Evaluation of Coral Reef Carbonate Production Models at a Global Scale

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Abstract
Calcification by coral reef communities is estimated to account for half of all carbonate produced in shallow water environments and more than 25% of the total carbonate buried in marine sediments globally. Production of calcium carbonate by coral reefs is therefore an important component of the global carbon cycle; it is also threatened by future global warming and other global change pressures. Numerical models of reefal carbonate production are needed for understanding how carbonate deposition responds to environmental conditions including atmospheric CO$_2$ concentrations in the past and into the future. However, before any projections can be made, the basic test is to establish model skill in recreating present day calcification rates. Here we evaluate four published model descriptions of reef carbonate production in terms of their predictive power, at both local and global scales. We also compile available global data on reef calcification to produce an independent observation-based dataset for the model evaluation of carbonate budget outputs. The four calcification models are based on functions sensitive to combinations of light availability, aragonite saturation ($\Omega_a$) and temperature and were implemented within a specifically-developed global framework, the Global Reef Accretion Model (GRAM). No model was able to reproduce independent rate estimates of whole reef calcification, and the output from the temperature-only based approach was the only model to significantly correlate with coral-calcification rate observations. The absence of any predictive power for whole reef systems, even when consistent at the scale of individual corals, points to the overriding importance of coral cover estimates in the calculations. Our work highlights the need for an ecosystem modeling approach, accounting for population dynamics in terms of mortality and recruitment and hence calcifier abundance, in estimating global reef carbonate budgets. In addition, validation of reef carbonate budgets is severely hampered by limited and inconsistent methodology in reef-scale observations.
1 Introduction

Coral reefs are the product of long-term CaCO$_3$ accretion by calcifying organisms of the reef community (e.g. Hatcher, 1997; Perry et al., 2008), principally scleractinian corals and crustose coralline algae (CCA; e.g. Chave et al., 1972; Barnes and Chalker, 1990; Kleypas and Langdon, 2006; Mallela, 2007; Vroom, 2011). Coral reefs persist where net CaCO$_3$ accretion is achieved, i.e. where calcification by reef organisms exceeds dissolution and bioerosion (reviewed by Kleypas and Langdon, 2006; Fig. 1; Perry, 2011). Globally, coral reef calcification accounts for ~50% of shallow water (neritic) CaCO$_3$ production (Milliman, 1993) with an estimated budget of 0.65–0.83 Pg of CaCO$_3$ each year (Vecsei, 2004). Most of this annual global carbonate production ($G_{\text{global}}$) is preserved and buried, and so coral reefs play an important role in global carbon cycling (Vecsei, 2004) and hence the control of atmospheric CO$_2$.

Although the precise mechanisms by which calcification occurs in both corals and coralline algae are still poorly understood (reviewed by Allemand et al., 2011), it is thought that the rate of calcification is environmentally modulated by some combination of seawater aragonite saturation state ($\Omega_a$), temperature and light availability (Buddemeier and Kinzie, 1976; Kleypas and Langdon, 2006; Tambutté et al., 2011). As a result, it is anticipated that calcification on coral reefs is sensitive to climate change and ocean acidification (e.g. Kleypas et al., 1999; Erez et al., 2011; Hoegh-Guldberg, 2011). In particular the reduction of $\Omega_a$ due to ocean acidification causing decreased calcification of individual corals (reviewed by Kleypas and Yates, 2009; Andersson and Gledhill, 2013) and coralline algae (e.g. Anthony et al., 2008; Johnson and Carpenter, 2012; Johnson et al., 2014), and rising sea surface temperatures causing an increase in coral bleaching frequency due to heat stress (e.g. Donner et al., 2005; Baker et al., 2008; Frieler et al., 2013).

The global reef carbonate budget (i.e. $G_{\text{global}}$) is inherently difficult to evaluate because it is impossible to empirically measure this variable; instead it must be extrapolated from reef-scale observations. Vecsei (2004) synthesized census-based measurements to produce values of reef calcification rates ($G_{\text{reef}}$; Fig. 1) – that varied both regionally and with depth – to estimate $G_{\text{global}}$ (0.65–0.83 Pg yr$^{-1}$). In contrast, the earlier estimate of $G_{\text{global}}$ (0.9 Pg yr$^{-1}$) from Milliman (1993) is calculated from two modal values for $G_{\text{reef}}$ (reefs: 0.4 g cm$^{-2}$ yr$^{-1}$, lagoons: 0.08 g cm$^{-2}$ yr$^{-1}$). Opdyke and
Walker (1992) found a lower estimate of reefal CaCO$_3$ budget of 1.4 Pg yr$^{-1}$ derived from published Holocene CaCO$_3$ accumulation rates. Census-based methods calculate $G_{\text{reef}}$ by summing the calcification by each reef-calcifier, multiplied by its fractional cover of the reef substrate (Chave et al., 1972; Perry et al., 2008). The calcification by individual components of the reef community may be derived from linear extension rates or published values for representative species (Vecsei, 2004). Often it is only calcification by scleractinian corals ($G_{\text{coral}}$) and coralline algae ($G_{\text{algae}}$) that are considered, due to their dominance in CaCO$_3$ production (e.g. Stearn et al., 1977; Eakin, 1996; Harney and Fletcher, 2003). Calcification rates for portions of a reef (e.g. reef flat or back reef) can also be calculated from the total alkalinity change ($\Delta A_T$) of seawater (e.g. Silverman et al., 2007; Shamberger et al., 2011; Albright et al., 2013). This is because precipitation of CaCO$_3$ decreases the total alkalinity ($A_T$) of seawater whereas dissolution has the opposite effect. This alkalinity anomaly technique was first used in a reef setting in the 1970s (Smith and Pesret, 1974; Smith and Kinsey, 1978) and has since been used to estimate basin-scale pelagic and coral reef calcification (Steiner et al., 2014). $G_{\text{reef}}$ is calculated by measuring the change in $A_T$ over a discrete time interval ($\Delta t$); because the change in $A_T$ includes dissolution the calcification measured is net ecosystem calcification (NEC) or net $G_{\text{reef}}$ (Eq. 1; Albright et al., 2013):

$$G_{\text{reef}} = -0.5 \cdot p z \frac{\Delta A_T}{\Delta t}$$  \hspace{1cm} (Eq. 1)

where $p$ is seawater density (kg m$^{-3}$) and $z$ is water depth (m). $G_{\text{reef}}$ measured using $\Delta A_T$ accounts for inorganic precipitation ($G_i$; Fig. 1) and dissolution; however, unlike census-based methods for calculating $G_{\text{reefs}}$ it is not possible to break down the contribution of individual calcifers in the reef community (Perry, 2011). $G_{\text{coral}}$ calculated from the width and density of annual bands within the colony skeleton is commonly used in census-based observations of $G_{\text{reef}}$ (Fig. 1; Knutson et al., 1972).

Estimates of $G_{\text{global}}$ alone tell us little about how reefs will be affected by climate change at a global scale. Instead, if coral calcification ($G_{\text{coral}}$) and reef community calcification rates ($G_{\text{reef}}$) can be numerically modeled as a function of the ambient physicochemical environment (e.g. irradiance ($E$), $\Omega_a$ and temperature), then the results could be scaled up to produce an estimate of $G_{\text{global}}$ that could be re-calculated
as global environmental conditions change. Examples of this approach (Table 1) include: (1) Kleypas (1997; ‘ReefHab’), which is sensitive to \( E \) only and was initially developed to predict global reef calcification (\( G_{\text{global}} \)) and habitat area and used to estimate changes in \( G_{\text{global}} \) since the Last Glacial Maximum; (2) Kleypas, Anthony and Gattuso (2011; ‘KAG’), which simulates \( G_{\text{reef}} \) as a function of \( E \) and \( \Omega_a \) and was originally developed to simulate carbonate chemistry changes in seawater on a reef transect; (3) Lough (2008; ‘LOUGH’) which simulates \( G_{\text{coral}} \) as a function of sea surface temperature (SST) and was derived from the strong relationship observed between SST and \( G_{\text{coral}} \) in massive \( P. \text{sp.} \) colonies from the Great Barrier Reef (GBR), Arabian Gulf and Papua New Guinea; and (4) Silverman, Lazar, Cao, Caldeira and Erez (2009; ‘SILCCE’), which simulates \( G_{\text{reef}} \) as a function of SST and \( \Omega_a \) and was used to simulate the effects of projected future SSTs and \( \Omega_a \) at known reef locations globally. Although further models exist describing \( G_{\text{coral}} \) as a function of carbonate ion concentration ([\( \text{CO}_3^{2-} \)); Suzuki et al., 1995; Nakamura and Nakamori, 2007] these are synonymous to the \( \Omega_a \) function used in KAG and SILCCE. With the exception of Kleypas et al. (2011), which included classes non-calcifying substrate, the above models do not account for community composition. Reef calcification rates vary considerably depending on the abundance of corals and coralline algae (Gattuso et al., 1998). Therefore, successful up scaling of \( G_{\text{reef}} \) and \( G_{\text{coral}} \) to estimate \( G_{\text{global}} \) also requires, as a minimum, quantifying live coral coral (LCC).

To date it remains to be demonstrated that any of the published models reproduce present day reef calcification rates (i.e. \( G_{\text{reef}} \)). Despite this, simulations of the effects of future climate scenarios have been attempted using calcification rate models. For example, McNeil et al. (2004) incorporated LOUGH with the linear relationship observed between \( \Omega_a \) and calcification in the BioSphere 2 project (Langdon et al., 2000), and predicted that \( G_{\text{reef}} \) will increase in the future. In contrast, a similar study by Silverman et al. (2009; SILCCE) concluded that coral reefs will start to dissolve. Whilst McNeil’s study was criticized for its incorrect underlying assumptions (Kleypas et al., 2005), the contradictory predictions from these two models highlights the importance of comparing and fully evaluating reef calcification models, starting with their performance against present day observations.
Here we describe a novel model framework, the global reef accretion model (GRAM), and evaluate the four previously published calcification models (ReefHab, KAG, LOUGH and SILCCE) in terms of their skill in predicting $G_{\text{coral}}$ and $G_{\text{reef}}$. The independent evaluation dataset comprises observations of $G_{\text{reef}}$ from census-based methods and $\Delta A_T$ experiments as well as $G_{\text{coral}}$ measured from coral cores. The individual model estimates of $G_{\text{global}}$ are discussed in comparison with previous empirical estimates. We highlight where model development is required in order to accurately simulate the effects of past and future environmental conditions on calcification rates in coral reefs.
2 Methods

2.1 Model Description

Four calcification models were selected for evaluation in global scale simulations: (1) ReefHab (Kleypas, 1997), (2) KAG (Kleypas et al., 2011), (3) LOUGH (Lough, 2008) and (4) SILCCE (Silverman et al., 2009; Table 2). Previous applications for these models cover a hierarchy of spatial scales (colony, LOUGH; reef, KAG and global, ReefHab and SILCCE) as well as representing different approaches for measuring $G_{\text{coral}}$ (Fig. 1; LOUGH) and $G_{\text{reef}}$ (Fig. 1; ReefHab, KAG and SILCCE). Any modification of the models from the published form is described below, and these are only made where necessary to fit them into the same GRAM framework.

2.1.1 ReefHab

Kleypas (1997) developed ReefHab to predict changes in the global extent of reef habitat since the last Glacial Maximum (Kleypas, 1997). Like photosynthesis, calcification is light saturated (Allemand et al., 2011); as the rate of calcification increases toward a maximum value, it becomes light saturated after irradiance increases beyond a critical value. This curvilinear relationship can be described with various functions, however, hyperbolic tangent and exponential functions have been found to best describe the relationship (Chalker, 1981). The ReefHab model calculates vertical accretion ($G_{\text{reef}}$ in cm m$^{-2}$ d$^{-1}$) as a function of irradiance at the depth of the seabed ($E_z$) and maximum growth rate ($G_{\text{max}} = 1$ cm yr$^{-1}$). The hyperbolic tangent function uses a fixed light saturation constant ($E_k = 250$ µmol m$^{-2}$ s$^{-1}$) to generate a scaling factor for $G_{\text{max}}$ (Eq. 2):

$$G_{\text{reef}} = G_{\text{max}} \cdot \tanh \left( \frac{E_z}{E_k} \right) \cdot TF \quad E_z > E_c$$

(Eq. 2)

where $E_z$ is derived from the surface irradiance ($E_{\text{surf}}$) and the inverse exponent of the product of the light attenuation coefficient ($K_{490}$) and depth ($z$; Eq. 3). Following the methodology in Kleypas (1997), if $E_z$ is less than the minimum irradiance necessary for calcification (250 µmol m$^{-2}$ s$^{-1}$) $G_{\text{reef}} = 0$ cm m$^{-2}$ d$^{-1}$. TF is the topography factor (Eq. 4), which reduces $G_{\text{reef}}$ in areas of low topographic relief.

$$E_z = E_{\text{surf}} \cdot e^{-K_{490}z}$$

(Eq. 3)
\[ TF = \frac{m(\alpha \cdot 100)}{5} \quad (Eq. 4) \]

where \( \alpha \) is calculated from a nine cell neighborhood (center index 2,2) by summing the inverse tangent of the difference between cell depths \((z_{ij} - z_{2,2})\) divided by the distance between cell centers \((D_{ij,2,2})\).

\[ \alpha = \sum_{i=1}^{3} \sum_{j=1}^{3} \frac{\tan^{-1}z_{ij} - z_{2,2}}{D_{ij,2,2}} \quad (Eq. 5) \]

Vertical accretion \((\text{cm m}^{-2} \text{ d}^{-1})\) is converted to \(g \ (\text{CaCO}_3) \text{ cm}^{-2} \text{ d}^{-1}\) by multiplying average carbonate density \((2.89 \text{ g cm}^{-3})\) and porosity \((50 \%)\) as defined by Kleypas (1997).

### 2.1.2 KAG

Anthony et al. (2011) performed laboratory flume incubations on \textit{Acropora aspera} to parameterize the relationship between (day and night) calcification rates and \(\Omega_a\), determining the reaction order \((n)\) and maximum calcification rates \((k_{\text{day}}\) and \(k_{\text{night}})\). The resultant model was then implemented by Kleypas et al. (2011), with the addition of an exponential light sensitive function that accounted for light enhanced calcification, to simulate seawater chemistry changes along a reef transect at Moorea, French Polynesia. The transect did not exceed 2 m in depth; therefore, it was appropriate to use the surface irradiance \((E_{\text{surf}})\) for the calculation of \(G_{\text{reef}}\). In this study \(G_{\text{reef}}\) is calculated \((Eq. 6)\) using \(E_z\) \((Eq. 3)\) rather than \(E_{\text{surf}}\) because the maximum depth in the model domain is 100 m, greatly exceeding the depth of the original application.

\[ G_{\text{reef}} = (G_{\text{max}}(1 - e^{-E_z/E_k})^n + G_{\text{dark}}) \cdot A_c \quad (Eq. 6) \]

where \(A_c\) is the fractional cover of live coral \((i.e. \ A_c = 1 \ when \ coral \ cover \ is \ 100\%)\). Here \(E_k\) is greater than in ReefHab \((400 \mu \text{mol m}^{-2} \text{ s}^{-1} \ versus \ 250 \mu \text{mol m}^{-2} \text{ s}^{-1})\) following the parameterization used by Kleypas et al. (2011). \(G_{\text{reef}}\) is calculated here in \(\text{mmol m}^{-2} \text{ d}^{-1}\) and is divided into day and night rates \((G_{\text{max}}\) and \(G_{\text{dark}})\) both are calculated as a function of \(\Omega_a\). For this study it was necessary to introduce day length \((L_{\text{day}}; \text{ hrs})\) to Eq. 7 and Eq. 8 because of the daily time step as opposed to the hourly timestep of the original model.
\[ G_{\text{max}} = k_{\text{day}}(\Omega - 1)^n L_{\text{day}} \]  
(Eq. 7)

\[ G_{\text{dark}} = k_{\text{dark}}(\Omega - 1)^n (24 - L_{\text{day}}) \]  
(Eq. 8)

\[ L_{\text{day}} \] was calculated using the method described by Haxeltine and Prentice (1996), which uses Julian day \((J_d)\) and latitude \((\text{lat})\) as follows:

\[ L_{\text{day}} = 0 \quad u \leq v \]  
(Eq. 9)

\[ L_{\text{day}} = 24 \cdot \frac{\cos^{-1}(-u/v)}{2\pi} \quad u > -v, u < v \]  
(Eq. 10)

\[ L_{\text{day}} = 24 \quad u \geq v \]  
(Eq. 11)

where the variables \(u\) and \(v\) are calculated from \(\text{lat}\) and \(aa\) (a function of \(J_d\); Eq. 14).

\[ u = \sin(\text{lat}) \cdot \sin(aa) \]  
(Eq. 12)

\[ v = \cos(\text{lat}) \cdot \cos(aa) \]  
(Eq. 13)

\[ aa = -23.4^\circ \cdot \cos \left( \frac{360(J_d+10)}{365} \right) \]  
(Eq. 14)

CaCO\(_3\) production in mmol m\(^{-2}\) d\(^{-1}\) was converted to g cm\(^{-2}\) d\(^{-1}\) using the molecular weight of CaCO\(_3\) \((MR = 100)\).

2.1.3 LOUGH

ReefHab and KAG were both derived from theoretical understanding of the process of calcification and parameterized by values observed in the literature or \textit{in situ}. In contrast, LOUGH was derived from the observed relationship between annual calcification rates of massive \textit{Porites} sp. colonies and local SST (Lough, 2008). A linear relationship (Eq. 15) was fitted to data from 49 reef sites from the Great Barrier Reef (GBR; Lough and Barnes, 2000), Arabian Gulf and Papua New Guinea (Lough, 2008), and accounted for 85 \% of the variance \((p < 0.001)\).

\[ G_{\text{coral}} = \frac{0.327 \cdot \text{SST} - 6.98}{365} \]  
(Eq. 15)
Division by 365 days is necessary here to adapt the original model to the daily timestep used in this study and results in $G_{\text{coral}}$ in g cm$^{-2}$ d$^{-1}$.

2.1.4 SILCCE

Using the alkalinity anomaly technique ($\Delta A_T$), Silverman et al. (2007) found a correlation between rates of inorganic precipitation ($G_i$) and net $G_{\text{reef}}$ (mmol m$^{-2}$ d$^{-1}$). Silverman et al. (2009) fitted observations to Eq. 16 to calculate $G_i$ as a function of $\Omega_a$ and SST (Eq. 17):

$$G_i = k_{\text{SST}}(\Omega_a - 1)^{n_{\text{SST}}}$$  \hspace{1cm} (Eq. 16)

$$G_i = \frac{24}{1000}(-0.0177 \cdot \text{SST}^2 + 1.4697 \cdot \text{SST} + 14.893)(\Omega_a - 1)^{0.0628 \cdot \text{SST} + 0.0985}$$  \hspace{1cm} (Eq. 17)

Incorporating Eq. 17 with SST and $\Omega_a$ sensitivity of coral calcification gives $G_{\text{reef}}$ (Eq. 18):

$$G_{\text{reef}} = k'_r \cdot G_i \cdot e^{-(k'_p(\text{SST} - T_{\text{opt}})/\Omega_a^2)} \cdot A_c$$  \hspace{1cm} (Eq. 18)

where $k'_r$ (38 m$^2$ m$^{-2}$) and $k'_p$ (1 °C$^{-1}$) are coefficients controlling the amplitude and width of the calcification curve. $T_{\text{opt}}$ is the optimal temperature of calcification and is derived from summer temperatures in the WOA 2009 monthly average SST (Locarnini et al., 2010): June (in the Northern Hemisphere) and December (in the Southern Hemisphere). Again, CaCO$_3$ production in mmol m$^{-2}$ d$^{-1}$ was converted to g cm$^{-2}$ d$^{-1}$ using the molecular weight of CaCO$_3$ ($MR = 100$).

2.1.5 Global Reef Accretion Model (GRAM) framework

The calcification production models above were implemented within our global reef accretion model (GRAM) framework. In this study, GRAM was implemented on a 0.25° × 0.25° global grid. Vertically, the model domain was resolved with 10 depth levels at equal 10 m intervals with the fraction, by area, of a model cell (quasi-seabed) within each 10 m layer recorded for calculating total CaCO$_3$ production (Fig. 2). A physicochemical mask was imposed to limit CaCO$_3$ production to shallow-water tropical and sub-tropical areas. This mask was defined following Kleypas (1997; Kleypas et al., 1999b): SST ($> 18$ °C), salinity (23.3-41.8) and depth ($\leq 100$ m).
Calcification was calculated on a daily basis over the course of one full calendar year and according to the environmental conditions at each grid cell (described below).

### 2.2 Input Data Description

Table 1 lists the data used to force GRAM. Ocean bathymetry was calculated from GEBCO One Minute dataset (https://www.bodc.ac.uk/data/online_delivery/gebco/) and mapped to the model grid. Monthly values for SST (Locarnini et al., 2010) and salinity (Antonov et al., 2010) were obtained from the World Ocean Atlas (WOA) 2009. These climatologies are reanalysis products of observations collected 1955-2009. The WOA data have a scaled vertical resolution with 24 layers, with a maximum depth of 1400 m; however, only surface values were used in this study. Daily photosynthetically available radiation (PAR), for the period 1991-1993, were obtained from the Bishop's High-resolution (DX) surface solar irradiance data (Lamont-Doherty Earth Observatory, 2000) derived from the International Satellite Cloud Climatology Project (ISCCP) data (Bishop and Rossow, 1991; Bishop et al., 1997). Following Kleypas (1997), units of dW m$^{-2}$ were converted to $\mu$mol m$^{-2}$ s$^{-1}$ by multiplying by a factor of 0.46. Monthly diffuse light attenuation coefficient of 490 nm light ($K_{490}$) was obtained from the Level-3 binned MODIS-Aqua products in the OceanColor database (available at http://oceancolor.gsfc.nasa.gov). Surface $\Omega_a$ was derived from the University of Victoria’s Earth System Climate Model (Schmittner et al., 2009; Turley et al., 2010) for the decade 1990-2000. All input data were converted, without interpolating, to the same resolution as the model by recording the closest data point to the coordinates of the model grid cell’s center. Missing values were extrapolated as an unweighted mean from the nearest values in the dataset found in the model cell’s neighborhood (including diagonals) in an area up to 1° from the missing data point.

### 2.3 Evaluation dataset and methodology

An independent dataset of *in situ* measured calcification rates ($G_{\text{reef}}$ and $G_{\text{coral}}$) was collated from the literature to evaluate model performance. In total, data from 11 coral core studies (Table 3; *Montastrea* and *Porites* sp.), 8 census-based and 12 $\Delta A_T$ studies (Table 4) were assembled. This dataset is not comprehensive of all studies that have measured $G_{\text{reef}}$ and $G_{\text{coral}}$; many older studies were excluded (e.g. Sadd, 1984) due to
errors in calculation of $G_{\text{reef}}$ that were resolved by Hubbard et al. (1990). The studies sampled cover a representative range of SST and $\Omega_a$ conditions in which present day reefs are found (Fig. 3). The positions of the \textit{in situ} measurements were used to extract the equivalent data points from the gridded model output. Where location coordinates were not reported, Google Earth (available at http://earth.google.com) was used to establish the longitude and latitude, accurate to the model resolution of 0.25°. For uniformity, reported units of measurement were converted to g (CaCO$_3$) cm$^{-2}$ yr$^{-1}$. The values of live coral cover (LCC) reported in the census-based and $\Delta A_T$ studies were used to convert model $G_{\text{coral}}$ to $G_{\text{reef}}$. A global average of 30% (Hodgson and Liebeler, 2002) was used where live coral cover was not reported (Table 4).

Model skill in reproducing the observed data was assessed using simple linear regression analysis preformed on observed calcification rates paired with their equivalent model value. When testing LOUGH against coral core data, values that were used in the original formulation of the model (Lough, 2008) were excluded so as to preserve the independence of the data. Similarly, when correlating SILCCE with $\Delta A_T$ data, the Silverman et al. (2007) datum was excluded. A global average live coral cover of 30% (Hodgson and Liebeler, 2002) was applied to model CaCO$_3$ production in model comparisons with census-based and $\Delta A_T$ $G_{\text{reef}}$ at a global scale. Global mean $G_{\text{reef}}$ and $G_{\text{global}}$ were calculated by applying a further 10% reefal area to model CaCO$_3$ production; this follows the assumption in Kleypas (1997) that 90% of the seabed is composed of unsuitable substrate for reef colonization and growth. Global and regional values are compared directly to the most recent estimates by Vecsei (2004), although other global estimates are also considered.
3 Results

3.1 Model carbonate production rates

Globally averaged values of $G_{\text{reef}}$ (summarized in Table 5) vary little between ReefHab ($0.65 \pm 0.35 \text{g cm}^{-2} \text{yr}^{-1}$), KAG ($0.51 \pm 0.21 \text{g cm}^{-2} \text{yr}^{-1}$) and LOUGH ($0.72 \pm 0.35 \text{g cm}^{-2} \text{yr}^{-1}$), with SILCCE producing a somewhat smaller value ($0.21 \pm 0.11 \text{g cm}^{-2} \text{yr}^{-1}$). A consistent feature across all models is the high carbonate production in the southern Red Sea along the coast of Saudi Arabia and Yemen and, in KAG and LOUGH, the East African coast (Fig. 4). In all models, there was very low calcium carbonate production in the northern Red Sea compared to the south. There is higher calcium carbonate production in the western Pacific than in the east, and along the Central American and northern South American coastline, and this is more pronounced in KAG and LOUGH than ReefHab. In scaling up to the global scale, estimates of $G_{\text{global}}$ based on the models ReefHab (1.40 Pg yr$^{-1}$) and SILCCE (1.1 Pg yr$^{-1}$) were substantially lower than for the other model setups (3.06 Pg yr$^{-1}$ for KAG and 4.32 Pg yr$^{-1}$ for LOUGH).

3.2 Observed carbonate production rates

Figure 5 shows the location and magnitude of the calcification observations. Coral core ($G_{\text{coral}}$) values are higher ($0.5$-$2.8 \text{g cm}^{-2} \text{yr}^{-1}$; full dataset in online supplementary material) than $G_{\text{reef}}$ measurements from either census-based ($0.1$-$0.9 \text{g cm}^{-2} \text{yr}^{-1}$) or $\Delta A_T$ ($0.003$-$0.7 \text{g cm}^{-2} \text{yr}^{-1}$; Table 4) methods. In general, coral core data show decreasing $G_{\text{coral}}$ with increasing latitude that is most pronounced in Hawaii and along both east and west Australian coastlines (Fig. 5). However, $G_{\text{coral}}$ is not always smaller at higher latitudes. For example, the Arabian Gulf is toward the upper end of all $G_{\text{coral}}$ observations ($1.44 \pm 0.57 \text{g cm}^{-2} \text{yr}^{-1}$; full dataset in online supplementary material) whereas $G_{\text{coral}}$ in the Gulf of Aqaba is twofold smaller ($0.78 \pm 0.28 \text{g cm}^{-2} \text{yr}^{-1}$) despite the similar latitude of the two locations. This result cannot be corroborated by $\Delta A_T$ or census data as there is no observation for the Arabian Gulf, however, there is agreement that calcification in the Gulf of Aqaba is toward to lower end of the observed range for $\Delta A_T$ measured $G_{\text{reef}}$ ($0.18 \pm 0.09 \text{g cm}^{-2} \text{yr}^{-1}$) and $G_{\text{coral}}$ measured from coral cores. In contrast, the census-based and $\Delta A_T$ measurements show no latitudinal trends.
3.3 Model evaluation

Fig. 6 shows the correlation of corresponding model and observed calcification rates. With a slope of 0.97, the only significant correlation was that between LOUGH and independent coral core data ($R^2 = 0.66, p < 0.0001$). The $G_{\text{reef}}$ measured by Perry et al. (2013) in the Caribbean also fell close to a 1:1 line with LOUGH, but the positive trend was not significant, either when considering just this data subset ($R^2 = 0.74, p = 0.14, n = 4$), or all $\Delta A_T$ measured $G_{\text{reef}}$ ($R^2 = 0.57, p = 0.14, n = 11$). The average regional $G_{\text{reef}}$ estimated by all models showed little geographic difference (Fig. 7), which is in conflict with the conclusions of Vecsei (2004) who found the Atlantic, including Caribbean reefs, had the highest $G_{\text{reef}}$ of all regions, followed by the Pacific and GBR (Table 5).

The SILCCE model produced a global average $G_{\text{reef}}$ (0.21 g cm$^{-2}$ yr$^{-1}$) that falls within Vecsei’s (2004) estimated range (0.09–0.27 g cm$^{-2}$ yr$^{-1}$) but all other models were in excess of this (Table 5). Similarly, all model estimates of $G_{\text{global}}$ (1.10–4.32 Pg yr$^{-1}$; Table 5) exceed estimates by Vecsei (2004; 0.65–0.83 Pg yr$^{-1}$). This difference was greatest for KAG and LOUGH (3.06 and 4.32 Pg yr$^{-1}$ respectively). Global reef area (the area sum of all model cells where $G_{\text{coral}} > 0$ g cm$^{-2}$ yr$^{-1}$ and with the 10% reefal area applied) varies significantly between models (Table 5). ReefHab designates 195 $\times 10^3$ km$^2$ as global reef area, which is less than that reported by Vecsei (2004; 304–345 $\times 10^3$ km$^2$), however, the other model setups estimate almost double this (500–592 $\times 10^3$ km$^2$).
4 Discussion

Four coral reef carbonate production models, contrasting in terms of dependent environmental controls, were evaluated at local, regional and global scales. The results show that only the model using SST alone (LOUGH) is able to predict $G_{\text{coral}}$, and to a degree $G_{\text{reefs}}$ with any statistical skill (Fig. 6). At the global scale, there is a large offset between the empirical and model estimates of $G_{\text{global}}$ (Table 5), with the LOUGH $G_{\text{global}}$ estimate approximately a factor of five greater than previous estimates by Milliman (1993) and Vecsei (2004). Although $G_{\text{global}}$ values from ReefHab and SILCCE (1.4 Pg yr$^{-1}$ and 1.1 Pg yr$^{-1}$) are significantly closer to the empirical estimates of $G_{\text{global}}$ than the other models, their poor performance at the local reef scale (measured by $G_{\text{reef}}$ and $G_{\text{coral}}$) undermines confidence in their predictive power at $G_{\text{global}}$ scale. Since empirical estimates of $G_{\text{global}}$ cannot themselves be evaluated, it is necessary to examine the factors involved in the estimation of $G_{\text{global}}$, and what role they play in terms of the disparity with the various model values.

Global reef area is used in extrapolating $G_{\text{reef}}$ to $G_{\text{global}}$ and so may have a significant effect on both model and empirical estimates of $G_{\text{global}}$. The LOUGH model achieves a global reef area of $567 \times 10^3$ km$^2$, comparable to the reef area used by Milliman (1993) and Opdyke and Walker (1992) of $617 \times 10^3$ km$^2$ taken directly from Smith (1978). Whereas Vecsei (2004) used a revised reef area of $304–345 \times 10^3$ km$^2$ (Spalding and Grenfell, 1997) which is almost half Smith’s estimate. Despite this difference in global reef area, Milliman (1993) and Vecsei (2004) estimate comparable values of $G_{\text{global}}$, further confounding evaluation of modeled $G_{\text{global}}$. The question of where to draw the line in terms of establishing reef boundaries is highly pertinent to modeling $G_{\text{global}}$ as it dictates the area considered to be ‘coral reef’. In our analysis, all grid cells with positive CaCO$_3$ production (i.e. $G > 0$ g cm$^{-2}$ yr$^{-1}$) are considered to contain coral reef, even those that may be close to 0 g cm$^{-2}$ yr$^{-1}$. Recently formed (immature) reefs with coral communities that have positive $G_{\text{reef}}$ but where little or no CaCO$_3$ framework is present do exist (Spalding et al., 2001) and are accounted for by all four models. However, these coral communities are not included in reef area reported by Spalding and Grenfell (1997) and further information about their production rates and global abundance is needed to accurately quantify their significance in estimating $G_{\text{global}}$ empirically. The presence of these coral communities
has been correlated with marginal environmental conditions where low (highly variable) temperatures and high nutrient concentrations are seen (Couce et al., 2012).

It logically follows that excluding these marginal reefs by tightening the physicochemical mask for SST to > 20 °C, as derived by Couce et al. (2012), would reduce global reef area and close the gap between empirical and model estimates of $G_{\text{global}}$. Further to this is the assumption within GRAM that the area between reef patches in a ‘reef’ cell (i.e. a cell with $G > 0$ g cm$^{-2}$ yr$^{-1}$) accounts for 90 % of the cell’s area, with only 10 % assumed to be composed of suitable substrate for reef formation and coral recruitment. The availability of suitable substrate has the greatest impact on the biogeography of coral reefs (Montaggioni, 2005) and so clearly needs to be evaluated to improve $G_{\text{global}}$ estimates.

Reef area does not account for all of the disparity between estimates of $G_{\text{global}}$; attenuation of $G_{\text{reef}}$ with depth may also be a causal factor. In both Atlantic and Indo-Pacific reefs, there was an exponential trend, decreasing with depth ($\leq 60$ m), in $G_{\text{reef}}$ data collated by Vecsei (2001). Modeled $G_{\text{reef}}$ estimates should, therefore, also vary as a function of depth. In its published form, LOUGH produces the same value for $G_{\text{reef}}$ throughout the water column; however, we can account for this model limitation by imposing a light-sensitive correction in the form of an exponential function to the output from LOUGH so that $G_{\text{reef}}$ is a function of surface $G_{\text{reef}}$ ($G_{\text{surf}}$) and depth ($z$; Eq. 19):

$$G_{\text{reef}} = G_{\text{surf}} e^{-k_g z} \quad \text{(Eq. 19)}$$

where $k_g$ is a constant controlling the degree of light attenuation with depth, in this estimate $K_{490}$ was used. Equation 19 has the same form as that for calculating light availability (Eq. 3) used in both ReefHab and KAG. Following this adjustment, the LOUGH $G_{\text{global}}$ estimate is reduced to 2.56 Pg yr$^{-1}$, which is closer to empirical estimates. However, where light availability has been incorporated into other models no significant skill in predicting $G_{\text{coral}}$ or $G_{\text{reef}}$ was observed (ReefHab and KAG in Fig. 6).

A further factor that strongly affects $G_{\text{reef}}$ and $G_{\text{global}}$ estimates is the percentage of the reef covered by calcifying organisms (generally abridged as the term ‘live coral
cover’, or LCC, although implicitly including other calcifiers). Applying the global average LCC of 30% clearly does not account for the large spatial and temporal variation in coral cover (<1–43% in the dataset collated here; Table 4). Indeed, only a very limited number of Pacific islands (4/46) were found to have ≥30% LCC between 2000 and 2009 in the compilation of Vroom (2011). The global average of 30% was calculated from surveys of 1107 reefs between 1997 and 2001 (Hodgson and Liebeler, 2002) and represents total hard coral cover (LCC plus recently killed coral), so is an overestimate of LCC. LOUGH has significant skill in replicating observed G_{coral} and has some skill in predicting G_{reef} values observed by a standardized census method (ReefBudget; Perry et al., 2012), but only when the local observed LCC is applied. If however, the global average LCC is applied to LOUGH the correlation with G_{reef} is lost. In addition, the global average coral cover may also account for the uniformity of regional G_{reef} values (Fig. 7), in contrast to the significant differences between regions identified by Vecsei (2004). For example, the Atlantic reefs (including the Caribbean) having the greatest G_{reef} (0.8 g cm^{-2} yr^{-1}) and reefs in the Indian Ocean the smallest G_{reef} (0.36 g cm^{-2} yr^{-1}; Vecsei, 2004; Table 5). The pattern is reversed in terms of coral cover, with Indo-Pacific reefs having ~35% hard coral cover compared to ~23% on Atlantic reefs (Hodgson and Liebeler, 2002). Further studies have shown that Caribbean reefs have greater G_{reef} and vertical accumulation rates than Indo-Pacific reefs, possibly due to increased competition for space on the later (Perry et al., 2008). These issues highlight the need for coral cover to vary dynamically within models, allowing it to change spatially and temporally according to coral population demographics (mortality, growth and recruitment).

A specific example of unrealistic G_{reef} is seen for the Gulf of Carpentaria, where there are no known currently-accreting reefs (Harris et al., 2004) but projections of carbonate production according to output from the LOUGH model are particularly high (Fig. 4). At least seven submerged reefs have been discovered in the Gulf of Carpentaria and a further 50 may exist, but these reefs ceased growth ~7 kyr BP when they were unable to keep-up with sea level rise (Harris et al., 2008). Failure to repopulate may be due to a combination of factors including very low larval connectivity in the Gulf of Carpentaria (Wood et al., 2014) and high turbidity, due to re-suspension of bottom sediments and particulate input from rivers (Harris et al.,
ReefHab is the only model to predict an absence of reef accretion in the majority of the Gulf of Carpentaria (Fig. 4) indicating that model sensitivity to light attenuation is essential. This example also raises two further points: firstly, that there are certainly undiscovered reefs that are not accounted for in empirical estimates of $G_{\text{global}}$ and, secondly, that larval connectivity should be considered in simulations of $G_{\text{reef}}$ because of its role in regulating coral abundance after disturbance (Almany et al., 2009; Jones et al., 2009).

In addition to static coral cover, growth parameters ($G_{\text{max}}$, Eq. 2; $E_k$, Eq. 2 and 6; $k_{\text{day}}$, Eq. 7; $k_{\text{dark}}$, Eq. 8; $k_*'$ and $k_*''$, Eq. 18) did not vary geographically, having the same value in all model grid cells. This potentially affected the skill of KAG in reproducing $G_{\text{coral}}$ and $G_{\text{reef}}$ since in the original application of the model (Kleypas et al., 2011) parameters ($k_{\text{day}}$, $k_{\text{dark}}$ and $E_k$) were determined for observations at the location of the reef transect that was simulated. However, when looking at the correlation of model to data it is important to acknowledge the observational variability and error. The standard deviation, where reported, for census-based and $\Delta A_T$ measured $G_{\text{reef}}$ is $\leq 100\%$ of the mean (Table 4). In addition to this variability, observational error is greater in census-based measurements of $G_{\text{reef}}$ than $\Delta A_T$ measurements (Vecsei, 2004). In a review of reef metabolism, $G_{\text{reef}}$ was shown to vary considerably (0.05–1.26 g cm$^{-2}$ yr$^{-1}$) depending on the abundance of coral and coralline algae (Gattuso et al., 1998). $G_{\text{reef}}$ (measured by $\Delta A_T$) appears to vary little across Pacific coral reefs (Smith and Kinsey, 1976) but Gattuso et al. (1998) attribute this to the similarity of these reefs in terms of community structure and composition, as well as coral cover. The apparent agreement between LOUGH and Caribbean $G_{\text{reef}}$ (as reported by Perry et al. 2013) suggests that a standardized experimental methodology for measuring $G_{\text{reef}}$ is needed and implementing this would also provide a consistent dataset that would be invaluable for model evaluation. Unexpectedly, this result also suggests that LOUGH may have skill in predicting $G_{\text{reef}}$ in the Atlantic Ocean despite the absence of massive $P. sp.$ on which the LOUGH model is built. $P. sp.$ is a particularly resilient genus (e.g. Barnes et al., 1970; Coles and Jokiel, 1992; Loya et al., 2001; Hendy et al., 2003; Fabricius et al., 2011) and so applicability to other reef settings, coral genera and calcifiers as a whole is surprising. $G_{\text{coral}}$ of a single species has been used in some
census-based studies to calculate the $G_{\text{coral}}$ of all scleractinian corals present (Bates et al., 2010) and the LOUGH results suggest this generalization may be appropriate.

Unlike census-based and $\Delta A_T$ methodologies, $G_{\text{coral}}$ measured from coral cores span multiple centuries (Lough and Barnes, 2000) and so smoothes the stochastic nature of coral growth and variations in reef accretion. $G_{\text{coral}}$ and $G_{\text{reef}}$ do vary a great deal temporally. For example, diurnal fluctuations may be up to five fold and result in net dissolution at night (e.g. Barnes, 1970; Chalker, 1976; Barnes and Crossland, 1980; Gladfelter, 1984; Constantz, 1986; McMahon et al., 2013). The median ratio of light to dark calcification rates is 3.0, however, measurements of dissolution in individual corals are rarely reported (Gattuso et al., 1999). At intermediate time scales (weekly–monthly) $G_{\text{coral}}$ may vary by a factor of three, with a degree of seasonal chronology (Crossland, 1984; Dar and Mohammed, 2009; Albright et al., 2013). Over longer time scales ($\geq$ 1 yr), $G_{\text{coral}}$ is less variable (Buddemeier and Kinzie, 1976) and both Hatcher (1997) and Perry et al. (2008) describe reef processes hierarchically according to temporal and spatial scales, finding that time spans of a year or more are required to study processes of reef accretion. The numerous observations of $G_{\text{coral}}$ measured from coral cores is a further advantage over the sparse census and $\Delta A_T$ determinations of $G_{\text{reef}}$ which are generally more costly and labor-intensive. More observations of $G_{\text{reef}}$ are, however, essential to improve statistical power and evaluation of model outputs.

$G_{\text{reef}}$ is also invaluable from a monitoring perspective (reviewed by Baker et al., 2008; e.g. Ateweberhan and McClanahan, 2010) by providing an effective measure of reef health that encompasses the whole reef community and accounting for different relative compositions of corals and algae (Vroom, 2011; Bruno et al., 2014). These benefits provide impetus for future measurements of $G_{\text{reef}}$, but our results demonstrate that a standardization of the methodology (as demonstrated in Perry et al., 2013) must be applied.

The four models used in this study all simplify the physiological mechanisms of calcification to predict $G_{\text{coral}}$ and $G_{\text{reef}}$ as a function of one or two external environmental variables. Calcification is principally a biologically controlled process in corals (e.g. Puverel et al., 2005); occurring at the interface between the polyp’s aboral layer and the skeleton, which is separated from seawater by the coelenteron and oral layer (Gattuso et al., 1999). This compartmentalization means that the
reagents for calcification (Ca\textsuperscript{2+} and inorganic carbon species) must be transported from the seawater through the tissue of the coral polyp to the site of calcification (reviewed in Allemand et al., 2011). Active transport of Ca\textsuperscript{2+}, bicarbonate ions (HCO\textsubscript{3}-) to the site of calcification and removal of protons (H\textsuperscript{+}) regulates the pH and Ω\textsubscript{a} of the calcifying fluid (found between aboral ectoderm and skeleton) and requires energy (reviewed in Tambutté et al., 2011). Although the precise mechanism is unknown it is thought that in light zooxanthellate corals derive this energy from the photosynthetic products (principally oxygen and glycerol) of their symbionts, which is thought to partially explain the phenomenon of light enhanced calcification (reviewed in Gattuso et al., 1999; Allemand et al., 2011; Tambutté et al., 2011). Both the ReefHab and KAG models use this relationship with light to determine \(G_\text{coral}\).

However, corals that have lost their symbionts by ‘bleaching’ continue to show enhanced calcification in the light (Colombo-Pallotta et al., 2010). As such, irradiance alone cannot account for changes in \(G_\text{coral}\). Precipitation of aragonite from the calcifying fluid has been assumed to follow the same reaction kinetics as inorganic calcification with respect to Ω\textsubscript{a} (Hohn and Merico, 2012), i.e. \(k_p \cdot (\Omega_\text{a} - 1)^n\) (following Burton and Walter, 1987). KAG and SILCCE both use this function of seawater Ω\textsubscript{a} in calculating calcification; however, despite the logical connection between Ω\textsubscript{a} and \(G_\text{coral}\) neither model could reproduce observed \(G_\text{coral}\) values. Inorganic precipitation of aragonite increases linearly with temperature (Burton and Walter, 1987) as does respiration in corals when oxygen is not limited (Colombo-Pallotta et al., 2010). This temperature dependence may explain the strong correlation found by Lough (2008) between \textit{Porites} growth and SST and the skill LOUGH has shown in this study at reproducing \(G_\text{coral}\) observed values.

This study has shown that it is possible to predict global variations in coral carbonate production rates (\(G_\text{coral}\)) across an environmental gradient with significant skill simply as a function SST (LOUGH). However, the LOUGH model assumes a linear relationship between SST and coral calcification (\(G_\text{coral}\)) whereas the increase in calcification as a function of increased temperature obviously stops at a certain threshold. For example, there is substantive evidence of declining coral calcification rates in recent decades coinciding with increasing temperatures (e.g. Cooper et al., 2008; De'ath et al., 2009; Cantin et al., 2010; Manzello, 2010; De'ath et al., 2013;
Tanzil et al., 2013). Further laboratory experiments have found a Gaussian or bell-shaped response to increasing temperature with optima between 25 °C and 27 °C (e.g. Clausen and Roth, 1975; Jokiel and Coles, 1977; Reynaud-Vaganay et al., 1999; Marshall and Clode, 2004). In contrast to the linear SST-relationship in LOUGH, Silverman et al. (2009; SILCCE) use the Gaussian relationship found by Marshall and Clode (2004) to modulate the rate of calcification derived from inorganic calcification \(G_i\) calculated from \(\Omega_a\). But, the output from SILCCE is shown to be a poor predictor of \(G_{\text{coral}}\) or \(G_{\text{reef}}\) in this study. While using the LOUGH model alone is clearly not appropriate when applied to future temperature simulations, environmental gradients in \(G_{\text{coral}}\) established using LOUGH could be modulated to account for the physiological effect for heat-stress using degree-heating-months (e.g. Donner et al., 2005; McClanahan et al., 2007) or summer SST anomaly (e.g. McWilliams et al., 2005). This approach would then account for the evidence that corals exhibit widely differing temperature optima depending on their temperature history or climatological-average temperature (Clausen and Roth, 1975).

Since none of the models evaluated in this study showed significant skill in capturing global patterns of \(G_{\text{reef}}\), none of the models provide a reliable estimate of \(G_{\text{global}}\). Successful up-scaling of carbonate production to the reef (\(G_{\text{reef}}\)) and global domain (\(G_{\text{global}}\)) will require accounting for both depth attenuation (e.g. light sensitivity) and inclusion of population demographics affecting calcifier abundance. An ecosystem modeling approach that captures demographic processes such as mortality and recruitment, together with growth, would result in a dynamically and spatially varying estimate of live coral cover. It is also clear that a standardized methodology for census-based measurements is required, as evident from the improved model–data fit in a subset of data collected using the ReefBudget methodology (Perry et al., 2012). Coral calcification rates have slowed by an estimated 30 % in the last three decades (e.g. Bruno and Selig, 2007; Cantin et al., 2010; De'ath et al., 2013; Tanzil et al., 2013) reinforcing the pessimistic prognosis for reefs into the future under climate change (e.g. Hoegh-Guldberg et al., 2007; Couce et al., 2013; Frieler et al., 2013); numerical modeling is an essential tool for validating and quantifying the severity of these trends.
Acknowledgments

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**Tables**

**Table 1** Summary of calcification models implemented in the global reef accretion model (GRAM) framework.

<table>
<thead>
<tr>
<th>Model</th>
<th>ReefHab</th>
<th>KAG</th>
<th>LOUGH</th>
<th>SILCCE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Application or Formulation</td>
<td>Predicting changes to reef habitat extent, globally, since last glacial maximum.</td>
<td>Seawater carbonate chemistry changes on a transect in Moorea, French Polynesia&lt;sup&gt;a&lt;/sup&gt;.</td>
<td>Derived from coral core (&lt;i&gt;Porites&lt;/i&gt; sp.) measurements and temperature form the HadISST dataset (Rayner et al., 2003).</td>
<td>Future climate simulations at reef locations provided by ReefBase&lt;sup&gt;b&lt;/sup&gt;.</td>
</tr>
<tr>
<td>Scale applied</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>&lt;i&gt;E&lt;/i&gt;&lt;sub&gt;surf&lt;/sub&gt;</td>
<td>✔</td>
<td>✔</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>&lt;i&gt;Ω&lt;/i&gt;</td>
<td>-</td>
<td>✔</td>
<td>-</td>
<td>✔</td>
</tr>
<tr>
<td>SST</td>
<td>-</td>
<td>-</td>
<td>✔</td>
<td>✔</td>
</tr>
<tr>
<td>Units</td>
<td>mm m&lt;sup&gt;-2&lt;/sup&gt; yr&lt;sup&gt;-1&lt;/sup&gt;</td>
<td>mmol m&lt;sup&gt;-2&lt;/sup&gt; hr&lt;sup&gt;-1&lt;/sup&gt;</td>
<td>g cm&lt;sup&gt;-2&lt;/sup&gt; yr&lt;sup&gt;-1&lt;/sup&gt;</td>
<td>mmol m&lt;sup&gt;-2&lt;/sup&gt; yr&lt;sup&gt;-1&lt;/sup&gt;</td>
</tr>
</tbody>
</table>

<sup>a</sup> Model output was compared to alkalinity changes measured <i>in situ</i> at Moorea by Gattuso et al. (1993), Gattuso et al. (1996), Gattuso et al. (1997); Boucher et al. (1998).

Table 2 Environmental data description (variable name, units, temporal and spatial resolution), and their sources, used to produce the physico-chemical domain mask (ranges shown) and force the calcification models (ReefHab, KAG, LOUGH and SILCCE) in the global reef accretion model (GRAM) framework.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Unit</th>
<th>Temporal</th>
<th>Spatial</th>
<th>Mask</th>
<th>Range</th>
<th>ReefHab</th>
<th>KAG</th>
<th>LOUGH</th>
<th>SILCCE</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>SST</td>
<td>°C</td>
<td>Monthly</td>
<td>1°</td>
<td>-</td>
<td>18.0 – 34.4</td>
<td>✓</td>
<td>✓</td>
<td>-</td>
<td>✓</td>
<td>WOA 2009 (Locarnini et al., 2010)</td>
</tr>
<tr>
<td>Salinity</td>
<td>–</td>
<td>Annual</td>
<td>1°</td>
<td>-</td>
<td>23.3 – 41.8</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>WOA 2009 (Antonov et al., 2010)</td>
</tr>
<tr>
<td>Bathymetry</td>
<td>m</td>
<td>1/60°</td>
<td>≤100</td>
<td>✓</td>
<td>✓</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>GECBO One Minute Grid</td>
</tr>
<tr>
<td>PAR</td>
<td>dW/m²</td>
<td>Daily</td>
<td>0.5°</td>
<td>✓</td>
<td>✓</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>Bishop's High-Resolution (DX) Surface Solar irradiance (Lamont-Doherty Earth Observatory, 2000)</td>
</tr>
<tr>
<td>$K_{490}$</td>
<td>m⁻¹</td>
<td>Annual</td>
<td>1/12°</td>
<td>✓</td>
<td>✓</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>OceanColor (2013)</td>
</tr>
<tr>
<td>$\Omega_{arag}$</td>
<td>–</td>
<td>Decadal</td>
<td>3.6×1.8°</td>
<td>-</td>
<td>✓</td>
<td>-</td>
<td>✓</td>
<td>-</td>
<td>✓</td>
<td>University of Victoria’s Earth System Model (Weaver et al., 2001; Schmittner et al., 2009; Turley et al., 2010)</td>
</tr>
</tbody>
</table>

SST – sea surface temperature; WOA – World Ocean Atlas; GECBO – general bathymetric chart of the Oceans; BODC – British Oceanographic Data Centre; PAR – surface photosynthetically available radiation; $K_{490}$ – 490nm light attenuation coefficient; $\Omega_{arag}$ – aragonite saturation.
Table 3 Details of studies used for evaluating model calcification rates; observed coral calcification rates ($G_{\text{coral}}$) derived from annual density banding in coral cores; ‘—’ indicates fields that were not reported. Full data, including values of $G_{\text{coral}}$, are supplied in online supplementary material. Studies are listed alphabetically by their ID.

<table>
<thead>
<tr>
<th>ID</th>
<th>Source</th>
<th>Sea/Region</th>
<th>Genus</th>
<th>No. Sites</th>
<th>Period Observed</th>
<th>Latitude °N</th>
<th>Longitude °E</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ch</td>
<td>Chen et al. (2011)</td>
<td>South China Sea</td>
<td>Porites</td>
<td>1</td>
<td>—</td>
<td>22.45</td>
<td>114.69</td>
</tr>
<tr>
<td>Co</td>
<td>Cooper et al. (2012)</td>
<td>Western Australia</td>
<td>Porites</td>
<td>6</td>
<td>1900 – 2010</td>
<td>-28.47 to -17.27</td>
<td>113.77 to 119.37</td>
</tr>
<tr>
<td>De</td>
<td>De'ath et al. (2009)</td>
<td>GBR</td>
<td>Porites</td>
<td>69</td>
<td>1900 – 2005</td>
<td>-23.55 to -9.58</td>
<td>142.17 to 152.75</td>
</tr>
<tr>
<td>Ed</td>
<td>Edinger et al. (2000)</td>
<td>Java Sea</td>
<td>Porites</td>
<td>5</td>
<td>1986 – 1996</td>
<td>-6.58 to -5.82</td>
<td>110.38 to 110.71</td>
</tr>
<tr>
<td>Fa</td>
<td>Fabricius et al. (2011)</td>
<td>Papua New Guinea</td>
<td>Porites</td>
<td>3</td>
<td>—</td>
<td>-9.83 to -9.74</td>
<td>150.82 to 150.88</td>
</tr>
<tr>
<td>Gr</td>
<td>Grigg (1982)</td>
<td>Hawaii</td>
<td>Porites</td>
<td>14</td>
<td>—</td>
<td>19.50 to 28.39</td>
<td>181.70 to 204.05</td>
</tr>
<tr>
<td>He</td>
<td>Heiss (1995)</td>
<td>Gulf of Aqaba</td>
<td>Porites</td>
<td>1</td>
<td>—</td>
<td>29.26</td>
<td>34.94</td>
</tr>
<tr>
<td>Sc</td>
<td>Scoffin et al. (1992)</td>
<td>Thailand</td>
<td>Porites</td>
<td>11</td>
<td>1984 – 1986</td>
<td>7.61 to 8.67</td>
<td>97.65 to 98.78</td>
</tr>
<tr>
<td>Sh</td>
<td>Shi et al. (2012)</td>
<td>South China Sea</td>
<td>Porites</td>
<td>1710 – 2012</td>
<td>9.90</td>
<td>115.54</td>
<td></td>
</tr>
</tbody>
</table>

aData were sourced from the Australian Institute of Marine Science (AIMS): AIMS (2014a) provides access to ‘De’ data and AIMS (2014b) provides access to ‘Co’ data. De data were used in the formulation of LOUGH (Lough, 2008) but subsequently published following further study (De’ath et al., 2009).
Table 4 Details of studies used for evaluating model calcification rates; observed calcification rates are for the reef community \((G_{\text{reef}})\) and are derived from census-based methods or alkalinity reduction experiments \((\Delta TA)\); ‘—’ indicates fields that were not reported. Studies are listed alphabetically by their ID.

<table>
<thead>
<tr>
<th>Measurement Method</th>
<th>ID</th>
<th>Source</th>
<th>Region</th>
<th>Genus or Groups</th>
<th>(G_{\text{reef}} \pm SD)</th>
<th>Cover ± SD</th>
<th>No. Sites</th>
<th>Period Observed</th>
<th>Latitude</th>
<th>Longitude</th>
</tr>
</thead>
<tbody>
<tr>
<td>CENSUS-BASED</td>
<td>Ea</td>
<td>Eakin (1996)</td>
<td>Panama</td>
<td>Pocillopora &amp; CCA</td>
<td>0.37 ± 0.08</td>
<td>30 ± 30</td>
<td>63 ± 32</td>
<td>—</td>
<td>1986 – 1995</td>
<td>7.82</td>
</tr>
<tr>
<td></td>
<td>Gl</td>
<td>Glynn et al. (1979)</td>
<td>Galapagos</td>
<td>Pocillopora &amp; CCA</td>
<td>0.58</td>
<td>26-43</td>
<td>2</td>
<td>1975 – 1976</td>
<td>-1.22</td>
<td>269.56</td>
</tr>
<tr>
<td></td>
<td>Hy</td>
<td>Harney and Fletcher (2003)</td>
<td>Hawaii</td>
<td>Porites, Montipora &amp; CCA</td>
<td>0.12 ± 0.04</td>
<td>32 ± 27</td>
<td>44</td>
<td>60</td>
<td>—</td>
<td>21.41</td>
</tr>
<tr>
<td></td>
<td>Ht</td>
<td>Hart and Kench (2007)</td>
<td>Torres Strait</td>
<td>Corals, CCA, Halimeda, foraminifera, molluscs</td>
<td>0.17 ± 0.18</td>
<td>43</td>
<td>47</td>
<td>—</td>
<td>—</td>
<td>-10.21</td>
</tr>
<tr>
<td></td>
<td>Hu</td>
<td>Hubbard et al. (1990)</td>
<td>St Croix</td>
<td>Montastrea, Agaricia, Porites &amp; CCA</td>
<td>0.12</td>
<td>16</td>
<td>59</td>
<td>4</td>
<td>—</td>
<td>17.78</td>
</tr>
<tr>
<td></td>
<td>La</td>
<td>Land (1979)</td>
<td>Jamaica</td>
<td>Acropora, Montastrea, Agaricia &amp; red/green algae</td>
<td>0.52</td>
<td>30 ± 16</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>18.55</td>
</tr>
<tr>
<td></td>
<td>P1</td>
<td>Perry et al. (2013)</td>
<td>Bonaire</td>
<td>Montastrea, Agaricia, Diploria, Millepora &amp; CCA</td>
<td>0.30 ± 0.21</td>
<td>16 ± 7</td>
<td>—</td>
<td>36</td>
<td>—</td>
<td>16.66</td>
</tr>
<tr>
<td></td>
<td>P2</td>
<td>Perry et al. (2013)</td>
<td>Belize</td>
<td>Montastrea, Agaricia, Diploria, Millepora &amp; CCA</td>
<td>0.30 ± 0.20</td>
<td>12 ± 6</td>
<td>—</td>
<td>26</td>
<td>—</td>
<td>19.30</td>
</tr>
<tr>
<td></td>
<td>P3</td>
<td>Grand Cayman</td>
<td>Bahamas</td>
<td>0.16 ± 0.05</td>
<td>7 ± 3</td>
<td>—</td>
<td>9</td>
<td>—</td>
<td>—</td>
<td>25.41</td>
</tr>
<tr>
<td></td>
<td>St</td>
<td>Stearn et al. (1977)</td>
<td>Barbados</td>
<td>7 coral genera &amp; CCA</td>
<td>0.90</td>
<td>37 ± 22</td>
<td>41</td>
<td>6</td>
<td>1969-1974</td>
<td>13.20</td>
</tr>
<tr>
<td>∆TA</td>
<td>Al</td>
<td>Albright et al. (2013)</td>
<td>GBR</td>
<td>NEC</td>
<td>0.48 ± 0.48</td>
<td>9 ± 2</td>
<td>8.5 ± 3.5</td>
<td>1</td>
<td>Aug &amp; Dec 2012</td>
<td>-18.33</td>
</tr>
<tr>
<td></td>
<td>Authors</td>
<td>Location</td>
<td>Nec</td>
<td>Lcc</td>
<td>Cca</td>
<td>Cca</td>
<td>Cca</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>---</td>
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<td>-----</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>G1</td>
<td>Gattuso et al. (1993)</td>
<td>French Polynesia</td>
<td>NEC</td>
<td>0.09</td>
<td>16c</td>
<td>-</td>
<td>-</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>G2</td>
<td>Gattuso et al. (1996)</td>
<td>French Polynesia</td>
<td>NEC</td>
<td>0.68</td>
<td>16d</td>
<td>4-21</td>
<td>2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>G3</td>
<td>Gattuso et al. (1997)</td>
<td>French Polynesia</td>
<td>NEC</td>
<td>0.003</td>
<td>0.002</td>
<td>~1</td>
<td>~3</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ka</td>
<td>Kayanne et al. (1995)</td>
<td>Japan</td>
<td>NEC</td>
<td>0.37</td>
<td>19#</td>
<td>&lt;1#</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>La</td>
<td>Lantz et al. (2014)</td>
<td>Hawaii</td>
<td>NEC</td>
<td>0.60</td>
<td>±0.15</td>
<td>14</td>
<td>5</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Na</td>
<td>Nakamura and Nakamori (2009)</td>
<td>Japan</td>
<td>NEC</td>
<td>0.16</td>
<td>±0.27</td>
<td>20</td>
<td>10</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ob</td>
<td>Ohde and van Woesik (1999)</td>
<td>Japan</td>
<td>NEC</td>
<td>0.79</td>
<td>22</td>
<td>2</td>
<td>2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sh</td>
<td>Shamberger et al. (2011)</td>
<td>Hawaii</td>
<td>NEC</td>
<td>0.72</td>
<td>±0.36</td>
<td>30</td>
<td>2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Si</td>
<td>Silverman et al. (2007)</td>
<td>Gulf of Aqaba</td>
<td>NEC</td>
<td>0.18</td>
<td>±0.09</td>
<td>35</td>
<td>2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sm</td>
<td>Smith and Harrison (1977)</td>
<td>Marshall Islands</td>
<td>Acropora, Montipora &amp; CCA</td>
<td>0.44</td>
<td>±0.66</td>
<td>14</td>
<td>58</td>
<td>11.45</td>
<td>162.37</td>
<td></td>
</tr>
<tr>
<td>SP</td>
<td>Smith and Pesret (1974)</td>
<td>Line Islands</td>
<td>NEC</td>
<td>0.1</td>
<td>30</td>
<td>100</td>
<td>4.00</td>
<td>201.00</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

CCA – crustose coralline algae; NEC – net ecosystem calcification.

a The value for CCA cover is the average of the % framework reported by Eakin (1996) that is defined as the area of dead coral upon which CCA grows.

b Authors note that the underlying assumptions for calculating calcification by algae may be unrealistic but make best use of the available data at the time of the study.

c Median LCC values of the reported ranges were applied to model output for the regression analysis.
The LCC range reported by Gattuso et al. (1993) was assumed to be the same as in the subsequent study at Moorea (Gattuso et al., 1996).

Values reported in Suzuki et al. (1995) for study conducted in 1991 (Nakamori et al., 1992) at the same location.
Table 5 Average regional and global reef calcification rates ($G_{\text{reef}}$) and global CaCO$_3$ budgets ($G_{\text{global}}$) and reef areas derived from the four model setups ($\leq 40$ m) and Vecsei (2004). Model $G_{\text{reef}}$ is calculated as the total CaCO$_3$ production multiplied by global average live coral cover (LCC) of 30% (Hodgson and Liebeler, 2002) and 10% seabed reefal area with the exception of ReefHab, which uses a function of seabed topographic relief to modify total CaCO$_3$ production to give $G_{\text{reef}}$. Global reef area is 10% of the total area accounting for inter-reefal area.

<table>
<thead>
<tr>
<th>Ocean Region</th>
<th>ReefHab</th>
<th>KAG</th>
<th>LOUGH</th>
<th>SILCCE</th>
<th>Vecsei (2004)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Caribbean Sea</td>
<td>0.86 ± 0.32</td>
<td>0.61 ± 0.07</td>
<td>0.82 ± 0.09</td>
<td>0.23 ± 0.05</td>
<td>0.80 &amp; 0.01$^a$</td>
</tr>
<tr>
<td>North Atlantic Ocean</td>
<td>0.74 ± 0.40</td>
<td>0.44 ± 0.22</td>
<td>0.59 ± 0.21</td>
<td>0.17 ± 0.10</td>
<td></td>
</tr>
<tr>
<td>South Atlantic Ocean</td>
<td>0.51 ± 0.35</td>
<td>0.40 ± 0.27</td>
<td>0.57 ± 0.25</td>
<td>0.16 ± 0.10</td>
<td></td>
</tr>
<tr>
<td>Indian Ocean</td>
<td>0.65 ± 0.36</td>
<td>0.54 ± 0.17</td>
<td>0.82 ± 0.17</td>
<td>0.22 ± 0.08</td>
<td>0.36</td>
</tr>
<tr>
<td>North Pacific Ocean</td>
<td>0.67 ± 0.35</td>
<td>0.49 ± 0.22</td>
<td>0.70 ± 0.22</td>
<td>0.20 ± 0.11</td>
<td>0.65</td>
</tr>
<tr>
<td>South Pacific Ocean</td>
<td>0.67 ± 0.30</td>
<td>0.61 ± 0.20</td>
<td>0.93 ± 0.21</td>
<td>0.29 ± 0.12</td>
<td></td>
</tr>
<tr>
<td>GBR</td>
<td>0.66 ± 0.31</td>
<td>0.67 ± 0.05</td>
<td>0.76 ± 0.04</td>
<td>0.25 ± 0.04</td>
<td>0.45</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Global Metrics ($\leq 40$ m)</th>
<th>$G_{\text{global}}$ (Pg yr$^{-1}$)</th>
<th>Reef area ($\times 10^3$ km$^2$)</th>
<th>$G_{\text{reef}}$ ± SD (g cm$^{-2}$ yr$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1.40</td>
<td>195</td>
<td>0.65 ± 0.35</td>
</tr>
<tr>
<td></td>
<td>3.06</td>
<td>592</td>
<td>0.51 ± 0.21</td>
</tr>
<tr>
<td></td>
<td>4.32</td>
<td>567</td>
<td>0.72 ± 0.35</td>
</tr>
<tr>
<td></td>
<td>1.10</td>
<td>500</td>
<td>0.21 ± 0.11</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0.09–0.27</td>
</tr>
</tbody>
</table>

$^a$ Values of $G_{\text{reef}}$ for Atlantic/Caribbean framework and biodetrital reef respectively.
Fig. 1 Schematic illustrating the coral reef carbonate budget and the modeled parameters ($G_{\text{reef}}$ and $G_{\text{coral}}$) used to quantify carbonate production. Carbonate framework is principally produced by scleractinian corals ($G_{\text{coral}}$) and crustose coralline algae (CCA; $G_{\text{algae}}$); the abiotic (inorganic) precipitation of carbonate cements ($G_i$) also occurs. Bioeroders breakdown the reef framework internally (e.g. worms, sponges) and externally (e.g. parrot fish, crown-of-thorns starfish). The rubble produced is incorporated back in to the framework, by cementation or burial, or exported from the reef. The observational data available to test models of carbonate budget include $G_{\text{coral}}$ measured from coral cores, and $G_{\text{reef}}$ calculated from a reef community census or the total alkalinity of surrounding seawater.
Fig. 2 Schematic of logical steps at each timestep within GRAM. GRAM’s domain is defined by a bathymetric and physicochemical mask within which calcification is calculated, at each timestep and in every domain grid cell, according to the calcification model used. Where calcification is modeled as a function of light, the availability of light at depth ($E_z$) is calculated for each model layer ($z_i$).
Fig. 3 Distribution of sea surface temperatures (SST) and aragonite saturation ($\Omega_a$) at:

(All) reef locations (ReefBase: A Global Information System for Coral Reefs. April, 2014. http://www.reefbase.org); (Cores) coral core data locations; (Census) census-based and ($\Delta A_T$) alkalinity anomaly study locations. SST values are taken from WOA 2009 annual average values (Locarnini et al., 2010) and $\Omega_a$ values are derived from UVic model (Weaver et al., 2001; Schmittner et al., 2009; Turley et al., 2010) output.

The range, 25th and 75th percentiles, median lines and outliers of SST and $\Omega_a$ are displayed in the box and whisker plots.
**Fig. 4** Model outputs of reef carbonate production. Depth integrated (≤ 40 m) CaCO₃ production, with 30% live coral cover (LCC) and 10% seabed reefal area ($G_{reef}$) for:

(a) ReefHab, (b) KAG, (c) LOUGH and (d) SILCCE. $G_{reef}$ values displayed are aggregated from the model resolution (0.25°) to a 1° grid to facilitate visualization.
Fig. 5 Compilation of published reef carbonate production measurements. Location and magnitude of: (a) coral calcification ($G_{\text{coral}}$) observed in coral cores and, reef community calcification ($G_{\text{reef}}$) measured in (b) census-based and (c) alkalinity anomaly studies (See Tables 4 and 5 for study ID keys).
**Fig. 6** Correlation of observed coral calcification ($G_{\text{coral}}$) and reef community calcification ($G_{\text{reef}}$) to model predictions for coral core, census-based and alkalinity anomaly ($\Delta A_T$) data (1:1 relationship shown as red dashed line). All model estimates
are multiplied by the live coral cover (LCC) reported in the observation studies to give $G_{\text{reef}}$ except ReefHab in which $G_{\text{reef}}$ is calculated using a function of topographic relief (TF). The use of TF follows the method of Kleypas (1997); it was derived from empirical observation of reef growth and was a means to scale potential calcification $(G_{\text{coral}})$ to produce $G_{\text{reef}}$ in the absence of global data for LCC. All significant linear regressions are plotted ($p < 0.05$; grey solid line) with equation and regression coefficient ($R^2$). Data used to develop a model are also plotted (open circles) but were excluded from the regression analysis to preserve data independence.
Fig. 7 Box and whisker plots of model estimates for global and regional CaCO$_3$ production. A live coral cover (LCC) of 30% is applied. Range (whiskers), 25$^{th}$ and 75$^{th}$ percentiles (boxes), median (red line), and data outliers (+) are plotted.