Constraining ecosystem carbon dynamics in a data-limited world: integrating ecological “common sense” in a model-data-fusion framework.

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Abstract. Many of the key processes represented in global terrestrial carbon models remain largely unconstrained. For instance, plant allocation patterns and residence times of carbon pools are poorly known globally, except perhaps at a few intensively studied sites. As a consequence of data scarcity, carbon models tend to be underdetermined, and so can produce similar net fluxes with very different parameters and internal dynamics. To address these problems, we propose a series of ecological and dynamic constraints (EDCs) on model parameters and initial conditions, as a means to constrain ecosystem variable inter-dependencies in the absence of local data. The EDCs consist of a range of conditions on (a) carbon pool turnover and allocation ratios, (b) steady state proximity, and (c) growth and decay of model carbon pools. We use a simple ecosystem carbon model in a model-data fusion framework to determine the added value of these constraints in a data-poor context. Based only on leaf area index (LAI) time series and soil carbon data, we estimate net ecosystem exchange (NEE) for (a) 40 synthetic experiments and (b) three AmeriFlux tower sites. For the synthetic experiments, we show that EDCs lead to an an overall 34 % relative error reduction in model parameters, and a 65 % reduction in the 3 yr NEE 90 % confidence range. In the application at AmeriFlux sites all NEE estimates were made independently of NEE measurements. Compared to these observations, EDCs resulted in a 69–93 % reduction in 3 yr cumulative NEE median biases (−0.26 to +0.08 kg C m⁻²), in comparison to standard 3 yr median NEE biases (−1.17 to −0.84 kg C m⁻²).

In light of these findings, we advocate the use of EDCs in future model-data fusion analyses of the terrestrial carbon cycle.
Introduction

Terrestrial ecosystem carbon exchange is a fundamental part of the global carbon cycle link to biosphere processes. Atmospheric CO\textsubscript{2} measurements indicate the presence of a global land C sink, i.e. uptake by the terrestrial biosphere exceeds losses. However, relative to all major terms in the global carbon budget, the global land sink exhibits both the largest inter-annual variability and the largest uncertainty (Le Quéré et al., 2013). The terrestrial carbon budget uncertainty stems largely from unknowns in the size, spatial distribution and temporal dynamics of the major terrestrial carbon pools. As a result, there is little agreement among modelled land sink projections for the 21st century (Todd-Brown et al., 2013; Friend et al., 2013), reflecting uncertainty in knowledge on the current state of the terrestrial C cycle and its dynamics.

In recent years a growing volume of data from flux towers, satellites and plant trait databases has been used to constrain some of the key components of the terrestrial carbon cycle (e.g. Baldocchi et al., 2001; Simard et al., 2011; Kattge et al., 2011). In particular, a range of ecosystem carbon models and datasets have been brought together in model-data fusion (MDF) frameworks to produce an enhanced analysis of ecosystem carbon cycling (e.g. Williams et al., 2005; Fox et al., 2009; Carvalhais et al., 2010; Luo et al., 2012; Smith et al., 2013). Where multiple data streams are available, MDF approaches can provide an extensive insight into carbon pool dynamics, turnover rates, and carbon allocation fractions (Richardson et al., 2010; Keenan et al., 2013). However, even at research intensive sites, MDF studies can produce a wide range of acceptable model parameter sets, due to under-determination of the carbon budget with available data. Some of these optimized parameter sets, even though they generate realistic fluxes over short timescales, are associated with major changes to larger carbon pools (soil, wood) that are nonsensical (Fox et al., 2009). For regional and global scale model implementation, the lack of in-situ measurements amplifies this problem, sometimes referred to as equifinality (Beven and Freer, 2001). Ultimately, we need to overcome data limitations and under-determination by integrating models and ecosystem knowledge in a common framework. This framework must ensure ecologically realistic outcomes, while still encompassing (i.e. effectively quantifying) the uncertainty associated with parameter estimation given observation errors (Hill et al., 2012).

Although a range of process-based models have been used to represent the dynamics of the terrestrial carbon cycle and land–atmosphere CO\textsubscript{2} exchange (e.g. Sitch et al., 2008; Schwalm et al., 2010), there are advantages in using simpler models to estimate ecosystem carbon state variables. Firstly, there is a trade-off between model complexity, such as the number of model parameters, and a model’s ability to reproduce observations (e.g. Akaike, 1974): therefore a low-complexity model is preferable when it can reproduce ecosystem observations with comparable skill. Secondly, complex models are often computationally expensive, and this is an inhibiting factor when using iterative methods (such as Monte Carlo approaches) to estimate model parameters and their uncertainty. Ideally, the key terms of ecosystem carbon dynamics can be constrained by combining ecosystem
observations with a model of appropriate complexity in a computationally efficient MDF framework.

Previous MDF studies have invariably relied on net ecosystem exchange (NEE) measurements (real and synthetic), along with other site-level observations (Williams et al., 2009). In a global context, the FLUXNET flux-tower network (Baldocchi et al., 2001) consists of hundreds of flux tower sites where hectare-scale NEE measurements have been made over the past two decades. In addition to NEE, complimentary site-level biometric data can help resolve model parameters and state variables in an MDF context (Richardson et al., 2010; Hill et al., 2012; Keenan et al., 2013), alleviating the problem of under-determination. However, the terrestrial biosphere will inevitably remain poorly sampled by FLUXNET. Alternative estimates of NEE from atmospheric CO₂ measurements (e.g. Peters et al., 2010; Feng et al., 2011) are only produced at continental-scale resolutions. Therefore, given the limited span of the FLUXNET flux-tower network, are spatially resolved global carbon cycle analyses limited by the sparsity of eddy flux and biometric data?

NEE, the difference between photosynthesis and ecosystem respiration, is a function of the dynamics of all carbon pools over a range of timescales. In the absence of NEE observations, model NEE estimates depend on a knowledge of carbon pool sizes and model parameter values. In reality, carbon pools and model parameters (especially those related to plant allocation fractions and pool turnover rates) are poorly constrained, and therefore NEE estimates are subject to a comparably large uncertainty. Nonetheless, fundamental knowledge on ecosystem behaviour can potentially be used to overcome the lack of location specific data or parameter values. For example, while parameters related to phenology, C allocation and turnover may vary across multiple orders of magnitude (Kattge et al., 2011; Fox et al., 2009), these parameters are strongly correlated (e.g. Sloan et al., 2013), and the range of possible parameter configurations is therefore limited. Such examples include correlations between leaf lifespan and leaf mass per area (Wright et al., 2004), leaf area index and total foliar N (Williams and Rastetter, 1999), and between foliar and root biomass (Sloan et al., 2013). These correlations can confine parameter searches to a smaller hyper-volume. Equally, while ecosystems exhibit a large range of non-steady state dynamic behaviours, strong inter-relationships are expected between inputs, outputs, carbon pool magnitudes and turnover rates (Luo and Weng, 2011). Richardson et al. (2010) introduced the concept of reality constraints (or internal model constraints) on carbon pool dynamics within a carbon cycle MDF analysis: such constraints on the model state can potentially be used to improve estimates of model parameters. Here we propose that a broad range of model parameter combinations can be discarded when phenology, carbon allocation, turnover rates and pool dynamics are considered ecologically “nonsensical”. Here we seek to address the following question: can we improve ecosystem model parameter and NEE estimates by incorporating ecological “common sense” into carbon cycle MDF analyses?

In this paper we propose a series of Ecological and Dynamic Constraints (EDCs) on model parameters: these include turnover and allocation parameter inter-relations, carbon pool dynamics and steady state proximity conditions (Sect. 2). We quantify the added value of imposing EDCs in syn-
thetic and real data MDF contexts using a simple ecosystem carbon model, by measuring bias and confidence interval reductions of carbon cycle analyses relative to independent data (Sect. 3). Finally we discuss the prospects and limitations of our approach, as well as the implications of a wider EDC implementation in terrestrial carbon cycle MDF methods (Sect. 4).

2 Methods

Here we present a series of EDCs for a daily box budget terrestrial C cycle model, the Data Assimilation Linked Ecosystem Carbon model version two (DALEC2). Within an MDF context, we test the added value of implementing EDCs. Our aims are (1) to quantify our ability to estimate DALEC2 parameters and NEE within a synthetic framework, and (2) to validate our ability to estimate NEE at three temperate forest AmeriFlux sites. We use simulated and real observations of (a) satellite-derived leaf area index (LAI) and (b) soil organic carbon from the Harmonized World Soil Database (HWSD, Hiederer and Köchy, 2012) in our MDF analyses. The choice of these two data sets serves as an analogue for the limited ecosystem carbon datasets available on a global scale.

2.1 DALEC2

DALEC has been extensively used in MDF frameworks (e.g. Williams et al., 2005; Quaife et al., 2008; Richardson et al., 2010, amongst others). In particular, a range of MDF approaches were used in the REFLEX project, where ecosystem observations were assimilated into DALEC to produce carbon state analyses (Fox et al., 2009). Here we use the DALEC2 ecosystem carbon balance model, which combines components of DALEC evergreen and DALEC deciduous (Williams et al., 2005; Fox et al., 2009) into a single model. Gross primary production (GPP) in DALEC2 is determined from the aggregated canopy model (Williams et al., 1997), and is allocated to the biomass pools (foliar, labile, wood, and fine roots) and to autotrophic respiration \( R_a \); degraded carbon from biomass pools goes to two dead organic matter pools with temperature dependent losses (heterotrophic respiration, \( R_h \)). The net ecosystem exchange is summarised as \( \text{NEE} = R_a + R_h - \text{GPP} \). C flow in DALEC2 is determined as a function of 23 parameters (including six initial carbon pool states, Table 1). We henceforth refer to the 23 parameters required to initiate DALEC2 as a parameter vector \( x \). DALEC2 C pools and fluxes are iteratively calculated at a daily time-step: the DALEC2 model equations are fully described in Appendix A. We henceforth refer to the ensemble of all model state variables (such as daily NEE, GPP, respiration terms and carbon pool trajectories) as DALEC2(\( x \)).

2.2 Ecological and Dynamic Constraints

In previous work, DALEC MDF approaches (Williams et al., 2005; Fox et al., 2009; Richardson et al., 2010; Hill et al., 2012) did not explicitly impose any conditions on the inter-relationships between model parameters, therefore parameter prior information had only consisted of prescribed
parameter ranges. In reality, broader ecological knowledge can be informative in terms of the inter-
relationships between parameter values. For example, long-term leaf turnover rate must be faster
than woody biomass turnover (e.g. Norby et al., 2002): such a relationship can provide a relative
constraint on model parameter values, without imposing any further constraints to the prior parame-
ter ranges (Table 1).

Here we propose a sequence of ecological and dynamic constraints (EDCs) on DALEC2 pa-
rameters and pool dynamics. For any given DALEC2 parameter vector $x$, all EDCs presented
in this section (henceforth EDC 1, EDC 2, etc.) are implemented. The probability of parameters
(henceforth $P_{\text{EDC}}(\text{DALEC2}(x))$) is 1 if all EDCs are met, otherwise $P_{\text{EDC}}(\text{DALEC2}(x)) = 0$. All
DALEC2 parameters (allocation fractions $f_{\text{auto}}$, $f_{\text{lab}}$, $f_{\text{fol}}$, $f_{\text{roo}}$, $f_{\text{woo}}$; turnover rate parameters $\theta_{\text{woo}}$,
$\theta_{\text{roo}}$, $\theta_{\text{lit}}$, $\theta_{\text{min}}$, $\Theta$; canopy parameters $d_{\text{onset}}$, $d_{\text{fall}}$, $c_{\text{eff}}$, $c_{\text{max}}$, $c_{\text{lf}}$, $c_{\text{r}}$, $c_{\text{e}}$, $c_{\text{rfall}}$; carbon pools at time $t$
$C_{t\text{lab}}$, $C_{t\text{fol}}$, $C_{t\text{woo}}$, $C_{t\text{som}}$, $C_{t\text{lit}}$, $C_{t\text{som}}$) are described in Table 1.

2.2.1 Turnover Constraints

We impose the following constraints on the relative sizes of turnover rates:

EDC 1: $\theta_{\text{som}} < \theta_{\text{lit}}$, \hspace{1cm} (1)
EDC 2: $\theta_{\text{som}} < \theta_{\text{min}}$, \hspace{1cm} (2)
EDC 3: $c_{\text{lf}} > 1 - (1 - \theta_{\text{woo}})^{365.25}$, \hspace{1cm} (3)
EDC 4: $(1 - \theta_{\text{roo}})^N > \Pi_{i=1}^{N}(1 - \theta_{\text{som}} e^{\theta T_i})$, \hspace{1cm} (4)

where $T_i$ are daily temperature values during an $N$-day time window (e.g. three years). These
constraints ensure the turnover rate ratios are consistent with knowledge of the carbon pool relative
residence times (e.g. Gaudinski et al., 2000; Norby et al., 2002; Trumbore, 2006). In particular, we
expect a faster litter turnover in contrast to soil organic matter (SOM) turnover (EDC 1), a faster
conversion rate of litter to SOM relative to SOM turnover (EDC 2), the annual leaf loss fraction
is greater than the annual woody biomass loss fraction (EDC 3), and a faster fine root turnover in
contrast to SOM turnover (EDC 4).

2.2.2 Root-Foliar $C$ allocation constraints

Strong correlations are expected between foliar and fine root carbon pools (e.g. Mokany et al., 2006;
Sloan et al., 2013). We constrain the $C$ allocation and dynamics of the root and foliar pools:

EDC 5: $0.2 f_{\text{roo}} < f_{\text{fol}} + f_{\text{lab}} < 5 f_{\text{roo}}$, \hspace{1cm} (5)
EDC 6: $0.2 C_{\text{fol}}< C_{\text{roo}} < 5 C_{\text{fol}}$, \hspace{1cm} (6)

where $C_{\text{fol}}$ and $C_{\text{roo}}$ are the mean foliar and fine root carbon pool sizes over the model run period.
EDC 5 ensures that the GPP allocated fraction to $C_{\text{roo}}$ and $C_{\text{fol}}$ (directly or via the labile $C$ pool) are
within a factor of 5 of each other. EDC 6 ensures that the mean fine root and foliar pool sizes are within a factor of 5 of each other.

2.2.3 Carbon Pool Growth

While we expect pools to potentially grow through time, we assume no recent disturbance and therefore limit the relative growth rate of pools. We constrain pool growth as follows:

$$\frac{C_{\text{pool}}^{\text{year}=n}}{C_{\text{pool}}^{\text{year}=1}} < 1 + G_{\text{max}} \frac{n - 1}{10},$$

where $C_{\text{pool}}^{\text{year}=1}$ is the mean carbon pool size in year 1, and $C_{\text{pool}}^{\text{year}=n}$ is the mean carbon pool size after $n - 1$ years. We choose a value of $G_{\text{max}} = 0.1$, which is equivalent to a 10% yearly growth rate (or doubling of carbon over 10 yr) as the maximum growth rate for each pool in EDC 7. This assumption is conservative, given data on global forest biomass growth rates (Baker et al., 2004; Luyssaert et al., 2008).

2.2.4 Carbon pool exponential decay trajectories

While carbon pools are expected to grow and contract through time, in the absence of major and recent disturbance events carbon pool trajectories are expected to exhibit gradual changes on interannual timescales (e.g. Bellamy et al., 2005). Under these circumstances, rapid exponential decay in modelled DALEC2 carbon pools can only occur as a result of an ecologically inconsistent $x$. We examine the system response within a three-year period by imposing a constraint on exponential pool trajectories (Fig. 1): we numerically fit an exponential decay curve $a + be^{ct}$ to all carbon pools, where $t$ is time in days, and $a$, $b$ and $c$ are the fitted exponential decay parameters.

DALEC2 pool trajectories are rejected if the half-life of carbon pool changes is less than three years, i.e.

$$c < -\frac{365.25 \times 3}{\log(2)}$$

We fully describe the numerical derivation of $c$ in Appendix B.

2.2.5 Steady State Proximity

For ecosystems with no recent disturbance events, we propose that each pool is within an order of magnitude of its steady state attractor. We use mean gross primary production ($\overline{F}_{\text{gpp}}$) as a proxy for long-term GPP to estimate the steady state attractors, $C_{\text{pool}}^\infty$, of four carbon pools (SOM, litter, wood and root). The steady state attractors for $C_{\text{som}}$, $C_{\text{lit}}$, $C_{\text{woo}}$ and $C_{\text{roo}}$ are analytically derived as follows:

$$C_{\text{som}}^\infty = \frac{(f_{\text{woo}} + (f_{\text{tot}} + f_{\text{roo}} + f_{\text{lab}})^{\theta_{\text{min}}})\overline{F}_{\text{gpp}}}{(\theta_{\text{min}} + \theta_{\text{lit}})^{\theta_{\text{som}}}}$$

where $\theta_{\text{min}}$ is the minimum temperature for growth.
\[
\begin{align*}
C_{\text{lit}}^\infty &= \frac{(f_{\text{fol}} + f_{\text{roo}} + f_{\text{lab}}) F_{\text{gpp}}}{\theta_{\text{lit}} e^{9T}}, \\
C_{\text{woo}}^\infty &= \frac{f_{\text{woo}} F_{\text{gpp}}}{\theta_{\text{woo}}}, \\
C_{\text{roo}}^\infty &= \frac{f_{\text{roo}} F_{\text{gpp}}}{\theta_{\text{roo}}},
\end{align*}
\]

where \( T \) is the mean annual temperature (°C). For each pool, we impose an order-of-magnitude constraint on the proximity of \( C_{\text{pool}}^\infty \) from the initial \( C_{\text{pool}}^0 \) value:

EDCs 9–12: \( \frac{C_{\text{pool}}^0}{10} < C_{\text{pool}}^\infty < 10C_{\text{pool}}^0 \) (13)

where \( C_{\text{pool}}^0 \) is the initial \( C_{\text{com}}, C_{\text{lit}}, C_{\text{woo}} \) and \( C_{\text{roo}} \) value for EDCs 9, 10, 11 and 12 respectively.

The twelve presented EDCs are what we believe to be the most ecologically suitable constraints on DALEC2 parameters and state variables, and are based on broader ecological knowledge of carbon dynamics. We discuss the advantages and the limitations of the proposed EDCs in Sect. 4 of this paper.

### 2.3 Model-Data Fusion

Given LAI observations, soil organic carbon estimates, prior parameter ranges (Table 1) and EDCs (Sect. 2.2), our aim for each experiment is to estimate the probability distribution of parameters \( x \). We assume no prior knowledge, other than the parameter ranges shown in Table 1: we therefore prescribe a uniform (i.e. non-informative) prior probability distribution onto all parameters. Within a Bayesian framework (e.g. Hill et al., 2012; Ziehn et al., 2012), we combine the above-mentioned information to derive the posterior probability density function of \( x, P(x|O) \), where

\[
P(x|O) \propto P(O|x) \cdot P_{\text{range}}(x) \cdot P_{\text{EDC}}(\text{DALEC2}(x))
\]

\( P(O|x) \) is the probability of the observations given \( x \), \( P_{\text{range}}(x) = 1 \) if all parameters are within the ranges prescribed in Table 1 (otherwise \( P_{\text{range}}(x) = 0 \), and \( P_{\text{EDC}}(\text{DALEC2}(x)) = 1 \) if all EDCs are met (otherwise \( P_{\text{EDC}}(\text{DALEC2}(x)) = 0 \)). For \( N \) observations, we derive the observation probability given \( x \), \( P(O|x) \), as follows:

\[
P(O|x) = e^{-\frac{1}{2} \sum_{n=1}^{N} (M_n - O_n)^2 / \sigma_n^2},
\]

where \( O_n \) is the \( n \)th observation, \( M_n \) is the corresponding state variable, and \( \sigma_n^2 \) is the \( n \)th error variance for each observation (e.g. Xu et al., 2006): here we assume no error covariance between observation errors.

We employ an adaptive Metropolis Hastings Markov Chain Monte Carlo (MHMCMC) approach to draw \( 5 \times 10^6 \) samples from \( P(x|O) \). This approach has been widely used to estimate the probability density function of ecosystem model parameters (Xu et al., 2006; Hill et al., 2012; Ziehn et al.,
2012; Caldararu et al., 2012; Smith et al., 2013; Keenan et al., 2013, amongst others) and is ideal to explore parameter space without a need to define normal prior distributions for each parameter (e.g. Richardson et al., 2010). We repeat the MHMCMC algorithm four times (i.e. four chains), to ensure convergence between $P(x|O)$ distributions from each chain. To minimise sample correlations we use 500 $x$ samples from the latter half of the accepted parameter vectors. We describe the details of our MHMCMC approach in Appendix C.

2.4 Synthetic truth – DALEC2 analyses

To quantify our ability to estimate synthetic DALEC2 ecosystem states, we perform the MDF approach over a three year period using LAI and SOM observations created from a synthetic DALEC2 truth, based on known DALEC2 parameters. Our choice of synthetic DALEC2 states represents globally spanning datasets of satellite LAI retrievals and soil carbon map data. Based on 40 DALEC2 parameter combinations, we create 40 synthetic datasets representing typical temperate forest carbon dynamics, with three years of semi-continuous LAI data and one simulated soil organic carbon estimate. We use the three-year meteorology drivers (temperate climate) from the REFLEX synthetic experiments (Fox et al., 2009).

We select 40 synthetic parameter combinations by randomly sampling parameter vectors $x$ within the DALEC2 parameter space (Table 1), where (i) $P_{EDC}(DALEC2(x)) = 1$, and (ii) $x$ values are relevant to temperate forest ecosystems (see Appendix D). We remove approximately 95% of daily LAI points to create an 8 day resolution semi-continuous LAI time-series. We add noise to the remaining 3 yr synthetic DALEC2 LAI: each LAI value is multiplied by a random error factor of $2^{N(0,1)}$, where $N(0,1)$ is a random number derived from a normal distribution with a mean of zero and a standard deviation of 1. For each synthetic soil carbon observation, we multiply $C_{0,som}^t$ at $t = 0$ by a random error factor of $2^{N(0,1)}$. We fully explain the derivation of the synthetic experiment parameter vectors, (henceforth $s$) in Appendix D.

We perform the MHMCMC and label the posterior parameter ensemble ($4 \times 500 \times 40 \times x$ samples) as $x_{s\, STA}$ (standard synthetic MDF) and $x_{s\, EDC}$ (synthetic MDF with EDCs). We assign an uncertainty factor of 2 to all synthetic observations, hence $O_n$ and $M_n$ are log-transformed observations and $\sigma_n = \log(2)$. For each posterior DALEC2 $x$, we determine the log-normalised parameter-space error $\epsilon(x)$ by comparing $x$ with its corresponding synthetic truth vector $s$:

$$
\epsilon(x) = \sqrt{\frac{\sum_{n=1}^{N} \frac{\log(x(n)) - \log(s(n))}{\log(x(n)_{max}) - \log(x(n)_{min})}^2}{\sqrt{N}}} \tag{16}
$$

where $x(n)$ and $s(n)$ represent the $n$th parameters of $x$ and $s$, $N$ is the number of parameters in $x$, and $x(n)_{min}$, $x(n)_{max}$ are the minimum and maximum parameter values (see Table 1). To assess the parameter estimation capability for each experiment, we derive the $\epsilon(x)$ for each parameter vector in (a) $x_{s\, STA}$ (b) $x_{s\, EDC}$ and (c) for uniformly random samples where $P_{range}(x) = 1$ (henceforth $x_{s\, RAN}$).
We refer to the ensemble of $\epsilon(x)$ values for $xs_{STA}$, $xs_{EDC}$ and $xs_{RAN}$ as $E(xs_{STA})$, $E(xs_{EDC})$ and $E(xs_{RAN})$. We quantify the overall EDC associated error reduction ($I_{EDC}$) as follows:

$$I_{EDC} = \left( \frac{\tilde{E}(xs_{RAN}) - \tilde{E}(xs_{EDC})}{\tilde{E}(xs_{RAN}) - \tilde{E}(xs_{STA})} - 1 \right) \times 100\%$$

where $\tilde{E}$ represents the median of $E$ for each posterior parameter ensemble. This allows us to assess the relative improvement of $xs_{EDC}$ over $xs_{STA}$ parameter estimates against the $xs_{RAN}$ “zero-knowledge” case. In addition, we determine the $I_{EDC}$ for two parameter subgroups: (a) directly constrained parameters, and (b) indirectly constrained parameters. We assign $c_{lf}$, $c_{ronset}$, $c_{rfall}$, $d_{onset}$ and $C_{som}^0$ to parameter group A: these parameters can be directly inferred from the LAI and soil organic carbon observations. We assign the remaining parameters to parameter group B: these can only be inferred from the DALEC2 model structure and – potentially – EDCs. Finally we compare NEE from DALEC2($xs_{EDC}$) and DALEC2($xs_{STA}$) against the NEE synthetic “truths” –

2.5 AmeriFlux – DALEC2 analyses

For the flux-tower experiments, we constrain DALEC2 parameters using (a) MODIS derived Leaf Area Index (LAI), and (b) total soil carbon from the harmonised world soil database (HWSD Hiederer and Köchy, 2011). We perform daily resolution three year DALEC2 analyses for three forest categories: evergreen needle-leaf (ENF), deciduous broad-leaf (DBF), and mixed forest (MF). We chose one AmeriFlux site from each forest type. To establish a suitable site for our method we chose sites with NEE data spanning across three years between 2001 and 2010. Our selected sites for each forest type are Howland Forest (US-Ho1, evergreen needleleaf forest – 45.2041° N, 68.7402° W – Hollinger et al., 1999), Morgan Monroe State Forest (US-MMS, deciduous broadleaf forest – 39.3231° N, 86.4131°W – Schmid et al., 2000) and Sylvania Wilderness (US-Syv, mixed forest – 46.2420° N, 89.3476° W – Desai et al., 2005). We chose temperate sites with little expected water-stress, and with a $\leq 3$ months of recorded below-freezing soil temperatures. These criteria reflect the current capabilities of DALEC2, as hydrological processes are not explicitly portrayed in the model.

For each AmeriFlux site, we extract the corresponding MODIS LAI retrievals from the MOD15A2 LAI 8 day version 005 1 km resolution product (downloaded from the Land Processes Distributed Active Archive Centre http://lpdaac.usgs.gov/): we only keep maximum quality flag data. Standard deviations are provided for 1 km MODIS LAI retrievals, however these (a) do not reflect the magnitude variability in uncertainty, (b) often imply the existence of negative LAI observations ($\sigma_{LAI} > \text{LAI}$) and (c) are occasionally missing. While various MODIS LAI evaluations have been performed (e.g. Sea et al., 2011; Serbin et al., 2013), large-scale spatiotemporal LAI retrieval errors remain poorly quantified. For the sake of simplicity, we assign a factor of 2 uncertainty (i.e. $\log(\text{LAI}) \pm \log(2)$) for each MODIS LAI observation. To minimise spatial discrepancies between
MODIS and AmeriFlux sites, each LAI observation is the arithmetic mean of all available LAI retrievals within a 9 pixel $3\text{ km} \times 3\text{ km}$ area (centred on each AmeriFlux site). Overall, we use 95, 120 and 119 LAI values at US-Syv, US-Ho1 and US-MMS (5th–95th percentile ranges for LAI values are 0.4–5.8, 1.0–5.6 and 0.4–5.5 respectively).

For each site we extract total soil carbon density from the nearest Harmonised World Soil Database 30 arc seconds resolution total soil carbon content (approx. 1 km at equator Hiederer and Köchy, 2011): the authors have performed multiple comparisons of the global HWSD against other products, however no pixel-scale uncertainties are provided. We chose to assign an uncertainty factor of 2 on each site-scale HWSD SOC estimate. The HWSD SOC values are $2.3 \times 10^4 \text{ g C m}^{-2}$, $2.3 \times 10^4 \text{ g C m}^{-2}$ and $5.2 \times 10^3 \text{ g C m}^{-2}$.

To limit our study to the use of globally spanning datasets, we extract DALEC2 drivers from $0.125^\circ \times 0.125^\circ$ ERA interim meteorology (see Appendix A for details). The DALEC2 analyses for each site are therefore completely independent from all site-level measurements (we note, however, that extensive meteorological and biometric data are meticulously recorded across the AmeriFlux site network). Therefore, we produce a fully independent ecosystem carbon cycle analysis, which can be evaluated against measured NEE at each flux-tower site.

As done for the synthetic experiments, we perform the MHMCMC approach at each site – with and without EDCs – and label the posterior parameter ensembles (4 chains $\times$ 500 $x$ samples) as $xa_{\text{STA}}$ (standard AmeriFlux MDF) and $xa_{\text{EDC}}$ (AmeriFlux MDF + EDCs). We compare the DALEC2 NEE analyses, DALEC2($xa_{\text{EDC}}$) and DALEC2($xa_{\text{STA}}$) against NEE measurements at each AmeriFlux site.

### 2.6 EDC sensitivity test

To determine the sensitivity of our results to EDCs 1-12, we repeat MDF estimates of $xs_{\text{EDC}}$ and $xa_{\text{EDC}}$ by imposing only one EDC at a time (henceforth $xs_{\text{EDC}(n)}$ and $xa_{\text{EDC}(n)}$, where $n$ is the $n$th EDC). For the synthetic experiments, we determine the relative contribution of the $n$th EDC by quantifying the overall EDC associated error reduction ($I_{\text{EDC}(n)}$, see equation 17) for each estimate of $xs_{\text{EDC}(n)}$. Given the large computational cost of estimating $xs_{\text{EDC}(n)}$ for each EDC (40 synthetic experiments $\times$ 12 EDCs $\times$ 4 chains), we limit our sensitivity analysis to $I_{\text{EDC}}$ estimates based on 4 (out of 40) synthetic experiments.

We compare 3 yr integrated DALEC2 NEE estimates and AmeriFlux NEE measurements at all three sites (AmeriFlux NEE measurement temporal gaps have been consistently excluded from DALEC2 3 yr NEE estimates). We determine the DALEC2 3 yr NEE 50% confidence range (50% CR: 25th–75th percentile interval) reduction as follows:

$$\left(1 - \frac{R_{\text{NEE,EDC}(n)}}{R_{\text{NEE,STA}}} \right) \times 100\%$$

(18)
where \( R_{\text{NEE,EDC}(n)} \) and \( R_{\text{NEE,STA}} \) are the 50% CR of DALEC2(\( x_a^{\text{EDC}(n)} \)) and DALEC2(\( x_a^{\text{STA}} \)) 3 yr NEE estimates. Similarly, we calculate the 3 yr NEE bias reduction (relative to AmeriFlux NEE measurements) as follows:

\[
(1 - \frac{|B_{\text{NEE,EDC}(n)}|}{|B_{\text{NEE,STA}}|}) \times 100% \tag{19}
\]

where \( B_{\text{NEE,EDC}(n)} \) and \( B_{\text{NEE,STA}} \) are the median biases of DALEC2(\( x_a^{\text{EDC}(n)} \)) and DALEC2(\( x_a^{\text{STA}} \)) 3 yr NEE estimates.

3 Results

3.1 Synthetic Experiments

The inclusion of EDCs resulted in substantial error reductions in posterior DALEC2 parameter and state variable estimates. We found an overall reduction in the posterior MHMCMC EDC parameter vector errors \( E(\text{xs}^{\text{EDC}}) \), relative to both the standard MHMCMC errors \( E(\text{xs}^{\text{STA}}) \) and the randomly sampled parameter vector errors \( E(\text{xs}^{\text{RAN}}) \): we found an improvement of \( I_{\text{EDC}} = 34\% \) associated with using EDCs (Fig. 2c). For the directly constrained parameters (parameter group A) we found similar distributions for both \( E(\text{xs}^{\text{STA}}) \) and \( E(\text{xs}^{\text{EDC}}) \) errors relative to \( E(\text{xs}^{\text{RAN}}) \) errors (Fig. 2a), and similarly lower \( \text{xs}^{\text{STA}} \) and \( \text{xs}^{\text{EDC}} \) errors values relative to \( \text{xs}^{\text{RAN}} \) errors (\( \tilde{E}(\text{xs}^{\text{STA}}) = 0.19, \tilde{E}(\text{xs}^{\text{EDC}}) = 0.21, \tilde{E}(\text{xs}^{\text{RAN}}) = 0.42, \) group A: \( I_{\text{EDC}} = -6\% \)). For the indirectly constrained parameters (group B), we found significantly smaller \( \text{xs}^{\text{EDC}} \) errors relative to \( \text{xs}^{\text{STA}} \) and \( \text{xs}^{\text{RAN}} \) (\( \tilde{E}(\text{xs}^{\text{EDC}}) = 0.29, \tilde{E}(\text{xs}^{\text{STA}}) = 0.34, \) and \( \tilde{E}(\text{xs}^{\text{RAN}}) = 0.38 \)), and hence improved estimates of \( s \) when we implemented EDCs (group B: \( I_{\text{EDC}} = 88\% \), Fig. 2b). We found that EDCs 5 and 8 accounted for the largest error reduction in DALEC2 parameter estimates (\( I_{\text{EDC}(5,8)} \geq 3\% \), Table 2), followed by EDCs 6, 10 and 12 (\( I_{\text{EDC}(6,10,12)} = 2\% \)). EDC 7 led to an overall parameter error increase (\( I_{\text{EDC}(7)} = -13\% \)). The remaining EDCs accounted for small or negative error reductions.

We compared EDC total \( \text{xs}^{\text{EDC}}, \text{xs}^{\text{STA}} \) and \( \text{xs}^{\text{RAN}} \) live biomass (\( C_{\text{roo}} + C_{\text{fol}} + C_{\text{lab}} + C_{\text{woo}} \)) and dead biomass (\( C_{\text{som}} + C_{\text{lit}} \)) pool biases relative to their corresponding synthetic truths (Fig. 2d–e). For dead biomass, both \( \text{xs}^{\text{EDC}} \) and \( \text{xs}^{\text{STA}} \) perform comparably better than \( \text{xs}^{\text{RAN}} \) (Fig. 2e), as dead biomass is mostly accounted for by the synthetic \( C_{\text{som}} \) observations: the median bias factors (1.1, 0.91) are close to 1 (i.e. a bias of zero) relative to \( \text{xs}^{\text{RAN}} \) median bias factor (0.04). For live biomass pools, \( \text{xs}^{\text{EDC}} \) live biomass bias estimates are smaller than \( \text{xs}^{\text{STA}} \) (Fig. 2d): the \( \text{xs}^{\text{EDC}} \) bias distribution (median = 1.20) is closer to 1 relative to the \( \text{xs}^{\text{STA}} \) bias distribution (0.48), with respect to \( \text{xs}^{\text{RAN}} \) median bias (0.20). For total biomass estimates, we found similar bias distributions relative to \( \text{xs}^{\text{RAN}} \): (\( \text{xs}^{\text{EDC}} \) median bias factor = 1.22, \( \text{xs}^{\text{STA}} \) bias factor = 0.98): both bias factors are closer to 1 relative to \( \text{xs}^{\text{RAN}} \) (bias factor = 0.16).

We found that incorporating EDCs resulted in a reduced mode and 90% confidence range
(90% CR: 95th–5th percentile interval) for three year NEE biases (Fig. 3). We found a 65% reduc-

tion in the DALEC2($x_{sEDC}$) three year NEE bias 90% CR ($9.0 \text{ g C m}^{-2} \text{d}^{-1}$), relative to the

daDALEC2($x_{sSTA}$) three year NEE bias 90% CR ($26.9 \text{ g C m}^{-2} \text{d}^{-1}$). The three year NEE bias

trends for DALEC2($x_{sEDC}$) and DALEC2($x_{sSTA}$) are $0.0 \text{ g C m}^{-2} \text{d}^{-1}$ and $-0.5 \text{ g C m}^{-2} \text{d}^{-1}$ (at

365

0.5 g $\text{C m}^{-2} \text{d}^{-1}$ intervals).

3.2 AmeriFlux results

The DALEC2($x_{aEDC}$) analyses outperformed the standard DALEC2($x_{aSTA}$) analyses at the Ameri-

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Flux tower sites. The inclusion of EDCs in DALEC2 analyses amounted to overall NEE bias re-

ductions at all sites (US-Syv, US-Ho1, US-MMS, we henceforth present all site results in this or-

der). The aggregated DALEC2($x_{aEDC}$) median daily NEE biases ($-0.02, 0.13, -0.03 \text{ g C m}^{-2} \text{d}^{-1}$)

are closer to the AmeriFlux measured NEE by roughly one order of magnitude in contrast to

DALEC2($x_{aSTA}$) median NEE biases ($-0.52, -0.86, -1.15 \text{ g C m}^{-2} \text{d}^{-1}$). The aggregated daily

DALEC2($x_{aEDC}$) NEE 90% confidence ranges at each site (10.9, 10.1, 8.3 $\text{ g C m}^{-2} \text{d}^{-1}$) were

all smaller (53–87%) than the corresponding DALEC2($x_{aSTA}$) NEE bias 90% CR (20.3, 18.3,

375 9.5 $\text{ g C m}^{-2} \text{d}^{-1}$). The reductions in bias are consistent across the three year comparison period at

each site (Fig. 4).

Cumulative AmeriFlux NEE observations are compared against corresponding DALEC2($x_{aSTA}$) and

DALEC2($x_{aEDC}$) NEE estimates (Fig. 5); AmeriFlux NEE temporal gaps have been omitted from both DALEC2 and AmeriFlux derived cumulative NEE time series. DALEC2($x_{aEDC}$)

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integrated NEE estimates outperformed DALEC2($x_{aSTA}$) NEE estimates at all three sites.

DALEC2($x_{aEDC}$) median NEE biases over the 3 yr period ($-0.26, 0.07, 0.08 \text{ kg C m}^{-2}$) are smaller

than the equivalent DALEC2($x_{aSTA}$) biases ($-0.84, -1.09, -1.18 \text{ kg C m}^{-2}$), with relative EDC bias reductions of 69%, 93% and 93%. The inclusion of EDCs also resulted in a reduction in NEE confidence intervals: DALEC2($x_{aEDC}$) 50% CR (1.17, 1.57, 1.16 $\text{ kg C m}^{-2}$) are 32–48% smaller than the corresponding DALEC2($x_{aSTA}$) 50% CR (2.04, 3.00, 1.70 $\text{ kg C m}^{-2}$). Based on

DALEC2($x_{aEDC(n)}$) 3 yr NEE estimates, EDC 10 resulted in a $\geq 18\%$ bias reduction and a $\geq 5\%$

385 50% CR reduction at all three sites, relative to DALEC2($x_{aSTA}$) (Table 2). EDCs 2 and 8 resulted in

a $> 10\%$ 3 yr NEE 50% CR reduction and an increase in 3 yr NEE bias at all three sites (NEE bias

reduction $\leq -22\%$). EDCs 7 and 9 resulted in a $\geq 50\%$ 3 yr NEE bias reduction and an increase in

390 3 yr NEE 50% CR at all three sites (NEE 50% CR reduction $\leq -15\%$).

4 Discussion

With the use of a simple model and globally available data, i.e. leaf area dynamics and soil carbon

observations, we have demonstrated that the EDC approach provides an improved ability to infer the

magnitude of carbon fluxes, live carbon pools and model parameters, in comparison to a standard
parameter optimisation approach (STA).

For ecologically relevant synthetic truths, EDCs provide improved estimates of the DALEC2 parameters and state variables. The EDC approach resulted in (a) parameter estimation error reductions, (b) NEE bias and confidence range reductions, and (c) improved estimates of the live biomass C pools, in contrast to the STA parameter and flux and C pool estimates. While there is little difference between directly inferable (Group A) estimated parameter errors between the EDC and STA approach, using EDCs led to a marked reduction in estimated parameter error for indirectly inferable (Group B) parameters. The indirectly inferred parameters include allocation fractions, subsurface pools and turnover rates, which are typically difficult to observe at field sites and virtually impossible to observe remotely (i.e. at regional scales).

By comparing DALEC2 analyses against independent AmeriFlux NEE measurements over real ecosystems, we further validated the advantages of using EDCs. At each AmeriFlux site, we found that EDCs led to an increased confidence and a largely reduced NEE bias; our DALEC2 model analyses suggests that the use of EDCs regionally and globally could significantly enhance our ability to estimate ecosystem state variables in the absence of direct observational constraints. In light of the large differences between earth system models (Todd-Brown et al., 2013; Friend et al., 2013), we anticipate that EDCs may help constrain ecosystem carbon terms on global scales, where carbon pools and their residence times are typically difficult or impossible to measure.

Together, EDCs 1-12 lead to overall improvements in parameter estimates and AmeriFlux site NEE confidence range/bias (Table 2): however, with the exception of EDC 10, when EDCs were tested individually, they did not lead to comprehensive improvements. For example, EDC 8 alone (no rapid exponential pool decay) resulted in large AmeriFlux site NEE confidence range reductions, as well as improved synthetic parameter estimates; however, EDC 8 resulted in higher AmeriFlux site NEE biases. Conversely, EDC 9 (steady state proximity of the soil carbon pool) resulted in the largest AmeriFlux site bias reductions, while NEE confidence was lower. EDC 5 (comparable fine root and foliar/labile allocation) led to the largest parameter improvements; however, the associated changes in AmeriFlux site NEE estimates were relatively small. Our findings demonstrate that robust improvements in carbon cycling parameter and state variable estimates only arise when EDCs are used collectively.

Here we developed a group of EDCs suitable to ecosystems with no recent major disturbance. However, we note that our EDCs can be adapted for a wider range of ecosystem dynamics. For example, recently disturbed ecosystems may be (a) rapidly recovering and (b) growing towards a steady state where carbon pools are greater than one order of magnitude from the initial carbon pools. Therefore a subset of our EDCs (EDCs 7–12) can be adapted to better represent ecological “common sense” in recovering ecosystems.

Ultimately, EDCs can be adapted to best represent ecological knowledge in a variety of ecosystem carbon model MDF applications, where the ecosystem observations are insufficient to constrain all
model state variables (e.g. Fox et al., 2009). For example, on regional and global spatial scales, there is often no explicit knowledge on various model parameter values and their associated uncertainty. In such cases, our EDC approach imposes inter-parameter constraints while simultaneously allowing a global parameter exploration across several orders of magnitude (see Table 1). Hence EDCs allow us to incorporate ecologically consistent relationships between parameters (i.e. allocation ratios, turnover ratios), without the need to constrain otherwise unknown parameter and state variables. Moreover, as an alternative to imposing plant-functional-type priors, which risk being subjective and over-rigid, ecosystem trait inter-relationships derived from plant trait data (e.g. Wright et al., 2004; Kattge et al., 2011) could be incorporated as additional EDCs. Given a quantitative knowledge of parameter inter-relationships, we also note that a prior parameter variance-covariance structure – in addition to EDCs – can also be used as an alternative or complementary constraint on the model state and parameters. Finally, we note that our choice of EDCs is open to adaptation and adjustment: we maintained relatively broad constraints (e.g. EDC 6 permissible root:foliar C range > one order of magnitude), which can likely be refined through further study.

In this study we limited our observational constraints to globally spanning MODIS LAI retrievals and the HWSD soil map. Given these two datasets, we have demonstrated that EDCs lead to improved model parameter estimates and reduced NEE bias and confidence ranges. Nonetheless, based on the posterior NEE probability density function, we are unable to determine whether sites are net carbon sinks or sources on annual timescales. However, an increasing number of continental and global scale biospheric datasets are becoming available: these include a global canopy height map by Simard et al. (2011), pan-tropical biomass maps by Saatchi et al. (2011); Baccini et al. (2012) and a pan-boreal carbon density map by Thurner et al. (2013). These products can potentially be used in conjunction with MODIS LAI, HWSD data and our EDC approach in a MDF framework to better constrain terrestrial carbon cycle dynamics.

5 Concluding Remarks

We have addressed the under-determined nature of the carbon cycle problem by applying a group of widely applicable ecological and dynamic constraints (EDCs) on an ecosystem carbon model in a model-data fusion (MDF) framework. Particularly where extensive in-situ measurements are not available, EDCs can be used to incorporate ecological knowledge, such as parameter inter-relationships and pool dynamics constraints, into ecosystem carbon model analyses. In a synthetic data experiment, we found improved estimates of DALEC2 model parameters, live carbon pools and net ecosystem exchange (NEE) when using EDCs in DALEC2 MDF analyses. By validating our DALEC2 MDF analyses against independent AmeriFlux NEE measurements, we found that EDCs led to a 69–93 % reduction in three year NEE biases. We incorporated twelve EDCs in DALEC2 analyses of temperate forest ecosystem carbon cycling: these EDCs can potentially be adapted for
a range of models and biomes. Moreover, additional EDCs can be derived to incorporate parameter inter-relationships derived from regional or global plant trait datasets into ecosystem carbon model analyses. Here we have shown that EDCs can be used to constrain the poorly resolved components of the carbon cycle: we therefore advocate the use of EDCs in future MDF analyses of the terrestrial carbon cycle.

Appendix A

DALEC2 model

The full DALEC2 model dynamics can be expressed as six equations:

\[
C_{\text{lab}}^{t+1} = (1 - \Phi_{\text{onset}}(t, d_{\text{onset}}, c_{\text{onset}}))C_{\text{lab}}^t + f_{\text{lab}}F_{\text{gpp}}^t
\]  \tag{A1}

\[
C_{\text{fol}}^{t+1} = (1 - \Phi_{\text{fall}}(t, d_{\text{fall}}, c_{\text{fall}}, c_{\text{span}}))C_{\text{fol}}^t + \Phi_{\text{onset}}(t, d_{\text{onset}}, c_{\text{onset}})C_{\text{lab}}^t + f_{\text{fol}}F_{\text{gpp}}^t
\]  \tag{A2}

\[
C_{\text{roo}}^{t+1} = (1 - \theta_{\text{roo}})C_{\text{roo}}^t + f_{\text{roo}}F_{\text{gpp}}^t
\]  \tag{A3}

\[
C_{\text{woo}}^{t+1} = (1 - \theta_{\text{woo}})C_{\text{woo}}^t + f_{\text{woo}}F_{\text{gpp}}^t
\]  \tag{A4}

\[
C_{\text{lit}}^{t+1} = (1 - (\theta_{\text{lit}} + \theta_{\text{min}})e^{\psi_f T_{t,d}})C_{\text{lit}}^t + \theta_{\text{roo}}C_{\text{roo}}^t + \Phi_{\text{fall}}(t, d_{\text{fall}}, c_{\text{fall}}, c_{\text{span}})C_{\text{fol}}^t
\]  \tag{A5}

\[
C_{\text{som}}^{t+1} = (1 - \theta_{\text{som}}e^{\psi_f T_{t,d}})C_{\text{som}}^t + \theta_{\text{woo}}C_{\text{woo}}^t + (\theta_{\text{min}})e^{\psi_f T_{t,d}}C_{\text{lit}}^t
\]  \tag{A6}

The 23 free parameters and carbon pool symbols are summarised in Table 1. The daily gross primary production \(F_{\text{gpp}}^t\), is derived from the aggregated canopy model (ACM, Williams et al., 1997), and is a function of daily driver data \(M\) (day of year, atmospheric \(\text{CO}_2\), minimum and maximum temperature, and global radiation), and parameters \(C_{\text{fol}}, c_{\text{ima}}\) and \(c_{\text{eff}}\) (parameter \(c_{\text{eff}}\), the canopy efficiency, is a replacement for the nitrogen \(\times\) nitrogen use efficiency product in ACM).

The model is initiated with six initial carbon pool values \((C_{\text{lab}}^0, C_{\text{fol}}^0, C_{\text{roo}}^0, C_{\text{woo}}^0, C_{\text{lit}}^0, C_{\text{som}}^0)\) and these are iteratively updated at a daily timestep. The leaf onset (labial to foliar pool \(C\) transfer) and leaf fall (foliar to litter pool \(C\) transfer) functions, \(\Phi_{\text{onset}}\) and \(\Phi_{\text{fall}}\) are defined below:

\[
\Phi_{\text{onset}}(t, d_{\text{onset}}, c_{\text{onset}}) = \frac{\sqrt{2}}{\sqrt{\pi}} \cdot \frac{6.9088}{c_{\text{onset}}} \cdot e^{-\left(\frac{1}{2}\frac{d_{\text{onset}} - 0.6245c_{\text{onset}}}{c_{\text{onset}}^2}\right)^2}
\]  \tag{A7}

\[
\Phi_{\text{fall}}(t, d_{\text{fall}}, c_{\text{fall}}, c_{\text{span}}) = \frac{\sqrt{2}}{\sqrt{\pi}} \cdot \frac{\log(c_{\text{span}}) - \log(c_{\text{span}} - 1)}{c_{\text{fall}}} \cdot e^{-\left(\frac{1}{2}\frac{c_{\text{fall}} - 0.6245c_{\text{fall}}}{c_{\text{fall}}^2}\right)^2}
\]  \tag{A8}

The \(\Phi_{\text{fall}}\) continuous cyclical step function derivatives were derived such that (a) \(\prod_{t=1}^{t=365} (1 - \Phi_{\text{onset}}(t, d_{\text{onset}}, c_{\text{onset}})) = 1 - \frac{1}{c_{\text{fall}}}\) (b) the maximum leaf loss rate occurs annually at \(t\% \text{365.25} = d_{\text{fall}}\). (c) 68\% of leaf loss occurs within \(c_{\text{onset}}\) days and 95\% of leaf loss within \(2c_{\text{fall}}\) days.

\(\psi_f\) is an offset term included to ensure that the maximum leaf loss rate, i.e. \(\frac{d^2C_{\text{lit}}}{dt^2} = 0\), occurs at \(t\% \text{365.25} = d_{\text{fall}}\) - it is a numerical solution to the following equation:

\[
2\sqrt{\pi} \cdot \log\left(\frac{c_{\text{span}}}{c_{\text{span}} - 1}\right) \cdot \psi + e^{-\psi^2} = 0.
\]  \tag{A9}
where $\psi = \sqrt{2} \frac{\psi_f}{c_{\text{out}}}$ (we note that Eq. (A9) can be solved using a Lambert W function, where $\psi = W(f(c_{\text{lt}}))$ - however, Lambert W functions cannot be solved analytically). We created a look up function for $\psi$ by fitting a 6th order polynomial between $\psi$ and $\log(c_{\text{lt}} - 1)$ – the full polynomial is included in the downloadable DALEC2 code. $\Phi_{\text{onset}}$ is a special case of the $\Phi_{\text{fall}}$ formula: it was derived such that 99.99% of $C_{\text{lab}}$ is transferred to $C_{\text{fol}}$ annually at $t\%365.25 = d_{\text{onset}}$ and 68% of leaf onset occurs within $c_{\text{onset}}$ day. The $\Phi$ functions are advantageous in that (a) the daily turnover rates result in a continuous and specified loss of carbon throughout a known time period, and (b) the functions are cyclical and hence do not need to be reset, “switched on” or “switched off” throughout the model run period. We also note that while we treated $d_{\text{onset}}$ and $d_{\text{fall}}$ as constant parameters, the $\Phi$ functions can easily accommodate temporally variable definitions for leaf onset and leaf fall. Total ecosystem respiration $F_{\text{rec}}^t$ and the net ecosystem exchange $F_{\text{nee}}^t$ fluxes are derived at each timestep and are shown below.

\[
F_{\text{rec}}^t = f_{\text{auto}} F_{\text{gpp}} + (\theta_{\text{lit}} C_{\text{lit}} + \theta_{\text{som}} C_{\text{som}}) e^{\Theta T_t} \tag{A10}
\]

\[
F_{\text{nee}}^t = F_{\text{rec}}^t - F_{\text{gpp}}^t \tag{A11}
\]

At time $t$ leaf area index (LAI) is defined as:

\[
\text{LAI}^t = \frac{C_{\text{fol}}^t}{c_{\text{ma}}} \tag{A12}
\]

A schematic of the of the carbon fluxes in DALEC2 is shown in Fig. 6.

For AmeriFlux DALEC2 analyses we used daily meteorological drivers for DALEC2 from 0.125° × 0.125° ERA-interim re-analyses. For each site we obtained coordinates from ameriflux.ornl.gov. We downloaded 6 h temperature and 12 h downward surface solar radiation data for all site locations and years from apps.ecmwf.int/datasets. We averaged temperature and radiation from the four nearest 0.125° × 0.125° ERA-interim grid-points. We obtained minimum and maximum temperatures from the 6 h ERA-interim temperature range. For $M$ daily radiation values we used the sum of the two 12 h radiation re-analyses.

**Appendix B**

**Exponential $C_{\text{pool}}$ decay**

Expontially decaying $C_{\text{pool}}^t$ trajectories can be approximated as $C_{\text{exp}}^t = a + be^{ct}$, where $a$, $b$ and $c$ are constants, $t$ is time in days. To implement EDC 8, we numerically estimate parameter $c$: to derive $c$ for each carbon pool trajectory ($C_{\text{pool}}$) we derive (i) the gradient between yearly means for years 1 and 2:

\[
\Delta C_0 = \frac{\sum_{t=365+1}^{365 \times 2} C_{\text{pool}}^t - \sum_{t=1}^{365} C_{\text{pool}}^t}{365} \tag{B1}
\]
and (ii) the gradient between the yearly means with a 1 day offset:

$$\Delta C_1 = \frac{365 \times 2 + 1}{365} \left[ \sum_{t=365+1}^{365+1} C_{\text{pool}}^t - \sum_{t=1+1}^{3=1+1} C_{\text{pool}}^t \right]$$

(B2)

Parameter $c$ can be expressed as:

$$c = \log(\frac{\Delta C_1}{\Delta C_0})$$

(B3)

In the case of a true exponential curve with a known value of $c$, the numeric derivation of $c$ shown in equations B1–B3 is exact (i.e. within numerical precision of the true $c$). In cases where there is no exponential decay, $c$ is either positive or complex. While $C_{\text{exp}}$ is an approximation of $C_{\text{pool}}^t$, in practice this approach is both computationally fast and effectively able to identify rapid exponential decay ($c < \frac{\log(2)}{365 \times 2 + 1}$) trajectories.

**Appendix C**

Adaptive MHMCMC algorithm

For the standard MDF parameter estimates the normalised parameter probability is:

$$P(x|O) = \alpha \cdot P(O|x) \cdot P_{\text{range}}(x),$$

(C1)

and for EDC MDF parameter estimates the normalised parameter probability is:

$$P(x|O) = \alpha \cdot P(O|x) \cdot P_{\text{range}}(x) \cdot P_{\text{EDC}}(\text{DALEC2}(x)),$$

(C2)

where $\alpha$ is a scaling constant ensuring $\int P(x|O) dx = 1$. For each chain, we search for a random $x_0$ starting point where $P_{\text{range}}(x_0) \cdot P_{\text{EDC}}(\text{DALEC2}(x_0)) = 1$ (for standard runs we randomly sample $x_0$ from $P_{\text{range}}(x_0) = 1$).

Based on the Ziehn et al. (2012) algorithm, we then iterate through the following steps:

1. $x_{i+1} = x_i + d$.
2. Run DALEC2($x_{i+1}$).
3. If $\frac{P(x_{i+1}|O)}{P(x_i|O)} > U(0, 1)$, accept $x_{i+1}$, and $i = i + 1$.

where $d$ is the stepsize. The ratio $\frac{P(x_{i+1}|O)}{P(x_i|O)}$ is derived from equations C1 and C2 for standard and EDC MHMCMC iterations, respectively (therefore knowledge of $\alpha$ is not required). At each iteration, for each parameter dimension $n$, $d(n) = s(n)N(0, 1)$, where $s$ is the proposal distribution and $N(0, 1)$ is a random number sampled from a normal distribution with mean = 0 and variance = 1. This sequence repeated until $10^7$ samples of $x$ have been accepted. While any proposal distribution
s can be used, adapting the proposal distribution can reduce the number of steps required to reach the maximum probability parameter space. For the first $5 \times 10^6$ samples, we adapt the proposal distribution $s$ every 100 iterations by (i) scaling $s$ to ensure an acceptance rate of 23–44% (Ziehn et al., 2012), and (ii) scale individual dimensions of $s$ to ensure that $2s_n > \sigma_x(n)$ where $\sigma_x(n)$ is the $n$th parameter standard deviation over 100 iterations. The $P(\mathbf{x}|\mathbf{O})$ distribution is then derived from the second $5 \times 10^6$ samples.

The MHMCMC parameter sampling approach is then repeated four times (four chains): to determine whether all four chains have converged to the same parameter distributions, we use the Gelman-Rubin convergence criterion $R$, where for each parameter $R < 1.1$ indicates an acceptable chain convergence (Gelman and Rubin, 1992; Xu et al., 2006). If the chains have not converged for all parameters, we sequentially test all $N$ chain combinations (where $N \geq 2$) to (a) repeat the GR criterion, and (b) determine the combination with the maximum number of converged chains.

Appendix D

Temperate forest synthetic truths

The 40 synthetic experiments were created by searching for parameter vectors $s$ where $P_{EDC}(DALEC2(s)) = 1$. To create synthetic experiments parameter vectors $s$ relevant to temperate forest ecosystems - henceforth $P_{TF}(DALEC2(s)) = 1$ - we imposed the following parameter and state variable conditions:

1. $60 < d_{onset} < 150$
2. $242 < d_{fall} < 332$
3. $c_{onset} > 20$
4. $c_{fall} > 30$
5. $c_{lf} > 0.25$
6. $1 < \text{LAI} < 8$
7. $3 \text{kg C m}^{-2} < C_{w0}^0 < 30 \text{kg C m}^{-2}$
8. $1 \text{kg C m}^{-2} < C_{som}^0 < 100 \text{kg C m}^{-2}$
9. $F_{gpp}^T > 2 \text{g C m}^{-2} \text{d}^{-1}$
10. $\frac{5}{6} < \frac{\text{LAI}_{year=2}}{\text{LAI}_{year=1}} < \frac{6}{5}$
For a given vector \( s \), all conditions must be met when \( P_{TF}(\text{DALEC2}(s)) = 1 \). The above-listed conditions ensure that the selected \( s \) vectors broadly reflect canopy dynamics (1–4), carbon pool sizes (5–6) mean photosynthetic uptake (7) and limited year-to-year canopy changes (8) associated with temperate forest ecosystems (e.g. Fox et al., 2009). We derive each parameter vector \( s \) by selecting a random parameter vector \( s_0 \) and incrementally adjusting it until \( P_{EDC}(\text{DALEC2}(s)) = 1 \). To represent a range of canopy dynamics, we also imposed either (a) a deciduous condition (where \( c_{\text{fall}} > \frac{10}{11} \)) or (b) a mixed forest or evergreen condition (where \( c_{\text{fall}} < \frac{10}{11} \)), with a 50%-50% probability for either constraint.

We simplistically simulate the 8-daily MODIS LAI data and soil carbon map HWSD products from DALEC2(\( s \)) LAI and \( C_{\text{som}} \): we multiplied each soil organic carbon “truth” at \( t = 0 \) (\( C_{\text{som}}^0 \)) by \( 2^{N(0,1)} \), where \( N(0,1) \) is a random number sampled from normally distribution with mean = 0 and variance = 1.

For LAI synthetic observations, we only kept one in eight LAI values, and created correlated gaps in the remaining LAI data of random lengths until at least 50% of the 8 daily data is removed. Overall, between 65 and 68 LAI observations are kept for each 3 yr synthetic experiment. Twenty-two parameter vectors are categorised as deciduous, and eighteen as evergreen. Mean 3 yr \( F_{\text{EPP}}^t \) ranges from 2.04–8.79 gCm\(^{-2}\)d\(^{-1}\) (median = 4.75gCm\(^{-2}\)d\(^{-1}\)) and mean 3 yr \( F_{\text{nee}}^t \) ranges from −3.71 to 2.87gCm\(^{-2}\)d\(^{-1}\) (median = −0.72gCm\(^{-2}\)d\(^{-1}\)).

Acknowledgements. This project was funded by the NERC National Centre for Earth Observation, U.K. This work has made use of the resources provided by the Edinburgh Compute and Data Facility (ECDF, http://www.ecdf.ed.ac.uk/). The research leading to these results has received funding from the European Union’s Seventh Framework Programme (FP7/2007-2013) under grant agreement n° 283080, project GEOCARBON. This work used eddy covariance data acquired by the FLUXNET community and in particular by the AmeriFlux (US Department of Energy, Biological and Environmental Research, Terrestrial Carbon Program (DEFG0204ER63917 and DEFG0204ER63911)). We acknowledge the financial support to the eddy covariance data harmonization provided by CarboEuropeIP, FAOGTOSTCO, iLEAPS, Max Planck Institute for Biogeochemistry, National Science Foundation, University of Tuscia, Université Laval and Environment Canada and US Department of Energy and the database development and technical support from Berkeley Water Center, Lawrence Berkeley National Laboratory, Microsoft Research eScience, Oak Ridge National Laboratory, University of California Berkeley, University of Virginia. AmeriFlux is funded by the the United States Department of Energy (DOE – TES), Department of Commerce (DOC – NOAA), the Department of Agriculture (USDA – Forest Service), the National Aeronautics and Space Administration (NASA), the National Science Foundation (NSF), US-Syv received funding support from Department of Energy, AmeriFlux Network Management Project Support for UW ChEAS Cluster and the Department of Energy, Terrestrial Carbon Processes. The writing of this paper was partially carried out at the Jet Propulsion Laboratory, California Institute of Technology, under a contract with the National Aeronautics and Space Administration. We are grateful for feedback from L. Smallman and discussions with J. Exbrayat and T. Hill.
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Table 1. DALEC2 model parameters, descriptions, and minimum – maximum parameter values: the corresponding DALEC2 equations are fully described in Appendix A.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f_{auto}$</td>
<td>autotrophic respiration fraction</td>
<td>0.3–0.7</td>
</tr>
<tr>
<td>$f_{lab}$</td>
<td>fraction of GPP allocated to labile C pool</td>
<td>0.01–0.5</td>
</tr>
<tr>
<td>$f_{fol}$</td>
<td>fraction of GPP allocated to foliage</td>
<td>0.01–0.5</td>
</tr>
<tr>
<td>$f_{roo}$</td>
<td>fraction of GPP allocated to fine roots</td>
<td>0.01–0.5</td>
</tr>
<tr>
<td>$f_{woo}$</td>
<td>fraction of GPP allocated to wood</td>
<td>0.01–0.5</td>
</tr>
<tr>
<td>$\theta_{woo}$</td>
<td>Woody C turnover rate</td>
<td>$2.5 \times 10^{-5}–10^{-3}$ d$^{-1}$</td>
</tr>
<tr>
<td>$\theta_{roo}$</td>
<td>Fine root C turnover rate</td>
<td>$10^{-4}–10^{-2}$ d$^{-1}$</td>
</tr>
<tr>
<td>$\theta_{lit}$</td>
<td>Litter C turnover rate</td>
<td>$10^{-4}–10^{-2}$ d$^{-1}$</td>
</tr>
<tr>
<td>$\theta_{som}$</td>
<td>Soil organic C turnover rate</td>
<td>$10^{-7}–10^{-3}$ d$^{-1}$</td>
</tr>
<tr>
<td>$\theta_{min}$</td>
<td>Litter mineralisation rate</td>
<td>$10^{-2}–10^{-5}$ d$^{-1}$</td>
</tr>
<tr>
<td>$\Theta$</td>
<td>temperature dependence exponent factor</td>
<td>0.018–0.08</td>
</tr>
<tr>
<td>$d_{onset}$</td>
<td>Leaf Onset Day</td>
<td>1–365</td>
</tr>
<tr>
<td>$d_{fall}$</td>
<td>Leaf Fall Day</td>
<td>1–365</td>
</tr>
<tr>
<td>$c_{eff}$</td>
<td>Canopy Efficiency Parameter</td>
<td>10–100</td>
</tr>
<tr>
<td>$c_{lma}$</td>
<td>Leaf Mass per area</td>
<td>10–400 g C m$^{-2}$</td>
</tr>
<tr>
<td>$c_{lf}$</td>
<td>Annual Leaf Loss Fraction</td>
<td>$\frac{1}{8}$–1</td>
</tr>
<tr>
<td>$c_{onset}$</td>
<td>Labile C release period</td>
<td>10–100 day</td>
</tr>
<tr>
<td>$c_{fall}$</td>
<td>Leaf-fall period</td>
<td>20–150 day</td>
</tr>
<tr>
<td>$C_{lab}^t$</td>
<td>Labile C pool at time $t$</td>
<td>20–2000 g C m$^{-2}$</td>
</tr>
<tr>
<td>$C_{fol}^t$</td>
<td>Foliar C pool at time $t$</td>
<td>20–2000 g C m$^{-2}$</td>
</tr>
<tr>
<td>$C_{roo}^t$</td>
<td>Fine root C pool at time $t$</td>
<td>20–2000 g C m$^{-2}$</td>
</tr>
<tr>
<td>$C_{woo}^t$</td>
<td>Above &amp; Below ground woody C pool at time $t$</td>
<td>$100–10^5$ g C m$^{-2}$</td>
</tr>
<tr>
<td>$C_{lit}^t$</td>
<td>Litter C pool at time $t$</td>
<td>20–2000 g C m$^{-2}$</td>
</tr>
<tr>
<td>$C_{som}^t$</td>
<td>Soil organic C pool at time $t$</td>
<td>$100–2 \times 10^5$ g C m$^{-2}$</td>
</tr>
</tbody>
</table>

$^1 f_{woo}$ is equivalent to $1 - f_{auto} - f_{fol} - f_{lab}$.

Table 2. Synthetic experiment parameter error reduction, and AmeriFlux experiment 3 yr NEE 50% CR and bias reduction for MDF estimates using individual EDCs, relative to the standard MDF estimates.

<table>
<thead>
<tr>
<th>EDC</th>
<th>Synthetic experiment parameter error reduction ($I_{EPC(n)}$)</th>
<th>AmeriFlux experiments 2\textsuperscript{nd} NEE 50% CR reduction (bias reduction)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$-0%$</td>
<td>$27%$ ($-11%$) $19%$ ($-13%$) $3%$ ($-11%$)</td>
</tr>
<tr>
<td>2</td>
<td>$-1%$</td>
<td>$39%$ ($-26%$) $29%$ ($-25%$) $14%$ ($-19%$)</td>
</tr>
<tr>
<td>3</td>
<td>$0%$</td>
<td>$13%$ ($-0%$) $1%$ ($3%$) $0%$ ($-7%$)</td>
</tr>
<tr>
<td>4</td>
<td>$-1%$</td>
<td>$30%$ ($-14%$) $22%$ ($-14%$) $9%$ ($-17%$)</td>
</tr>
<tr>
<td>5</td>
<td>$8%$</td>
<td>$3%$ ($-3%$) $0%$ ($-4%$) $1%$ ($-11%$)</td>
</tr>
<tr>
<td>6</td>
<td>$2%$</td>
<td>$10%$ ($3%$) $-2%$ ($6%$) $-1%$ ($-3%$)</td>
</tr>
<tr>
<td>7</td>
<td>$-13%$</td>
<td>$-15%$ ($52%$) $-28%$ ($76%$) $-25%$ ($95%$)</td>
</tr>
<tr>
<td>8</td>
<td>$3%$</td>
<td>$34%$ ($-36%$) $37%$ ($-9%$) $16%$ ($-66%$)</td>
</tr>
<tr>
<td>9</td>
<td>$1%$</td>
<td>$-39%$ ($89%$) $-50%$ ($57%$) $-31%$ ($100%$)</td>
</tr>
<tr>
<td>10</td>
<td>$2%$</td>
<td>$10%$ ($19%$) $6%$ ($25%$) $5%$ ($18%$)</td>
</tr>
<tr>
<td>11</td>
<td>$-1%$</td>
<td>$10%$ ($-0%$) $1%$ ($11%$) $3%$ ($1%$)</td>
</tr>
<tr>
<td>12</td>
<td>$2%$</td>
<td>$8%$ ($-1%$) $2%$ ($0%$) $3%$ ($-6%$)</td>
</tr>
<tr>
<td><strong>ALL EDCs</strong></td>
<td><strong>34%</strong></td>
<td><strong>43%</strong> ($69%$) <strong>48%</strong> ($93%$) <strong>32%</strong> ($93%$)</td>
</tr>
</tbody>
</table>

\textsuperscript{1}The parameter error reduction metric, $I_{EPC(n)}$, is described in section 2.4. \textsuperscript{2}The derivations of 3 yr NEE 50% CR and bias reductions are described in section 2.6.
Fig. 1. Exponential decay test (EDC 8) performed on nine example normalised $C_{\text{pool}}$ trajectories over a 3 yr time-span. The $C_{\text{pool}}$ trajectories are normalised such that $C_{\text{pool}} = 1$ at $t = 0$. Examples 1–5 were accepted (EDC 8 = 1) and examples 6–9 were rejected (EDC 8 = 0). The exponential decay fit (dashed line) is shown for pool trajectories where EDC 8 = 0.
Fig. 2. Aggregated parameter estimates $\mathbf{x}_{\text{STA}}$ (standard sampling – blue) and $\mathbf{x}_{\text{EDC}}$ (EDC sampling - red) from deciduous and evergreen synthetic LAI and soil organic carbon observations – these are compared against observation and EDC independent parameter samples $\mathbf{x}_{\text{RAN}}$ (light grey). Panels (a–c) Normalised parameter space error ($\epsilon$) probability density functions for (a) Group A (directly inferable) parameters, (b) Group B (indirectly inferable) parameters, and (c) all DALEC2 parameters. $\epsilon$ values for each parameter group were derived using Eq. (15). In panels (d) and (e) the probability density functions of live carbon stock (foliar labile wood and roots) and dead carbon stock (litter and soil carbon) biases against the synthetic truth parameters $\mathbf{s}$ are shown for $\mathbf{x}_{\text{RAN}}$, $\mathbf{x}_{\text{STA}}$ and $\mathbf{x}_{\text{EDC}}$ parameter estimates.
Fig. 3. Three year mean DALEC2 net ecosystem exchange (NEE) biases (relative to synthetic truth) aggregated across 40 synthetic experiments at $0.5 \text{ g C m}^{-2} \text{ d}^{-1}$ intervals. The bias frequencies are shown for DALEC2($x_{STA}$) (standard sampling – blue) and DALEC2($x_{EDC}$) (EDC sampling – red) relative to the synthetic truth DALEC2($s$) (black dashed line).
Fig. 4. DALEC2 daily NEE ensemble estimates at three AmeriFlux sites: Sylvania Wilderness (US-Syv, mixed forest, top two rows), Howland Forest (US-Ho1, evergreen needleleaf, middle two rows), and Morgan Monroe State Forest (US-MMS, deciduous broadleaf, bottom two rows). For each site the DALEC2($\alpha_{EDC}$) and the DALEC2($\alpha_{STA}$) ensemble confidence intervals are denoted as EDC and STA, respectively. The DALEC2 analyses - based on MODIS LAI retrievals, HWSD soil organic carbon estimates and ERA interim meteorological drivers - are completely independent from all AmeriFlux site measurements.
Fig. 5. Three year mean DALEC2 cumulative NEE (kg C m\(^{-2}\)) compared against cumulative measured NEE at three AmeriFlux sites: Sylvania Wilderness (US-Syv, mixed forest, left), Howland Forest (US-Ho1, evergreen needleleaf, middle), and Morgan Monroe State Forest (US-MMS, deciduous broadleaf, right). The standard analysis median and 50% confidence ranges (CR) are shown in blue, and the corresponding analyses with EDCs are shown in red. AmeriFlux NEE measurements are denoted as a black line. The DALEC2 analyses – based on MODIS LAI retrievals, HWSD soil organic carbon estimates and ERA interim meteorological drivers – are completely independent from all AmeriFlux site measurements.
Fig. 6. Schematic of the carbon fluxes in DALEC2. The green arrow indicates the gross primary production (GPP). Red arrows represent respiration fluxes: autotrophic respiration ($R_{auto}$) and heterotrophic respiration ($R_{het}$). Blue arrows represent C allocation to the labile ($C_{lab}$), foliar ($C_{fol}$), wood ($C_{woo}$) and fine root ($C_{roo}$) pools. Grey arrows represent the litterfall and decomposition fluxes to the litter ($C_{lit}$) and soil organic matter ($C_{som}$) pools.