et al., 2012), studying these interactions is beyond the scope of this work. For the similar reason, we fixed the atmospheric CO$_2$ concentration at 380 ppmv to exclude possible impacts of CO$_2$ fertilization effects.

2.3 Synthetic weather generator

The synthetic weather generator used here has two major components: i) to stochastically generate daily rainfall based on a stochastic rainfall model, and ii) to conditionally sample all other environmental variables from historical records to preserve the covariance among climate forcing variables.

The stochastic rainfall model can be expressed as MAP=$\alpha \lambda T_w/f_w$, and we set $f_w$ to be 0.9, i.e. the period including 90% of total annual rainfall is defined as “rainy season” (exchangeable with “wet season” hereafter). In particular, we first use Markham (1970)’s approach to find the center of the rainy season, and then extend the same length to both sides of the center until the total rainfall amount in this temporal window (i.e. “rainy season”) is equal to 90% of the total annual rainfall. Rainy season and dry season have their own rainfall frequency and intensity. Two seasons are separately modeled based on the Market Poisson Process. Here we only focus on and manipulate rainy-season rainfall characteristics in our study, as rainy-season rainfall accounts for almost all the meaningful rainfall inputs for plant use. Thus in the following paper, whenever we mention $\alpha$ or $\lambda$, we refer to those during the rainy season.

In this rainfall model, any day can be either rainy or not, and a rainy day is counted as one rainy event; rainfall events occur as a Poisson Process, with the parameter $1/\lambda$ (unit: days/event) being the mean intervals between rainfall events, and rainfall intensity $\alpha$ for each rainfall event following an exponential distribution, with $\alpha$ being the mean rainfall intensity per event (Rodríguez-Iturbe et al., 1999). The wet season length is modeled as a beta distribution bounded from 0 to 1, scaled by 365 days. All the necessary parameters to fit for the stochastic rainfall model (including the mean and variance of rainfall frequency, intensity and length of wet and dry
seasons) were derived from the satellite-gauge-merged rainfall measurement from TRMM 3b42V7 (Huffman et al., 2007) for the period of 1998 to 2012, based on the above assumptions for the rainfall process. Specifically, we applied our definition of “rainy season” to each year of the TRMM rainfall data for per pixel, and calculated the mean and variance of the “rainy season length”, using which we fitted the beta distribution for $T_w$. For rainfall frequency and intensity, we lumped all the wet or dry season rainfall record together to derive their parameters. The two steps of the synthetic weather generator are described below:

**Step 1:** Model the daily rainfall following the Marked Poisson process described above. In particular, for a specific year, we first stochastically generate the wet season length by sampling from the beta distribution, and the dry season length is determined accordingly. Then we generate the daily rainfall for wet and dry season respectively.

**Step 2:** Based on the simulated daily rainfall time series in Step 1, we conditionally sample temperature, wind, and humidity from the Global Meteorological Forcing Dataset (GMFD, Sheffield et al., 2006), as well as cloud fraction and soil temperature from the Climate Forecast System Reanalysis (CFSR) from National Centers for Environmental Prediction (NCEP) (Saha et al., 2010). To sample for a specific day, all the historical record within a 21-day time window centered at that specific day makes up a sampling pool. From the sampling pool, we choose the day such that the historical rainfall amount of the chosen day is within (100-30)% to (100+30)% of the simulated daily rainfall amount. We then draw all the environmental variables (except rainfall) on that sampled day to the new climate forcing. If we can find a sample from the pool based on the above rule, this sampling is called “successful”. When there is more than one suitable sample, we randomly select one. When there is no suitable sample, we randomly select one day within the pool. The mean “successful” rate for all the experiments and ensembles across Africa is 83%.

To test the validity of the synthetic weather generator, we ran SEIB-DGVM using the historical climate record ($S_{climatology}$) and the synthetic forcing ($S_{control}$), with the latter generated using the weather generator based on the rainfall characteristics derived from the former. Figure S1 shows that the SEIB-DGVM simulations driven
by these two different forcings generate similar biome distributions with a Cohen’s Kappa coefficient of 0.78 (Cohen, 1960), and similar GPP patterns in Africa, with the linear fit of annual GPP as: $GPP(S_{\text{control}}) = 1.03 \times GPP(S_{\text{climatology}}) + 0.215$ ($R^2=0.89$, $P<0.0001$). Both biome and GPP patterns are consistent with observations (Sato and Ise, 2012). These results provide confidence in using the synthetic weather generator and SEIB-DGVM to conduct the further study.

2.4 Experiment design

Three experiments are designed as follows:

**Exp 1** (Perturbation of rainfall frequency and intensity, termed as $S_{\lambda-\alpha}$ hereafter) Simulations forced by the synthetic forcings with varying $\lambda$ and $\alpha$ simultaneously for wet season (20% increases of $\lambda$ and corresponding decreases of $\alpha$ to make MAP unchanged; 20% decreases of $\lambda$ and corresponding increases of $\alpha$ to make MAP unchanged; no change for dry season rainfall characteristics), while fixing $T_w$ at the current climatology;

**Exp 2** (Perturbation of rainfall frequency and rainy season length, termed as $S_{T_w-\lambda}$) Simulations forced by the synthetic forcing with varying $T_w$ and $\lambda$ simultaneously for wet season (20% increases of $T_w$ and corresponding decreases of $\lambda$ to make MAP unchanged; 20% decreases of $T_w$ and corresponding increases of $\lambda$ to make MAP unchanged; no change for dry season characteristics), while fixing $\alpha$ at the current climatology;

**Exp 3** (Perturbation of rainy season length and intensity, termed as $S_{T_w-\alpha}$) Simulations forced by the synthetic forcing with varying $T_w$ and $\alpha$ simultaneously for wet season (20% increases of $T_w$ and corresponding decreases of $\alpha$ to make MAP unchanged; 20% decreases of $T_w$ and corresponding increases of $\alpha$ to make MAP unchanged; no change for dry season characteristics), while fixing $\lambda$ at the current climatology.

Because $\lambda$ and $T_w$ have bounded ranges ($\lambda \sim [0, 1]$ and $T_w \sim [0, 365]$), if these two variables after perturbation exceeds the range, we would force their value to be the lower or upper bound, and rearrange the other corresponding rainfall characteristic to ensure MAP unchanged. Each rainfall scenario has six ensemble realizations of
3. Results

We present the differences in simulated biome distributions of the three experiments (i.e. $S_{\lambda-\alpha}$, $S_{Tw-\lambda}$, $S_{Tw-\alpha}$) in Figure 3, and their spatial patterns are shown in Figure S2 and S3. Differences in simulated annually averaged soil moisture and GPP for each experiment are shown in Figure 4 and 6. These differences represent the simulated ecosystem sensitivity to the slight perturbation of intra-seasonal rainfall characteristics deviating from the current climatology. To further explore how MAP and these rainfall characteristics affect the simulated GPP, Figure 5 shows the difference of simulated GPP as a function of MAP and a perturbed rainfall characteristic in the corresponding experiment. We term Figure 5 as “GPP sensitivity space”, and “positive GPP sensitivity” means that GPP changes at the same direction with MAP or rainfall characteristics, and vise versa for “negative GPP response”. These “GPP sensitivity spaces” are generated based on the aggregated mean GPP in each bin of the rainfall properties. The bin size for MAP, rainfall frequency, rainfall intensity and rainy season length are 100 mm/year, 0.05 event/day, 1 mm/event and 15 days respectively.

We also provide the standard error (SE) of the “GPP sensitivity spaces” in each bin to assess their uncertainties, with higher SE meaning larger uncertainties. $SE = \sigma / \sqrt{n}$, where $\sigma$ and n refer to the standard deviation of GPP values and the sample size in each bin respectively. A series of illustrations in Figure 6 were generalized from the simulated time series, and are used to explain the underlying mechanisms.

3.1 Ecosystem sensitivity to rainfall frequency and intensity (Experiment $S_{\lambda-\alpha}$)

Experiment $S_{\lambda-\alpha}$ assesses ecosystem responses after increasing rainfall frequency $\lambda$ and decreasing rainfall intensity $\alpha$ ($\lambda$↑, $\alpha$↓) under a fixed total annual rainfall. The

[insert Figure 3; Figure 4; Figure 5]
simulated biome distributions show that a small portion of regions are converted from woodland to grassland at low rainfall regime (~500 mm/year), corresponding to a decrease of GPP in these regions. In the high rainfall regime (around 1500 mm/year, Figure 3a), increasing rainfall frequency significantly converts tropical evergreen forests into woodlands. In the intermediate rainfall regime (600-1000 mm/year), there is little change in biome distributions. We further check the spatial patterns of differences in annual mean soil moisture and annual total GPP (Figure 4a and 5b). We find that GPP increases with increasing rainfall frequency across most of the Africa continent, except in the very dry end (in the southern and eastern Africa) and the very wet regions (in central Africa and northeastern Madagascar). This GPP pattern mostly mirrors the soil moisture change in woodlands and grasslands (Figure 4b), except the wet tropics, where the changes of soil moisture and GPP are reversed.

Figure 5a shows the GPP sensitivity as a function of MAP and the climatological rainfall frequency, and we find three major patterns:

**Pattern 1.1:** Negative GPP sensitivity shows up in the very dry end of MAP regime (MAP<400 mm/year) and with relatively low rainfall frequency ($\lambda$<0.3 event/day), i.e. GPP decreases with more frequent but less intense rainfall in this low rainfall range.

**Pattern 1.2:** Across most rainfall ranges (MAP from 400 mm/year to 1600 mm/year), increasing frequency of rainfall (and simultaneously decreasing rainfall intensity) lead to positive GPP sensitivity. This positive GPP sensitivity peaks at the low range of rainfall frequency (~0.35 event/day) and around the MAP of 1000 mm/year.

**Pattern 1.3:** At the high range of MAP (>1800 mm/year) with low rainfall frequency (~0.4 event/day), GPP decreases with increased rainfall frequency.

The relationship of GPP sensitivity to MAP and rainfall intensity (Fig. 6c) has no clear patterns as previous ones, mostly because the GPP sensitivity space (Fig. A4c) contains large uncertainties (Fig. A4d, shown as large variance in the data). Thus we will not over-interpret the pattern in Fig. 6c.

Pattern 1.1 and Pattern 1.2 can be explained by the illustrative time series in Figure 6a and 6b, respectively. Figure 6a shows that when rainfall events are small and very infrequent, increasing rainfall frequency while decreasing intensity would
cause more frequent downcrossings of soil moisture at the wilting point $S_w$, which subsequently would reduce the effective time of carbon assimilation and plant growth (i.e. when soil moisture is below $S_w$, plants would be in the extreme water stress and slow down or stop physiological activity). This case only happens where MAP is very low with low frequency and the biome is predominantly grasslands, which explains why negative changes in soil moisture and GPP in Figure 4a and 4b are distributed in those regions. This result also corroborates the field findings of the negative impacts from increasing rainfall frequency in Heisler-White et al.(2009) and Thomey et al. (2011) at low rainfall regimes.

Figure 6b provides the hydrological mechanism for the positive sensitivity of soil moisture and GPP with increasing rainfall frequency over the most African continent (Pattern 1.2). Once individual rainfall event has enough intensity and rainfall frequency is enough, downcrossings of $S_w$ would not easily happen. Instead, the accumulative rainy-season soil moisture becomes the dominant control of plant growth, and increasing rainfall frequency has led to a significant increase of soil moisture for plant water use (Figure 4a and 4b). This conclusion drawn from our numerical modeling is consistent with previous findings in Rodríguez-Iturbe and Porporato (2004) based on stochastic modeling. We also find that this positive GPP sensitivity reaches to its maximum in the intermediate total rainfall (~1000 mm/year) and relatively low rainfall frequency (~0.35 event/day), indicating that in these regimes increasing rainfall frequency could most effectively increase soil moisture for plant water use and create marginal benefits of GPP to the increased rainfall frequency. Further increase in large total annual rainfall or rainfall frequency would reduce the sensitivity to water stress with fewer downcrossings of soil moisture critical point $S^*$; and once the soil moisture is always ample (i.e. above $S^*$), the changes in either MAP or rainfall frequency would not alter plant water stress.

Pattern 1.3 also shows a negative GPP sensitivity, but its mechanism is different from the previous case of Pattern 1.1. In regions with total rainfall usually more than 1800 mm/year, SEIB-simulated tropical forests exhibit radiation-limitation rather than water-limitation during wet season. Increase of rainfall frequency at daily scale would
enhance cloud fraction and suppress plant productivity in these regions (Graham et al., 2003). Thus even though soil moisture still increases (Figure 4a), GPP decreases with increased rainfall frequency. This mechanism also explains why tropical evergreen forests shrink its area with increased rainfall frequency (Figure 3a).

It is worth noting that the magnitude of GPP changes due to rainfall frequency and intensity is relatively small in most of the woodlands, but can be relatively large for drylands with MAP below 600 mm/year (up to 10-20% of annual GPP). This pattern also explains why only modest changes in biome distribution happen between woodlands and grasslands in S_{λ-α} (Figure 3a).

[insert Figure 6]

### 3.2 Ecosystem sensitivity to rainfall seasonality and frequency (Experiment S_{Tw-λ})

Experiment S_{Tw-λ} assesses ecosystem responses after increasing rainy season length and decreasing rainfall frequency (i.e. T_w↑, λ↓) under a fixed total annual rainfall. The simulated biome distribution shows a gain of area in tropical evergreen forests converted from woodlands. The northern Africa has an area increase of woodlands converted from grasslands, and African Horn region has a small expansion of grasslands into woodlands (Figure 3b). Figure 4c and 4d show that increasing rainy season length T_w and decreasing frequency λ would significantly increase annual mean soil moisture and GPP (up to 30%) in most woodland area. Meanwhile decreased soil moisture and GPP are found in the southern and eastern Africa. Tropical evergreen forests show little response. We further explore the GPP sensitivity space in Figure 5e and 5g, and find the following robust patterns (based on small standard errors shown in Figure 5f and 5h):

**Pattern 2.1**: The negative GPP sensitivity tends to happen where MAP is mostly below 1000 mm/year with long rainy season length (T_w>150 days) and low rainfall frequency (λ<0.35 event/day).

**Pattern 2.2**: When MAP and rainfall frequency are large enough (MAP>1000 mm/year and λ>0.4 event/day), decreasing λ while increasing T_w would significantly
increase GPP. The maximum positive GPP sensitivity happens at the intermediate MAP range (1100-1500 mm/year) and the high rainfall frequency ($\lambda \sim 0.7$ event/day).

**Pattern 2.3:** There exists an “optimal rainy season length” for relative changes in ecosystem productivity across large MAP ranges (the white area between the red and blue space in Figure 5e). For the same MAP, any deviation of $T_w$ from the “optimal rainy season length” would reduce GPP. This “optimal rainy season length” follows an increasing trend with MAP until 1400 mm/year.

Figure 6c explains the hydrological mechanism for the negative GPP sensitivity in Pattern 2.1. In the situation with low MAP and infrequent rainfall events, decreasing rainfall frequency and expanding rainy season length (i.e. $T_w \uparrow$, $\lambda \downarrow$) would lead to longer intervals between rainfall events and possibly longer excursions below $S_w$, which would disrupt continuous plant growth and have detrimental effects on ecosystem productivity. It is worth noting that long rainy season in dryland (Figure 5e) is usually accompanied with low rainfall frequency (Figure 5g). The southern African drylands (south of 15°S) typically fall in this category, and these regions thus have negative GPP sensitivity (Figure 4c and 4d), accompanied by a small biome conversion from woodlands to grasslands (Figure 3b).

Figure 6d explains the hydrological mechanisms for the positive GPP sensitivity in Pattern 2.2. When rainfall is ample enough to maintain little or no water stress during rainy season, increasing the interval of rainfall events may introduce little additional water stress but can significantly extend the growing season. This situation mostly happens in woodlands, where limited water stress exists during rainy season, and dry season length is the major constraint for plant growth. Thus the increase of rainy season length extends the temporal niche for plant growth, and leads to a significant woodland expansion to grasslands as well as an expansion of tropical evergreen forests to woodlands (Figure 3b).

The little GPP sensitivity in tropical evergreen forest regions is mostly attributed to the long rainy season length in this ecosystem. Thus further increasing $T_w$ may reach to its saturation (365 days) and has little impact to ecosystem productivity. This also explains why the magnitude of GPP sensitivity is much smaller at high MAP.
The finding of “optimal rainy season length” across different rainfall regimes (Figure 5e) is consistent with our previous empirical finding about the similar pattern of “optimal rainy season length” for tree fractional cover in Africa derived based on a satellite remote sensing product (Guan et al., 2014). The existence of “optimal rainy season length” fully demonstrates the importance to explicitly consider the non-linear impacts of rainy season length on ecosystem productivity under climate change, which has been largely overlooked before.

3.3 Ecosystem sensitivity to rainfall seasonality and intensity ($S_{Tw-\alpha}$)

Results of Experiment $S_{Tw-\alpha}$ have many similarities with those of $S_{Tw-\lambda}$, including the similar changes in biome distributions (Figure 3), soil moisture and GPP patterns (Figure 4e and 4f). We further find that the GPP sensitivity space with MAP and rainy season length for $S_{Tw-\alpha}$ (Figure 5i) is also similar with that for $S_{Tw-\lambda}$ (Figure 5e). One new finding is that rainfall intensity has little impact on GPP, as the contour lines in Figure 5k are mostly parallel with y-axis (i.e. rainfall intensity).

Figure 6e and 6f explain the governing hydrological mechanisms for the patterns of $S_{Tw-\alpha}$, which also have many similarities with $S_{Tw-\lambda}$. For the negative case (Figure 6e), decreasing rainfall intensity and increasing rainy season length in the very low MAP regime may lead to more downcrossings of $S_w$ and interrupt continuous plant growth. The positive case (Figure 6e) is similar as that in Figure 6d, i.e. the repartitioning of excessive wet-season rainfall to the dry season for an extended growing period would significantly benefit plant growth and possible increase tree fraction cover.

4. Discussion

In this paper we provide a new modeling approach to systematically interpret the ecological impacts from changes in intra-seasonal rainfall characteristics (i.e. rainfall frequency, rainfall intensity and rainy season length) across biomes and climate gradients in the African continent.
4.1 Limitation of the methodology

Though our modeling framework is able to characterize the diverse ecosystem responses to the shifts in different rainfall characteristics, it nevertheless has its limitations. The current rainfall model only deals with the case of single rainy season per year, and approximates the case of double rainy seasons per year to be the single rainy season case. This assumption may induce unrealistic synthetic rainfall patterns in the equatorial dryland regions, in particular the Horn of Africa. Thus the simulated sensitivity of these regions may be less reliable. We also assume that rainfall frequency and intensity are homogenous throughout wet seasons (or dry seasons), but in reality they have seasonal variations. We only consider rainy season length for rainfall seasonality, and neglect the possible temporal phase change; in reality, rainfall seasonality change usually has length and phase shifts in concert. These rainfall-model-related limitations can be possibly overcome by simulating smaller intervals of rainfall processes (e.g. each month has their own \( \alpha \) and \( \lambda \)) rather than simulating the whole wet or dry season using one fixed set of \( \alpha \) and \( \lambda \). Besides, only using one ecosystem model also means that the simulated ecosystem sensitivity can be model-specific. Though magnitudes or thresholds for the corresponding patterns may vary depending on different models, we argue that the qualitative results for the GPP sensitivity patterns (e.g. Figure 4 and Figure 5) should hold as the necessary ecohydrological processes have been incorporated in SEIB-DGVM. We also recognize that to exclude fire impacts in the current simulation may bring some limitation for this study, as evidence shows that many savanna regions can be bistable due to fire effects (Staver et al 2011; Hirota et al 2011; Higgins and Scheiter 2012; also see for a possible rebuttal in Hanan et al, 2013). Changes in rainfall regimes not only have direct effects on vegetation productivity, but can also indirectly affect ecosystems through its interactions with fire, with rapid biome shifts being a possible consequence. These feedbacks can be important in situations when the changes in growing season length are related to fuel loads, fuel moisture dynamics and hence fire intensity (Lehmann et al., 2011). Quantifying these fire-rainfall feedbacks will be the
important future direction to pursue.

4.2 Clarifying the impacts of rainfall frequency and intensity on ecosystem productivity

In this modeling study, we provide a plausible answer to possibly resolve the previous debate about whether increasing rainfall intensity (or equivalently decreasing rainfall frequency, i.e. $\lambda \downarrow$, $\alpha \uparrow$) has positive or negative impacts on above-ground primary productivity under a fixed annual rainfall total. We identify that negative GPP sensitivity with increased rainfall frequency is possible at very low MAP range (~400 mm/year) with relatively low rainfall frequency (<0.35 event/day) (Figure 5a), due to the increased downcrossings of soil moisture wilting point, which restricts plant growth (Figure 6a). This derived MAP threshold (~400 mm/year) is consistent with our meta-analysis based on the previous field studies (Table 1), which shows a threshold of MAP at 340 mm/year separates positive and negative impacts of more intense rainfall on aboveground net primary production (ANPP). Our findings are also consistent with another study about increased tree encroachments with increased rainfall intensity in low rainfall regime (<544mm/year, Kulmatiski and Beard, 2013), which essentially follows the same mechanism as identified in Figure 6a.

In addition, we thoroughly investigated the ecosystem responses across a wide range of annual rainfall in Africa. We find that beyond the very low rainfall range (below 400 mm/year), most grasslands and woodlands would benefit from increasing rainfall frequency, which also corroborate the previous large-scale findings about the positive effects of increased rainfall frequency (and decreased rainfall intensity) for tree fractions across the African continent (Good and Caylor, 2011). The only exception happens at the very wet end of MAP (~1800mm/year) where cloud-induced radiation-limitation may suppress ecosystem productivity with increased rainfall frequency. We also find that changes in rainfall frequency and intensity mostly affect grassland-dominated savannas (changes of GPP up to 20%), and the corresponding effects are much smaller in woodlands and have little impact on woodland distribution. Though this work is only based on a single model, it provides a primary assessment
for understanding of interactive changes between $\lambda$ and $\alpha$ in ecosystem functioning, and expands the analysis to a wide range of annual rainfall conditions compared with previous studies (e.g. Porporato et al., 2004).

4.3 Ecological importance of rainy season length

The results involving rainy season length (i.e. $S_{Tw-\lambda}$ and $S_{Tw-\alpha}$) provide evidence for the ecological importance of rainfall seasonality. The magnitudes of changes in soil moisture, GPP and biome distribution in $S_{Tw-\lambda}$ and $S_{Tw-\alpha}$ are much larger than those of $S_{\lambda-\alpha}$, with almost one order of magnitude difference. These disproportional impacts of $T_w$ indicate that slight changes in rainy season length could modify biome distribution and ecosystem function more dramatically compared with the same percentage changes in rainfall frequency and intensity. We also notice that $S_{Tw-\lambda}$ and $S_{Tw-\alpha}$ have similar results. This is because that both $\lambda$ and $\alpha$ describe rainfall characteristics within wet season, while $T_w$ describes rainfall characteristics of both dry season and wet season. Cautions are required that our simplified treatment rainy season length may overestimate its importance, and we did not consider the rainfall phase information here.

Given the importance of rainy season length, its ecological impacts under climate change are largely understudied, though substantial shifts in rainfall seasonality have been projected in both Sahel and South Africa (Biasutti and Sobel, 2009; Shongwe et al., 2009; Seth et al., 2013). Here we only address the rainfall seasonality in terms of its length, and future changes in rainfall seasonality may modify their phase and magnitude in concert. The climate community has focused on the increase of extreme rainfall events (Field et al., 2012), which could be captured by the changes in $\lambda$ or $\alpha$ towards heavier tails in their distribution. However, explicit and systematic assessments and projection on rainfall seasonality changes (including both phase and magnitude) are still limited even in the latest Intergovernmental Panel on Climate Change (IPCC) synthesis reports (Field et al., 2012; Stocker et al., 2013). More detailed studies related to these changes and their ecological implications are required for future hydroclimate-ecosystem research.
4.4 Not all rainfall regimes are ecologically equivalent

As Figure 1 gives a convincing example that the same total annual rainfall may arrive in a very different way, our results further demonstrate that ecosystems respond differently to the changes in these intra-seasonal rainfall variability. For example, with similar MAP, drylands in West Africa and Southwest Africa show reversed responses to the same changes in intra-seasonal rainfall variability. As shown in the experiments of $S_{Tw-\lambda}$ and $S_{Tw-\alpha}$, increasing $T_w$ while decreasing $\lambda$ or $\alpha$ generates slightly positive soil moisture and GPP sensitivity in West Africa (Figure 4c and 4d), but would cause relatively large GPP decrease in Southwest Africa. The prior hydroclimate conditions of these two regions can explain these differences: West Africa has much shorter rainy season with more intense rainfall events; in contrast, Southwest Africa has a long rainy season but many small and sporadic rainfall events. As a result, under a fixed annual rainfall total, slightly increasing rainy season and meanwhile decreasing rainfall intensity would benefit plant growth in West Africa, but the same change would lengthen dry spells in Southwest Africa and bring negative effects to the ecosystem productivity. We further deduce that the rainfall use efficiency (RUE, defined as the ratio of plant net primary production to total rainfall amount) in these two drylands could be different: West Africa may have lower RUE, and the intense rainfall could lead to more infiltration-excess runoff, and thus less water would be used by plants; while Southwest Africa can have higher RUE, because its sporadic and feeble rainfall events would favor grass to fully take the advantage of the ephemerally existed water resources. This conclusion is partly supported by Martiny et al. (2007) based on satellite remote sensing. We further hypothesize that landscape geomorphology in these two drylands may be different and therefore reflect distinctive rainfall characteristics. More bare soil may exist in West Africa grasslands due to intense-rainfall-induced erosion, while Southwest Africa may have more grass fraction and less bare soil fraction. Testing these interesting hypotheses is beyond the scope of this paper, but is worthy the further exploration.
Acknowledgements:

K. Guan and E. F. Wood acknowledge the financial supports from the NASA NESSF fellowship. S.P. Good and K. K. Caylor acknowledge the financial supports from the National Science Foundation through the Grant EAR-0847368. The authors thank Ignacio Rodríguez-Iturbe for his valuable inputs and discussion.
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Robertson, T. R.; Bell, C. W.; Zak, J. C. & Tissue, D. T. (2009), 'Precipitation timing and magnitude differentially affect aboveground annual net primary productivity in


Sato, H.; Kobayashi, H. & Delbart, N. (2010), 'Simulation study of the vegetation structure and function in eastern Siberian larch forests using the individual-based


Table 1. Summary of previous representative studies on assessing the impacts of rainfall characteristics (i.e. rainfall frequency, intensity and seasonality) on the structure and function of terrestrial ecosystem.

**Focus**: frequency (freq); intensity (int); seasonality (sea); variation (CV).

**Methods**: Field Experiments (Field); Remote Sensing (RS); Flux Tower (Flux).

**Major Conclusion**: increasing rainfall intensity (or decreasing frequency) has positive impacts (int+); increasing intensity (or decreasing frequency) has negative impacts (int-); increasing rainfall CV has positive impacts (CV+); increasing rainfall CV has negative impacts (CV-).

<table>
<thead>
<tr>
<th>Focus</th>
<th>Methods</th>
<th>Spatial Scale</th>
<th>Time scale</th>
<th>MAP (mm/year)</th>
<th>Ecosystem type</th>
<th>Major Conclusion</th>
<th>Reference</th>
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<tbody>
<tr>
<td>freq; int</td>
<td>RS</td>
<td>Africa continent</td>
<td>intra-annual</td>
<td>[0,3000]</td>
<td>Africa all</td>
<td>(int-) woody cover</td>
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<td>RS</td>
<td>US</td>
<td>intra-annual</td>
<td>[163,1227]</td>
<td>US</td>
<td>(int-) ANPP greatest in arid grassland (16%) and Mediterranean forest (20%) and less for mesic grassland and temperate forest (3%)</td>
<td>Zhang et al., 2013</td>
</tr>
<tr>
<td>freq; int</td>
<td>RS</td>
<td>Pan-tropics (35°N to 15°S)</td>
<td>inter-annual</td>
<td>[0,3000]</td>
<td>Tropical ecosystems</td>
<td>(CV+) wood cover in dry tropics; (CV-) wood cover in wet tropics</td>
<td>Holmgren et al., 2013</td>
</tr>
<tr>
<td>freq; int</td>
<td>RS</td>
<td>Northern China</td>
<td>intra-annual</td>
<td>[100,850]</td>
<td>temperate grassland and forests</td>
<td>(int-) NDVI for temperate grassland and broadleaf forests, not for coniferous forest</td>
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<td>shrubland and forest</td>
<td>(int-) GPP, RE and NEP</td>
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<td>grassland</td>
<td>(int-) ANPP</td>
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<td>ANPP</td>
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<td>grassland</td>
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<td>impact biomass and bare soil fraction</td>
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<td>242</td>
<td>grassland</td>
<td>Mediterranean dryland ecosystem has more resilience for intra- and inter-annual changes in rainfall</td>
<td>Miranda et al., 2008</td>
</tr>
</tbody>
</table>
Figure 1. a-b: Spatial pattern of the rainfall characteristics in Africa: a-MAP; b-rainfall intensity; c-rainfall frequency; d-rainy season length. The black-line identified areas refer to two savanna regions in West and Southwest Africa. e-f: Normalized histograms of the rainfall characteristics in two savanna regions of West and Southwest Africa. e-MAP (bin width for the x-axis: 100 mm/year); f-rainfall intensity (bin width for the x-axis: 1 mm/event); g-rainfall frequency (bin width for the x-axis: 0.1 event/day); h-rainy season length (bin width for the x-axis: 20 days).
Figure 2. Schematic diagram of water stress factor ranging from 0 (most stressful) to 1 (no stress), which acts to reduce transpiration and carbon assimilation. The red dotted line is based on Porporato et al. (2001) with a reversed sign, and SEIB-DGVM has a nonlinear implementation (blue solid line, Sato and Ise, 2012).
Figure 3. Differences in simulated dominated biomes in the three experiments (i.e. $S_{\lambda-\alpha}$, $ST_{w-\lambda}$, $ST_{w-\alpha}$).
Figure 4. Simulated changes in annual mean soil moisture (0-500mm, first column) and annual mean GPP (second column) for different experiments. Please note that the scales of $S_{\lambda-\alpha}$ is much smaller than those of $S_{Tw-\lambda}$ and $S_{Tw-\alpha}$. The two areas with black boundaries in each panel are West African grassland and Southwest African grassland associated with Figure 1. The spatial patterns shown here are smoothed by 3*3 smoothing window from the raw data.
Figure 5. Differences in simulated annual GPP as a function of mean annual precipitation and one of the perturbed rainfall characteristics in all the three experiments (i.e. $S_{\lambda-a}$, $S_{Tw-\lambda}$, $S_{Tw-a}$) in the left column. The right column shows the correspondent standard errors (SE, calculated as $SE = \frac{\sigma}{\sqrt{n}}$, where $\sigma$ refers to the standard deviation within each bin, $n$ is the sample size in each bin, and $n$ and $\sigma$ are shown in Figure S4), with larger values associated with more uncertainties and requires more caution in interpretation. The contours are based on the binned values, with for each 100 mm/year in MAP, each 0.05 event/day in rainfall frequency, each 1 mm/event in rainfall intensity and each 15 day in rainy season length.
Figure 6. Illustrative time series for hydrological controls on plant root-zone soil moisture dynamics for all the experiments, and these illustrations are generalized based on the simulated time series from the experiments. Both negative and positive cases are shown, and cases with directly hydrological controls are shown (i.e. cloud-induced negative impacts in tropical forests are not shown). The cumulative shaded areas refer to “plant water stress” defined by Porporato et al. (2001).
Supplementary materials:

Figure S1. Comparison of biomes and annual GPP between $S_{\text{climatology}}$ and $S_{\text{control}}$ to test the validity of the synthetic weather generator. The biome definition follows Sato and Ise (2012).
Figure S2. Simulated biomes for different experiments.
Figure S3. Normalized histograms of three simulated dominating biomes in the three experiments.
Figure S4. The sample size ($n$) in each bin (left column) and standard deviation ($\sigma$) in each bin (right column), corresponding to Figure 5. In Figure 5 right column, standard deviation (SE) is calculated as $SE = \frac{\sigma}{\sqrt{n}}$. 