The importance of micrometeorological variations for photosynthesis and transpiration in a boreal coniferous forest

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Abstract

Plant canopies affect the canopy micrometeorology, and thereby alter canopy exchange processes. For the simulation of these exchange processes on a regional or global scale, large-scale vegetation models often assume homogeneous environmental conditions within the canopy. In this study, we address the importance of vertical variations in light, temperature, CO$_2$ concentration and humidity within the canopy for fluxes of photosynthesis and transpiration of a boreal coniferous forest in central Sweden. A leaf-level photosynthesis-stomatal conductance model was used for aggregating these processes to canopy level while applying the within-canopy distributions of these driving variables.

The simulation model showed good agreement with eddy covariance-derived gross primary production (GPP) estimates on daily and annual timescales, and showed a reasonable agreement between transpiration and observed H$_2$O fluxes, where discrepancies are largely attributable to a lack of forest floor evaporation in the model. Simulations in which vertical heterogeneity was artificially suppressed revealed that the vertical distribution of light is the driver of vertical heterogeneity. Despite large differences between above-canopy and within canopy humidity, and despite large gradients in CO$_2$ concentration during early morning hours after nights with stable conditions, neither humidity nor CO$_2$ played an important role for vertical heterogeneity of photosynthesis and transpiration.

1 Introduction

Plant canopies intercept radiation and alter the circulation of air and the exchange of energy at the land surface. The biochemical processes taking place in the plants and the soil affect the chemical composition of the air within the canopy. These biogeophysical and biogeochemical alterations made to the local environment in turn affect the canopy’s biochemistry and exchange processes, and thereby provide a feedback to the growth of the canopy itself.

The extinction of light in the canopy results in a large gradient of light conditions within the canopy, and the differences get even more pronounced when considering shading, resulting
in directly lit leaf area and leaf area that is shaded (e.g. Cowan, 1968; Norman, 1975). Within-canopy gradients of CO$_2$ have been measured exceeding 50 ppm (e.g. Buchmann et al., 1996; Brooks et al., 1997; Han et al., 2003). Moreover, forest canopies alter the temperature and humidity inside (Arx et al., 2012), with in general more moderate temporal variations within the canopy compared to the above-canopy environment.

Some of these types of heterogeneity have been captured in stand-scale models: For light extinction, a layering of the canopy can be applied (e.g. Monteith, 1965; Duncan et al., 1967; Cowan, 1968; Norman, 1975), as well as a separation of sunlit and shaded leaves (e.g. Duncan et al., 1967; Spitters, 1986). Model studies have been performed investigating the importance of forest structure on exchange processes (Ellsworth and Reich, 1993; Falge et al., 1997).

The Farquhar model (Farquhar et al., 1980) and models based on that (e.g., Leuning, 1990; Collatz et al., 1991), which describe leaf-level CO$_2$ assimilation, form the basis of many canopy-scale photosynthesis models. Similarly, leaf-level stomatal conductance models (e.g., Ball et al., 1987; Leuning, 1995) have been applied at canopy scale. For these canopy-scale applications, homogeneous conditions within the canopy are often assumed. This simplification has great advantage for the simulation of the exchange processes: the canopy can be treated as a single big leaf (the so-called “big-leaf approach”; Sinclair et al., 1976; Sellers et al., 1992), and the upscaling from leaf-level process rates to a canopy-integrated rate can be done linearly by using the leaf area index of the canopy.

Although dynamic vegetation models typically apply leaf-scale models for describing the processes at the canopy scale, they vary greatly in the level of detail that they use to represent light extinction. The big-leaf approach described above is adopted by some dynamic vegetation models (e.g., LPJ, Sitch et al. (2003); or Sheffield-DGVM, Woodward and Lomas (2004)). Other dynamic vegetation models, or land surface schemes within climate or Earth system models, include a layering (e.g., O-CN, Zaehle and Friend (2010); or SEIB-DGVM, Sato et al. (2007)). In addition to a vertical layering, Mercado et al. (2009) applied a distinction between sunlit and shaded leaves as well in the land surface scheme JULES. The
layering described above is applied to determine light extinction; none of the large-scale models applies vertical gradients of humidity or CO$_2$ concentration.

The assumption of homogeneous conditions within the canopy warrants a critical assessment: The possible gradients in canopy conditions, as mentioned above, have the potential to affect leaf photosynthesis and transpiration, and thereby cause deviations from this linear relationship, which affects the canopy-integrated values. In this study, we quantify the importance of vertical heterogeneity in environmental drivers at the leaf scale for the simulation of stand-scale fluxes of photosynthesis and transpiration for a coniferous forest in central Sweden for 1999. Within-canopy profile measurements were used to determine the heterogeneity in driving variables (temperature, ambient CO$_2$ concentration, water vapour concentration and wind speed), and a detailed light transfer model was applied to compute the distribution of photosynthetic absorbed radiation (PAR). In the first part of the study, model results are compared with observations. In the second part, model simulations are described applying average within-canopy or above-canopy conditions instead of distributions, in order to assess the importance of heterogeneity for simulated GPP and transpiration. The importance of within-canopy variability is compared with the variability caused by diurnal and annual changes in driving variables.

2 Materials and methods

This study applies observations from the Norunda forest site, a coniferous forest in Central Sweden, 60°05′11″ N, 17°28′46″ E, altitude 45 m. The site is situated on a sandy glacial till; long-term mean annual temperature is 5.5°C and annual precipitation is 527 mm y$^{-1}$ (Lundin et al. 1999). The forest is dominated by Scots pine (Pinus sylvestris) and Norway spruce (Picea abies), with occasional broadleaf trees, the canopy is approximately 25 m high and has a leaf area index (LAI) of 4.5. More details about the site are found in Lundin et al. (1999).

For this site, a detailed photosynthesis-stomatal conductance model was applied to simulate canopy-scale photosynthesis and transpiration rates for 1999–2002. Simulated fluxes
were compared with the fluxes of CO\textsubscript{2} and H\textsubscript{2}O measured with eddy covariance. The simulations for 1999 were analysed further to address the importance of within-canopy heterogeneity in the simulations.

2.1 Measurements

2.1.1 Canopy profile measurements

Profile measurements of CO\textsubscript{2} and water vapour concentrations, as well as air temperature and wind speed, were performed at a number of levels within and above the canopy. In this study we used the measurements within the canopy, as well as the first measurement above, to derive the profile of these properties within the canopy. The measurements from 8.5 m, 13.5 m, 19.0 m, 24.5 m and 28.0 m above the forest floor were used (Lundin et al., 1999; Mölder et al., 2000). In addition, the concentrations of water vapour were measured at 0.7 m above the forest floor as well. All concentrations were averaged to half-hourly means.

For the simulation of within-canopy conditions, these profiles were linearly interpolated to represent the conditions. The lowest measurement was considered representative for the part of the canopy between the forest floor and the lowest measurement height.

2.1.2 Flux measurements of H\textsubscript{2}O and CO\textsubscript{2}

Eddy covariance measurements of exchange of CO\textsubscript{2} and H\textsubscript{2}O were made at a height of 35 m (approximately 10 m above the canopy) with a closed-path system (a LI-6262 gas analyser, LI-COR Inc. and a Gill R2 sonic anemometer, Gill Instruments) at a frequency of 10 Hz. The high-frequency flux measurements were aggregated to 30 min averages. A detailed description of the eddy covariance setup and the flux calculations is given in Grelle and Lindroth (1996) and Grelle et al. (1999).

Stable conditions prevailing during nighttime can cause a build-up of CO\textsubscript{2}, and to a lesser extent H\textsubscript{2}O, within the canopy (Goulden et al., 1996; Aubinet et al., 2005). This was observed for the Norunda site as well (Feigenwinter et al., 2010), and we corrected the flux measurements for this storage of CO\textsubscript{2} and H\textsubscript{2}O within the canopy with the help of the profile...
measurements of CO$_2$ and H$_2$O concentrations (Baldocchi and Wilson, 2001). To do so, the profiles of CO$_2$ and H$_2$O below the sensor were interpolated between the observation levels for the 30 min interval before and after that of the observed fluxes. The difference between the integrated profiles for these two time periods, divided by the average time between the two (60’) was assumed as storage flux $F_{stor}$ for the given time interval $t$:

$$F_{stor,t} = \frac{\int_{0}^{h} c_{z,t+\Delta t}dz - \int_{0}^{h} c_{z,t-\Delta t}dz}{2\Delta t}$$  \hspace{1cm} (1)$$

in which $c_z$ is the concentration of CO$_2$ or H$_2$O at height $z$ (expressed here in mol m$^{-3}$), obtained from linear interpolation of the profile data, and $\Delta t$ is the time interval for the aggregated measurements (30’).

Estimates of gross primary production (GPP) were derived from the measured CO$_2$ flux (net ecosystem exchange, NEE) by subtracting ecosystem respiration. For this, the data were distributed in 5-day periods, and for each period, the temperature dependence of ecosystem respiration was computed according to Reichstein et al. (2005) with a function (Lloyd and Taylor, 1994) fitted through all nighttime fluxes within a 15 day window centered around the 5 day period of consideration. For some periods, nighttime respiration showed little or no sensitivity to temperature, leading to subtraction of a (near-)constant respiration.

Periods with missing observations (either missing climate data for the forcing, or missing flux data for comparison) were omitted from the analysis.

Grelle (1997) showed that the flux footprint of the 35 m level was well within the homogeneous ca. 100 years old mixed pine/spruce forest surrounding the tower in all directions. Occasionally the nighttime flux footprint extended beyond the homogeneous part of the forest into younger stands, ca. 50 years old, but still consisting of mixed coniferous forest.

2.1.3 Auxiliary measurements

Apart from the within-canopy properties, above-canopy conditions were used. Photosynthetically active radiation (PAR) was measured with a LI-1905Z PAR sensor (LI-COR Inc.).
Measurements of diffuse radiation were not available for the studied period, but measurements of diffuse radiation with a BF-3 sunshine sensor (Delta-T Devices Ltd) that started in 2004 were applied to derive a relationship between the fraction of diffuse radiation at the surface and the fraction of the top-of-atmosphere radiation that reached the surface (described below, Sect. 2.2.1).

In addition to the eddy covariance measurements of the H₂O flux, which represents the canopy’s evapotranspiration, measurements of tree transpiration were performed in 1999 for a nearby site (500 m distance) using the tissue heat balance technique (Čermák et al., 1973). The site is younger (approximately 50 years old) than the footprint of the tower, but climatological and hydrological conditions were similar to those in the footprint, and it has a similar species composition and leaf area. Details to the sapflow measurements are given in Lagergren and Lindroth (2002).

2.2 Model description

2.2.1 Light distribution

Because within-canopy measurements for light interception did not exist for this site, and because an accurate representation of the light interception requires a considerably larger distribution than the measurements at certain heights in the canopy as done for the other forcing data, a detailed radiation transfer scheme was constructed to simulate light distribution (Appendix A), which was used to simulate the distribution of PAR within the canopy. The scheme uses existing theory on light extinction and reflection, while using the assumptions made in large-scale models. It separates vertical layers, and sunlit and shaded fractions of the leaves within these layers. Moreover, within each fraction and layer, the leaf angle distribution (assuming an isotropic or spherical distribution) is represented by a grid of azimuth and zenith angles. For each of the leaf orientations in the sunlit and shaded fraction within each of the layers, absorption, reflection and transmission are computed with a two-way scheme computing the downward and upward scattering within the canopy with an angular distribution. Based on the separation between sunlit and shaded leaf area, it provides
a probability density function of absorbed PAR for each of the layers. The scheme does not account for clumping of leaves, nor does it account for penumbral radiation. Details of the light distribution scheme are provided in Appendix A.

The light distribution model requires a separation between direct and diffuse light. Observations of the diffuse flux were not available for the study period, but observations of the diffuse and the total shortwave flux were available for June 2004 till December 2010. The latter were used to reparameterize a relationship between the diffuse fraction ($f_{\text{dif}}$, the ratio between diffuse and global radiation at the surface) and the fraction of the top-of-atmosphere flux that is transmitted through the atmosphere ($f_{\text{trans}}$, the ratio between the global radiation at the surface and the global radiation at the top of the atmosphere), described by Spitters et al. (1986). The boundaries between the regimes in this relationship, which were originally derived for De Bilt (Netherlands), did not match the observations from the Norunda forest site. Therefore, the parameters describing these boundaries were optimized by maximizing the coefficient of determination of the function using the data for 2004–2010 (Fig. 1), resulting in the following relationship:

$$
\begin{align*}
    f_{\text{dif}} &= 1 & \text{for } f_{\text{trans}} < 0.27 \\
    f_{\text{dif}} &= 1 - 18.3(f_{\text{trans}} - 0.27)^2 & \text{for } 0.27 \leq f_{\text{trans}} < 0.33 \\
    f_{\text{dif}} &= 1.67 - 2.20 f_{\text{trans}} & \text{for } 0.33 \leq f_{\text{trans}} < 0.65 \\
    f_{\text{dif}} &= 0.23 & \text{for } f_{\text{trans}} \geq 0.65
\end{align*}
$$

(2)

Apart from the fraction of diffuse radiation, the model requires a distribution of the diffuse light over sky azimuth and zenith angles. For this, we applied a standard overcast sky (Monteith and Unsworth, 1990), which has no azimuthal preference for the light, for conditions in which all radiation is diffuse ($f_{\text{dif}} = 1$). For a high fraction of diffuse radiation ($0.8 < f_{\text{dif}} < 1$), a skylight distribution representing translucent high clouds (Grant et al., 1996) was applied, which represents diffuse conditions, but concentrates part of the skylight in the solar direction. For lower fractions of diffuse radiation ($f_{\text{dif}} \leq 0.8$), a clear sky distribution (Harrison and Coombes, 1988) was adopted.
The detailed light extinction model (Appendix [A]) requires a distribution of the light between absorption, reflection and transmission at the leaf level. For this, the fractions 0.85, 0.09 and 0.06 were used, respectively, values provided by Ross (1975) for mean green leaves.

2.2.2 Flux model

A combined photosynthesis-stomatal conductance model was constructed, similar to the algorithms used in many large-scale ecosystem models (e.g. in ORCHIDEE; Krinner et al., 2005). The model combines a Farquhar-type photosynthesis model (Farquhar et al., 1980) with a Ball–Berry type stomatal conductance model (Ball et al., 1987). However, in contrast to typical large-scale models, we treat it here as a leaf-level model, and do the upscaling from leaf level to canopy level explicitly by accounting for the heterogeneity in environmental drivers within the canopy (see Sect. 2.1.1).

Leaf-level photosynthesis is simulated as the minimum of the Rubisco-limited CO₂ assimilation rate $A_c$ and the electron transport-limited CO₂ assimilation rate $A_j$ following Farquhar et al. (1980) and Von Caemmerer (2000):

$$A = \min(A_c, A_j)$$  \hspace{1cm} (3)

Because of the comparison with the NEE-derived photosynthesis flux, which has all respiration components subtracted, there is no accounting for the leaf’s dark respiration in the computation of $A_c$ or $A_j$.

The Rubisco-limited rate $A_c$ is simulated as a function of CO₂ concentration and O₂ concentration with temperature-dependent Michaelis–Menten constants for carboxylation and oxygenation (Von Caemmerer, 2000), and is dependent on the maximum Rubisco rate $V_{c,\text{max}}$ (Table 1):

$$A_c = \frac{(C_i - \Gamma_*) V_{c,\text{max}}}{C_i + \frac{O}{K_o}}$$  \hspace{1cm} (4)
Here, \( C_i \) is the leaf-internal \( \text{CO}_2 \) concentration, \( O \) is the leaf-internal \( \text{O}_2 \) concentration (assumed constant at 21\%), \( \Gamma_* \) is the \( \text{CO}_2 \) compensation point, and \( K_c \) and \( K_o \) are the Michaelis–Menten constants for carboxylation and oxygenation, respectively, which are temperature-dependent (Von Caemmerer, 2000). The electron transport-limited \( \text{CO}_2 \) assimilation rate \( A_j \) depends primarily on the electron transport rate \( J \) at the leaf level, as well as on the leaf-internal \( \text{CO}_2 \) concentration (Von Caemmerer, 2000):

\[
A_j = \frac{(C_i - \Gamma_*)J}{4C_i + 8\Gamma_*}
\]  

(5)

The electron transport rate \( J \) is determined from the empirical function describing \( J \) as a function of the absorbed irradiance \( I \) (corrected for spectral quality and leaf absorptance) and the maximum electron transport rate \( J_{max} \) (Table 1), applying an empirical curvature factor \( \theta \) (Farquhar et al., 1980; Von Caemmerer, 2000):

\[
J = \frac{I + J_{max} - \sqrt{(I + J_{max})^2 - 4\theta I J_{max}}}{2\theta}
\]  

(6)

The photosynthetic parameters determined by Thum et al. (2008), who used stand-scale eddy covariance measurements from Norunda for 2001 to parameterize their model, were adopted (Table 1).

Leaf-level stomatal conductance, \( g_s \), is simulated following Ball et al. (1987) with a modification by Collatz et al. (1991) as a function of the \( \text{CO}_2 \) assimilation rate, leaf surface \( \text{CO}_2 \) concentration \( c_s \) and leaf surface relative humidity \( h_s \):

\[
g_s = b + k \frac{A}{c_s} h_s
\]  

(7)

The values for the intercept \( b \) and the dimensionless slope \( k \) in this relationship are taken from Collatz et al. (1991) (Table 1). The leaf’s aerodynamic conductance, \( g_b \), is described as a function of leaf size and wind speed, following Goudriaan (1977).
The mutual interaction between photosynthesis and stomatal conductance (stomatal conductance is affected by the CO\textsubscript{2} assimilation rate $A$, and CO\textsubscript{2} assimilation is affected by the leaf-internal CO\textsubscript{2} concentration and thus by stomatal conductance) is determined iteratively by solving a squared function of the stomatal conductance $g_s$ applying bisection.

The transpiration flux $E$ is computed from the gradient between the water vapour concentrations in the stomata (assumed to be saturated, $H_i$) and the outside air ($H_a$) using the stomatal and aerodynamic resistances for water vapour (denoted as $g'_s$ and $g'_b$, respectively) in series:

$$E = (H_i - H_a)(g'_s + g'_b)$$ (8)

Driving variables for the model are PAR, CO\textsubscript{2} concentration, humidity, temperature and wind speed. The model applies the simulated distributions of light (Sect. 2.2.1) and the observed vertical profiles of CO\textsubscript{2}, humidity, temperature and wind speed (Sect. 2.1.1). The observed vertical distribution of leaf area (Sect. 2.3) was used to integrate the leaf-scale photosynthesis and transpiration rates to the stand scale.

2.3 Simulation setup

The photosynthesis-stomatal conductance model described above was applied to simulate leaf-level photosynthesis and transpiration in the canopy of the Norunda forest site. To do so, the canopy was distributed in 25 vertical layers of 1 m thickness, to which leaf density was prescribed according to the LAI profile for the site derived from the vertical leaf area distribution in the tree crowns (Morén et al. 2000) combined with an extensive stratified sampling of tree heights and tree crown lengths (Håkansson and Körling 2002). Within these layers, the sunlit and shaded parts of the needles were separated as described above, and within each of these two fractions, a spherical leaf angle distribution was represented with $4 \times 4$ leaf normal azimuth and zenith angles. These 16 leaf angle classes were distributed over the hemisphere so that each of the 16 classes represents an equal fraction 1/16 of the full distribution.
The light distribution model (Sect. 2.2.1 and Appendix A) was applied to simulate the leaf-level absorption of photosynthetically active radiation (PAR). For each layer, the concentrations of water vapour and CO$_2$, as well as the temperature and wind speed, were obtained from linear interpolation of the within-canopy measurements (Sect. 2.1.1). These conditions varied between the layers, whereas the different leaf angle classes within one layer were considered to have the same temperature, wind speed and atmospheric concentrations of CO$_2$ and H$_2$O. Because of the varying PAR between the classes, stomatal conductance, and thereby leaf-internal CO$_2$ concentration, were able to vary between these as well.

Apart from these simulations in which the heterogeneity within the canopy was represented explicitly (hereafter referred to as simulation HET), a number of simulations were performed in which these conditions were averaged spatially, thereby removing part of the vertical heterogeneity. For these simulations, the conditions were prescribed to the (LAI-weighted) canopy average instead of the distribution, or in some cases to the above-canopy ($h = 28.0$ m) or within-canopy ($h = 8.5$ m) value. A complete overview of the simulations performed in this study is given in Table 2.

Moreover, the importance of vertical heterogeneity in forcing parameters was compared with the annual and diurnal variability in the forcing with the help of two sets of simulations in which this temporal variability was artificially removed for all parameters except one. These simulations were driven without annual heterogeneity (labeled as AHET in Table 2, applying an annually averaged vertical profile and diurnal cycle) for all parameters except one. Similarly, the simulations without diurnal heterogeneity (labeled as DHET, applying average daily conditions while maintaining the annual cycle and vertical profile) had the diurnal heterogeneity removed for all parameters except one. The simulated temporally varying vertical profiles of CO$_2$ assimilation and transpiration were averaged per day and integrated over the canopy (AHET), averaged per half-hourly period of the day and integrated over the canopy (DHET), or averaged over both days and hours for each layer in the profile (HET), and the distributions (presented as percentiles) were computed.
3 Results

3.1 Comparison with observations

Photosynthesis and transpiration from the simulation in which the heterogeneity was accounted for (HET, Table 2) were compared with the photosynthesis derived from the observed CO₂ flux and the observed H₂O flux, respectively, for the years 1999–2002.

The annual cycle of photosynthesis (Fig. 2a) was generally well captured by the model. The day-to-day variability was represented, with individual days with low photosynthesis, resulting primarily from low incoming radiation on these days (not shown). A marked decrease in photosynthesis was observed for a two-week period in 1999 starting from 28 July (days 209–223), likely as a result of a preceding period of drought, coinciding with low soil moisture values (not shown, Lagergren and Lindroth, 2002). This decrease was not captured by the model, because the impact of soil moisture conditions is not accounted for. The diurnal cycle for photosynthesis (Fig. 3a) was captured well by the model for all seasons, except for winter, when the model considerably overestimated photosynthesis. A similar two-week drought occurred in 2001 starting end of June.

The annual cycle of transpiration (Fig. 2b) showed a reasonable agreement with the observed H₂O flux (which consists of both evaporation and transpiration). In general, the observed flux was considerably higher than the simulated one in winter and spring (February–June), which can likely be attributed to a high contribution of evaporation to the H₂O flux, in spring coinciding with the snow melt period. Transpiration estimates for 1999 from sapflow measurements (applying the tissue heat balance method, Lagergren and Lindroth, 2002) showed a later onset of transpiration (Fig. 2b and c), in better agreement with the simulated rates. The diurnal cycle of transpiration (Fig. 3b) showed this overestimation for winter and spring in the daytime, with a particular mismatch for the winter season, when simulated transpiration was negligible. For summer and autumn, however, the average diurnal cycle was captured well by the model, with a slight underestimation between 6 a.m. and noon.

Three 5 day periods were selected as case studies (Fig. 4), which are analysed below with respect to their within-canopy variations in environmental conditions (Fig. 4a–d). Case
1 (18–22 May 1999) was selected to represent large within-canopy gradients of humidity and temperature. Case 2 (24–28 August 1999) represents large changes in sky conditions, and therefore large changes in the vertical distribution of light. Case 3 (8–12 September 1999) exhibits large gradients of atmospheric CO$_2$ concentration within the canopy. For these cases, the dynamics of canopy-scale photosynthesis and transpiration (Fig. 4g and h) were captured well by the simulation model. Negative fluxes of CO$_2$ assimilation in the observations (Fig. 4g) are due to the method used to separate the net CO$_2$ flux into CO$_2$ assimilation and ecosystem respiration, and represent the noise in the observation-based flux.

These cases were analysed in detail, after which the impact of heterogeneity was assessed at the annual level. Because of the small needle diameter, the leaf boundary layer is shallow, and the simulated exchange processes turned out to be insensitive to wind speed. Therefore, the analysis below will concentrate on humidity and temperature, PAR and CO$_2$ concentration.

### 3.2 Heterogeneity in humidity and temperature

For the period of the first case study, 18-22 May 1999, the CO$_2$ assimilation flux was captured well by the model (Fig. 4g), and the simulated transpiration flux was slightly underestimated for 18 and 19 May, whereas it was captured well for 20–22 May (Fig. 4h). During this 5-day period, there were marked differences between the conditions above the canopy and within the canopy (Fig. 5). In general, temperatures were up to 3 K higher above the canopy than within, and relative humidity was up to 15 % lower. Differences were largest during nighttime, e.g. in the nights between 18 and 19 and between 19 and 20 May (Fig. 5a and b), but even in the early morning and late evening, while photosynthesis occurred, differences were apparent. The pattern of stomatal conductance (Fig. 5c) followed primarily that of photosynthesis (Fig. 4e), which is the main cause for the similarity in the vertical profiles of photosynthesis and transpiration (Fig. 4f).

Variations in relative humidity have two opposing effects: (1) a high relative humidity causes the stomatal conductance to be high (Eq. 7) and thereby stimulates transpiration
and CO₂ assimilation, and (2) under high relative humidity, the humidity gradient between the substomatal cavity (which is assumed to be saturated) and the air surrounding the leaf is low, thereby hampering transpiration.

The simulation with homogeneous temperature (HOM_TEM) or humidity (HOM_HUM) resulted in very similar CO₂ assimilation and transpiration compared with the simulation applying heterogeneous conditions (HET). Because the vertical variations in humidity and temperature were relatively small, and the response is reasonably linear, the deviations were not large (not shown).

However, when applying within-canopy (8.5 m, simulation HOM_HUM_IC) or above-canopy (28 m, simulation HOM_HUM_AC) humidity instead of the canopy-average value (Fig. 5d), transpiration can be over- or underestimated within the canopy (Fig. 5e-f), in particular in late evening, night and early morning, in line with the observed gradients for humidity (Fig. 5a). The lower humidity above the canopy, which caused the largest deviations, resulted in an overestimation of transpiration of up to 80% during the abovementioned time of the day (e.g., during the night from 19 to 20 May). Applying the above-canopy conditions yielded reasonable results in the top of the canopy, but overestimated transpiration in the lower canopy (Fig. 5e). The use of within-canopy humidity caused reasonable results for the lower canopy (with no deviations for the actual height of the measurements, 8.5 m), but with the top of the canopy depicting an underestimation of transpiration (Fig. 5f). From the two opposing effects mentioned above, the changes in humidity gradient were driving these deviations, whereas the stomatal response had only a mild counteracting effect.

The deviations can be considerable during the period with little or no daylight, but the difference disappeared during daytime. Hence, the daily total transpiration was only slightly affected, with 7 days exceeding an overestimation of 10% in the period April–September for the simulation with above-canopy humidity, and 7 days exceeding an underestimation of 10% for the same period for the simulation with within-canopy humidity. On an annual basis, the total overestimation of the annual transpiration was 1.0% in the simulation with above-canopy humidity, and the underestimation was 1.6% in the simulation with within-canopy humidity (not shown). Effects of above-canopy or within-canopy temperature rather
than the temperature average yielded even lower deviations in the simulated transpiration (not shown): an underestimation of 0.5% when using above-canopy temperature, and no difference when using within-canopy temperature. Because the changes in stomatal conductance were only minor, the simulated CO$_2$ assimilation flux was affected less than the transpiration flux.

### 3.3 Heterogeneity in light absorption

Within-canopy heterogeneity in light conditions was the most important contribution to the within-canopy heterogeneity of the simulated photosynthesis and transpiration rates. The case study period 24–28 August 1999 (Fig. 4) showed a marked difference in the vertical profiles of light absorption (Fig. 4a), photosynthesis (Fig. 4e) and transpiration (Fig. 4f) between clear days (e.g. 25 August) and overcast days (e.g. 27 August), resulting in canopy photosynthesis rates that differ greatly (Fig. 4g). These differences were largely caused by the absolute amounts of radiation.

The angular distribution of the light is often counteracting the impact of high levels of radiation. Figure 6a shows that the dominant part of the radiation was direct for 25 August, whereas there was only diffuse radiation on 27 August. This distribution over direct and diffuse radiation affected the efficiency of the canopy to assimilate: With large amounts of direct radiation, part of the canopy is light-saturated and produces at its maximum rate. However, a large part of the canopy, most notably the shaded leaves, receive considerably lower amounts of radiation. In contrast, for overcast conditions, e.g. those prevailing on 27 August, the light is distributed more evenly in the canopy. This, combined with the generally lower level of radiation, makes that less leaves are under light-saturated conditions, and that the lower part of the canopy receives more light and is contributing more to the canopy photosynthesis.

The impact of sky conditions on the distribution of the light affected the light use efficiency (LUE, which is defined here as the CO$_2$ assimilation flux per amount of absorbed PAR) of the canopy, both within the vertical profile (Fig. 6b) and for the canopy as a whole (Fig. 6e). Around noon on sunlit days, the absorption in the top of the canopy was high, and the LUE
in the top of the canopy was low, resulting in lower canopy LUE values (Fig. 6e). In the early morning and late evening hours of clear-sky days, as well as on overcast days, the fraction of diffuse radiation was high and the absolute amount of incoming PAR was low, resulting in a more even distribution of the light in the canopy, and generally lower photosynthesis rates. In contrast with the low absolute amounts, the efficiency was higher, which resulted in improved canopy LUE.

The light extinction scheme applied here distinguishes leaf-level heterogeneity in light absorption caused by the distinction between sunlit and shaded leaves, the vertical layering of the canopy and the distribution of leaf angles. The contribution of these factors to the heterogeneity in CO₂ assimilation, and thereby their impact on LUE, is illustrated in Fig. 6b-d. Simulation HOM_PAR_LAYER, which did not separate sunlit and shaded leaves or leaf angles, and which obtains its heterogeneity only from the layering in the canopy, had uniform conditions within the vertical layers, and represents a light extinction scheme that does not account for sunlit-shaded leaves, as is often applied in large-scale models. It resulted in considerably higher LUE values (Fig. 6c), particularly in the lower part of the canopy, where the distinction between sunlit and shaded leaves results in a small proportion with high PAR levels and a large proportion with very low levels. An even more equal distribution of the light was obtained with simulation HOM_PAR (Fig. 6d), which had no layering in the canopy either. This represents the so-called big-leaf approach, as used in large-scale models that lack a vertical layering. It resulted in a homogeneous distribution of the light, and in the highest LUE values for the canopy (Fig. 6e).

The distinction between direct and diffuse radiation, and the effect of the solar angle on light extinction and distribution were important contributions to the within-canopy heterogeneity. Apart from the generally higher levels of radiation and hence CO₂ assimilation obtained under high solar angle, the radiation penetrated deeper into the canopy, resulting in a more even distribution of the radiation (Fig. 7a) and higher levels of CO₂ assimilation further down in the canopy (Fig. 7b) compared to cases with a low solar angle. Similarly, the high levels of diffuse radiation obtained under overcast conditions resulted in a more
homogeneous distribution of the light because of the contributions from different azimuth and zenith angles, resulting in a more even vertical distribution of CO$_2$ assimilation (Fig. 7).

This profound difference between clear and overcast conditions was obtained as well when separating the daily CO$_2$ assimilation flux over clear days (defined here as days with more than 50% of the radiation reaching the canopy directly) and cloudy days (less than 50% of the radiation reaching the canopy directly): For clear days, lower efficiencies in CO$_2$ assimilation with a given amount of light (Fig. 8) were obtained, the light use efficiency is depicted here as the slope in the figure. The model setup depicting the full distribution of light in the canopy (simulation HET) was able to capture the efficiency for both the clear days and cloudy days, and showed a marked difference between the two. The setup without heterogeneity in the canopy light distribution (simulation HOM_PAR) generally overestimated the efficiency because of the equal distribution of light. Moreover, the difference in light use efficiency between clear days and cloudy days was smaller. The model setup used for HOM_PAR did not differentiate between direct and diffuse radiation, but the regression still depicted a difference because of the relative importance of high PAR days to the clear day set, which show generally a lower efficiency.

On the annual scale, GPP was captured well by the simulation applying full heterogeneity (simulation HET), with a slight overestimation of 3% of the annual GPP compared with the observations for the days for which data are available. The simulation without heterogeneity in the light distribution (HOM_PAR) overestimated GPP by 44% compared to this full heterogeneity setup, whereas the simulation with a layering only (HOM_PAR_LAYER) overestimated GPP by 14%.

3.4 Heterogeneity in CO$_2$ concentration

Within the canopy, the ambient concentration of CO$_2$ can vary considerably, both in time and in the vertical (Fig. 4b). Large gradients are formed under stable conditions during nighttime, when CO$_2$ assimilation has stopped, but heterotrophic and autotrophic respiration continue, while vertical mixing is reduced in the canopy. These gradients disappear quickly after sunrise, when the boundary layer growth starts and initiates turbulent mixing.
It is mainly during these early morning hours that effects of a CO$_2$ gradient in the canopy on fluxes of CO$_2$ assimilation and transpiration were to be expected.

These large gradients were seen in the third case period (Fig. 4b), and we will illustrate this impact by analysing the dynamics of this gradient on 12 September 1999 in more detail (Fig. 9). For this date, the CO$_2$ gradient built up during nighttime, and a gradient of more than 50 ppm was maintained up to two hours after sunrise (Fig. 9c). Ignoring this gradient in the simulation of CO$_2$ assimilation by using a constant (canopy-average or above-canopy) CO$_2$ concentration caused deviations of a few percents locally (Fig. 9d), but its impact on the actual profile (Fig. 9e), or on the canopy-integrated CO$_2$ assimilation flux was negligible. From 8.30 a.m. onwards, the gradient disappeared rapidly and had no further impact on CO$_2$ assimilation during the day (Fig. 9c–e).

Despite the substantial gradient in CO$_2$ concentration, its impact was small. This is because (1) photosynthesis largely takes place at the top of the canopy, where the deviations of the CO$_2$ concentration from the above-canopy value is small (Fig. 9c and e), (2) during the early hours, the solar angle is low, so light does not penetrate deeply into the canopy, hence the lower leaves can barely profit from the higher CO$_2$ concentrations, (3) leaves compensate for higher CO$_2$ concentrations with a closure of their stomata (Ball et al., 1987, Eq. 7), which causes the gradient in stomatal concentrations to be much lower than that of atmospheric concentrations. The changes in the stomatal conductance in (3) have the potential to alter transpiration as well. In the cases where photosynthesis is underestimated in the lower canopy, the simulations yield an underestimation of transpiration as well because of the lower CO$_2$ concentration (not shown). However, similarly to the impact on photosynthesis, the change in transpiration had only a marginal impact, and occurred where and when transpiration rates were small anyway.

The occurrence of CO$_2$ gradients, predominantly during nighttime and morning hours, has therefore a negligible impact on canopy-integrated photosynthesis levels.
3.5 Comparison with annual and diurnal heterogeneity

The analysis above showed the vast dominance of light as the cause for within-canopy heterogeneity of CO$_2$ assimilation and transpiration. A set of simulations that were forced by within-canopy heterogeneity of only one of the driving parameters (PAR, CO$_2$, temperature and humidity, simulations HET_PAR, HET_CO2, HET_TEM and HET_HUM) illustrates this: Fig. 10a1 and 10b1 compare the observed variability in CO$_2$ assimilation and transpiration fluxes within the canopy between the full heterogeneity simulation (HET) and the set of partial heterogeneity simulations. It clearly shows that the simulation in which light was the only heterogeneous variable (HET_PAR) had comparable variability for both CO$_2$ assimilation and transpiration fluxes, whereas the other simulations had a much smaller variability.

In order to compare the importance of vertical heterogeneity with those obtained from annual and diurnal changes in the forcing, the variability was determined at the annual and diurnal scale for the two additional sets of simulations in which annual and diurnal heterogeneity in the forcing were removed, respectively. Figure 10a2 shows that the annual variability in the flux of CO$_2$ assimilation is determined in equal amounts by variations in PAR and temperature. For the annual variability in transpiration, variability in humidity played a dominant role, with minor contributions from PAR and temperature as well (Fig. 10b2).

The diurnal variability of the CO$_2$ assimilation flux was largely dominated by PAR (Fig. 10a3), which is the obvious driver of the daytime-to-nighttime difference in CO$_2$ assimilation. Moreover, temperature contributed to the diurnal variability as well. For diurnal variations in transpiration, PAR and humidity changes played equal roles (Fig. 10b3).

Summarizing, the within-canopy variability in fluxes of CO$_2$ assimilation and transpiration was of a similar order of magnitude as the variability at annual or diurnal scales (Fig. 10), though typically slightly less than the latter. PAR-related variability within the canopy was of similar magnitude as the PAR-related variability at the annual cycle.
4 Discussion

For the evaluation of the model, gross primary production (GPP) was derived from the CO$_2$ flux determined with eddy covariance. To do so, respiration was substracted following Reichstein et al. (2005), however, the nighttime fluxes for Norunda did not always show a clear temperature dependence. Moreover, the comparison between the simulated canopy-scale transpiration and the H$_2$O flux determined with eddy covariance showed large deviations in winter and spring, most likely caused by the contribution of evaporation to the flux, as supported by the improved comparison between model and observations obtained with sapflow measurements (Lagergren and Lindroth, 2002). Unfortunately, sapflow measurements were available only for a nearby (distance approximately 500 m) site, and not for all years used in the model evaluation.

The model simulated CO$_2$ assimilation and transpiration fluxes as a function of atmospheric conditions, but did not account for soil conditions. Soil moisture limitations may affect the stomatal conductance, and thereby the fluxes of CO$_2$ assimilation and transpiration. Such water limitation occasionally occurred in the forest site studied here, mainly during summertime and for periods up to 15 days (Jansson et al. 1999; Grelle et al. 1999; Lagergren and Lindroth, 2002; Thum et al. 2007), but the non-water limited results are representative for this site for most of the year. For other sites, it may be considerably more important to capture this response.

Despite these drawbacks, simulated and observed CO$_2$ assimilation fluxes showed a good agreement, and simulated transpiration showed a reasonable agreement with the observed evapotranspiration.

The heterogeneity setup applied in this study captured the main drivers of photosynthesis and transpiration in the canopy, and showed that the vertical distribution of photosynthetically active radiation is the dominating source of vertical heterogeneity. The importance of sky conditions for the flux of CO$_2$ assimilation has been studied in other coniferous forests. Considerably higher photosynthetic light use efficiency, and thereby a stronger net carbon sink, was observed for cloudy days as compared with clear days for a Picea abies stand in
Czech Republic (Urban et al., 2007), for two *Picea sitchensis* stands in the UK (Dengel and Grace, 2010), and for a *Pinus sylvestris* stand in Finland (Law et al., 2002), in agreement with the results presented in this study.

Stomatal conductance was observed to be larger for cloudy conditions than for clear conditions (Dengel and Grace, 2010), for which the enhancement of light absorption and thereby photosynthesis is only one possible explanation: In general, cloudy conditions coincide with a relatively low vapour pressure deficit, which enhances stomatal conductance as well. Our results suggest that this is of little importance for the diurnal dynamics of photosynthesis, but it may be more important for the seasonal dynamics (as addressed by Dengel and Grace, 2010). Moreover, the higher contribution of blue light to the radiation under diffuse conditions has been suggested as an explanation for higher conductance (Dengel and Grace, 2010), but this was not confirmed for the *Picea abies* stand in Czech republic (Urban et al., 2012). These effects of spectral differences cannot be studied with our model in its current form, but may be interesting for future model development.

Variability within the CO$_2$ profile had little effect on the simulated canopy CO$_2$ assimilation rates in this study, mainly due to the counteracting effects of changes in ambient CO$_2$ and changes in stomatal conductance (and thereby leaf-internal CO$_2$). Brooks et al. (1997) estimated an increase of 5–6% in understorey CO$_2$ assimilation due to the elevated levels of CO$_2$ resulting from respiration for two boreal forest sites in Canada. However, the understorey is not likely to contribute substantially to the canopy GPP. Rough estimates of ground vegetation net primary production for this site (unpublished results) indicate a contribution of less than 10% to the total, which is in the range obtained for other Swedish forest sites (Berggren et al., 2002). We expect the contribution to GPP to be of similar magnitude.

Similarly, the temperature gradients observed for this site had little impact on the simulated photosynthesis and transpiration. It needs to be noted that the heterogeneity in temperature used here was derived from air temperature measurements in a number of layers, and is thus not entirely representative for leaf temperatures. Importantly, leaf temperatures are affected by fluxes of radiation, and sunlit and shaded leaves may thus exhibit different temperatures. Observations on individual leaf temperatures, and its distribution in the
canopy, are rare, and in order to investigate the importance of temperatures further, a leaf energy balance model may be used to compute temperatures.

Apart from the variations in the environmental driving variables, variations can occur in model parameters as well. The vertical gradient in light availability causes plants to distribute the leaf nitrogen content, and thereby the photosynthetic capacity, with a similar vertical gradient (Hirose and Werger, 1987; Givnish, 1988); in models this effect is often translated into an assumed optimum vertical distribution of nitrogen and photosynthetic capacity (De Pury and Farquhar, 1997). We have performed sensitivity tests applying an exponentially decreasing $V_{c,\text{max}}$ as suggested by De Pury and Farquhar (1997), resulting in an enhanced vertical gradient in $CO_2$ assimilation under all sky conditions, resulting in a further decrease of the light use efficiency. At the canopy scale, the light use was affected equally under clear or cloudy days, causing a reduction of 16% in LUE.

Similarly, temporal variations of photosynthetic capacities occur during the growing season, which was found for the Norunda forest site as well (Thum et al., 2008). However, Op de Beeck et al. (2010) found these seasonal variations to be relatively unimportant for the simulation of net ecosystem exchange in a Pinus sylvestris forest in Belgium. Apart from the vertical heterogeneity, there is a difference in these photosynthetic parameters as well between tree species. Pinus sylvestris has been observed to have generally higher rates of CO$_2$ assimilation than Picea abies, both for the Rubisco-limited (Eq. 4) and for the electron transport-limited (Eq. 5) regimes (e.g. Wullschleger, 1993; Thum et al., 2008). In the current model, this separation, which requires the interaction between two (or more) tree species for computing the light transfer, cannot be accounted for. Moreover, such a separation would enhance uncertainties related to the parameterization.

5 Conclusions

The simulations of fluxes of CO$_2$ assimilation and transpiration for a boreal coniferous forest in central Sweden revealed that the gradient of PAR is the main driver of vertical heterogeneity within the canopy. Because of the concave shape of the response of photosynthesis
to light, averaging of PAR in the canopy resulted in an overestimation of the photosynthesis rate. The other driving variables tested here (temperature, CO₂ concentration, humidity and wind speed) had little impact on the canopy-integrated rates of photosynthesis and transpiration, and these can be well-represented with a canopy-average value.

In models applied at regional or global scale, vertical heterogeneity in the driving variables is largely ignored. Whereas a canopy-average value is sufficient to represent temperature, CO₂ concentration and humidity, the distribution of PAR needs to be represented with more detail than a big-leaf approach, a result in accordance with earlier studies (Roderick et al., 2001; Alton et al., 2007; Knohl and Baldocchi, 2008; Mercado et al., 2009). A more detailed representation in large-scale models will enable a more realistic treatment of the effects of sky conditions on photosynthesis.

Given the size of the vertical variability of the fluxes of CO₂ assimilation and transpiration within the canopy, which was shown to be of similar magnitude as the variability occurring on diurnal or annual timescales, the impact of forest structure on microclimatic conditions should receive more attention in large-scale models. For studies addressing changes over decades or more, not only physiological changes should be considered, but the changes in canopy structure and hence in micrometeorological conditions may affect exchange processes as well.

**Appendix A: Description of light extinction scheme**

Light extinction was simulated with a numerical scheme that builds on existing theory, representing the heterogeneity in the canopy due to sunlit and shaded fractions (which was introduced by Duncan et al., 1967), vertical layering (used for representing the vertical heterogeneity by e.g. Monteith, 1965; Duncan et al., 1967; Cowan, 1968) and leaf angle distribution (addressed with numerical approximations by Goudriaan, 1977, 1988). However, in contrast to existing schemes, we refrain from averaging intermediate results (e.g. the distribution of insolation levels obtained from varying leaf angles) over the canopy, so that the distribution obtained represents the full distribution of light at the leaf level.
A1 Leaf angle distribution

Leaf orientation is represented with two dimensions: an azimuth angle $\phi_l$ ($0 \leq \phi_l < 360^\circ$) and a zenith angle $\theta_l$ ($0 \leq \theta_l < 90^\circ$) of the leaf normal. The distribution of leaf orientation in these two dimensions is represented in a discrete manner as a lattice with $n_{l\phi} \times n_{l\theta}$ combinations of azimuth and zenith angles. The spacing in $\phi$ and $\theta$ is done so that each combination $(\phi_l, \theta_l)$ has an equal likelihood, and represents $1/(n_{l\phi} n_{l\theta})$ of the complete leaf area. For the simulations in this study, we applied a spherical (or isotropic) leaf angle distribution, which is obtained with a uniform distribution (equal spacing) of the azimuth angles $\phi_l$ over the entire $360^\circ$, and a spacing at equal distances between the cosines of the angles for the zenith angles $\theta_l$, so that the increasing density towards the horizon compensates for the increasing area of the sphere.

A2 Distribution of sunlight and skylight

In the model, sunlight is described as a point source with a given azimuth and zenith angle $\phi_{\text{sun}}$ and $\theta_{\text{sun}}$, respectively, together with a photosynthetic quantum flux density $I_{\text{sun}}$ (in mol m$^{-2}$ s$^{-1}$). Similar to the leaf angles, skylight is described with a distribution of azimuth and zenith angles over the hemisphere. In contrast to the leaf angle distribution, however, azimuth and zenith angles are spaced equally, resulting in $n_{i\phi} \times n_{i\theta}$ combinations of $(\phi_s, \theta_s)$, and the intensity for each combination is given by $I_s(\phi_s, \theta_s)$. The distribution of the light over sunlight (direct radiation) and skylight (diffuse radiation), as well as the distribution of skylight over all angles $(\phi_s, \theta_s)$ is determined by sky conditions.

To accommodate upward scattering of light within the canopy, a second hemisphere was introduced, which has the same number and distribution of azimuth and zenith angle classes.

A3 Light absorption

The canopy is represented with $n_h$ layers, and light absorption, reflection and transmission in the canopy are calculated by combining the direct radiation and the distribution of skylight radiation over the sky angles (Sect. A2) for each of the leaf orientations (Sect. A1) in
each layer, thus resulting in a probability density function of leaf-level absorbed radiation. Below, we will describe the processes at the leaf level first, followed by a description of the aggregation of these processes to canopy scale.

The leaf angle distribution is assumed to be spherical (or isotropic), meaning that the leaf area in layer \( h \), \( A_h \), is distributed equally over all leaf angle orientations \((\phi_l, \theta_l)\), which is commonly used to describe a generic canopy in large-scale models (Cowan [1968], Leuning et al. [1995]). The leaf area was divided into a sunlit and a shaded fraction (computation of these fractions will be explained further down). This leaf area intercepts a fraction of the radiation that comes from a given direction \((\phi_s, \theta_s)\) proportional to its area, and it depends on the angle between the leaf normal and the direction of the radiation:

\[
f_{\text{int}, s, l, h} = \frac{\sin \gamma_{s,l} L_h}{\cos \theta_s n_l \phi_l n_l \theta_l}
\]

(A1)

In this equation, the angle between beam and leaf, \( \gamma_{s,l} \), can be computed from the inner product of the vectors of the beam and the leaf normal, which can be expressed based on their azimuth angles \( \phi \) and zenith angles \( \theta \) (see e.g. Ross [1981]):

\[
\gamma_{s,l} = \arcsin(\cos \phi_s \sin \theta_s \cos \phi_l \sin \theta_l + \sin \phi_s \sin \theta_s \sin \phi_l \sin \theta_l + \cos \theta_s \cos \theta_l)
\]

(A2)

This intercepted fraction of the radiation, \( f_{\text{int}, s, l, h} \) (Eq. A1) is absorbed, reflected or transmitted by the leaf, which is distributed according to constant fractions. To obtain the total amount of intercepted diffuse radiation by the leaf \( I_{\text{dif}, l, h} \) (which represents intercepted radiation by the leaf area with orientation \( l \) in layer \( h \)), these fractions, multiplied with the light intensities \( I_{\text{dif}} \), need to be integrated over all skylight angles:

\[
I_{\text{dif}, l, h} = \sum_{s=1}^{n_s} \left( f_{\text{int}, s, l, h} I_{\text{dif}, s} \sin \gamma_{s,l} \right)
\]

(A3)

This integration is performed both for the upper hemisphere and for the lower one to accommodate fluxes from below due to scattering.
Similarly, the fraction of intercepted beam radiation can be computed from Eq. (A1) by replacing the skylight angles with sunlight angles, which results in the beam radiation intercepted by a leaf with orientation $l$ in layer $h$ of

$$I_{\text{sun},l,h} = f_{\text{int,sun},l} I_{\text{sun}} \sin \gamma_{\text{sun},l}$$

The total amount of intercepted radiation by the leaf area with orientation $l$ in layer $h$, which can be written as $I_{\text{sun},l,h} + f_{\text{sun},h} I_{\text{dif},l,h}$ for sunlit leaves, and $(1 - f_{\text{sun},h}) I_{\text{dif},l,h}$ for shaded leaves, is distributed over the sunlit and shaded leaf area, respectively, to obtain the radiation intensity at the leaf level:

$$I_{\text{int,sunlit},l,h} = \frac{I_{\text{sun},l,h} + f_{\text{sun},h} I_{\text{dif},l,h}}{f_{\text{sun},h} n_\phi n_\theta L_h}$$

$$I_{\text{int,shaded},l,h} = \frac{I_{\text{dif},l,h}}{n_\phi n_\theta L_h}$$

The fractions of sunlit and shaded leaves are computed from the same theory: the total interception of radiation in layer $h$ is calculated by integrating Eq. (A1) over all leaf angles:

$$f_{\text{int},h} = \sum_{l=1}^{n_\phi n_\theta} f_{\text{int},l}(\phi_l, \theta_l)$$

The fraction of sunlit leaves for each layer $h$ is computed from the shading in the layers above, assuming the leaves to be distributed randomly in space (no spatial aggregation), similar to Monteith (1965):

$$f_{\text{sun},h} = (1 - f_{\text{int}})^{h-1}$$

This results in an exponential profile of the sunlit fraction in the canopy.

The absorbed photon flux densities at the leaf level, obtained from Eqs. (A5 and A6) are used to compute CO$_2$ assimilation (see Sect. 2.2.2). The unintercepted radiation passes
the layer without adjustments to the angular distribution. The radiation transmitted and reflected is distributed again over the two hemispheres of diffuse radiation. The leaf surface is assumed to be a Lambertian scatterer: The leaf reflects the largest flux in the direction of the leaf normal, and transmits the largest flux in the opposite direction. When the diffuse light reaches the leaf surface from below, transmittance is pointing in the direction of the leaf normal, and reflectance in the opposite direction.

These leaf-level processes can be aggregated to the canopy level. For all leaf orientations \( j \) in all layers \( h \), absorptance, reflectance and transmittance from the layer as a whole can be determined as described above. Within a layer, the scattering in all directions of the upward and downward pointing hemisphere is integrated over all leaf orientations, and these amounts are added to the fluxes of diffuse radiation that pass through the layer without interference with the leaves.

The distribution of this scattered light over the canopy is solved iteratively by computing the total absorption of both downward and upward pointing fluxes for all layers first from top to bottom, then from bottom to top. This is repeated until the remaining scattered light within the canopy is lower than a pre-defined minimum residual (0.001 %). This way of distributing the light in the model canopy is relatively efficient, it requires a few iterations to reach this residual.

The two-directional treatment of scattering is similar as used in the models by Norman et al. (1971) and Norman (1975). The model described here contrasts with that approach, however, in the explicit description of angular scattering, and the numerical solution that is used to obtain that.

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References


Table 1. Parameter values for the photosynthesis-stomatal conductance model.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
<th>Unit</th>
<th>Reference</th>
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</thead>
<tbody>
<tr>
<td>maximum rate of electron transport at 298 K</td>
<td>$J_{\text{max}}$</td>
<td>$144 \times 10^{-6}$</td>
<td>mol m$^{-2}$ s$^{-1}$</td>
<td>Thum et al. (2008)</td>
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<td>maximum rate of Rubisco activity at 298 K</td>
<td>$V_{c,max}$</td>
<td>$25.4 \times 10^{-6}$</td>
<td>mol m$^{-2}$ s$^{-1}$</td>
<td>Thum et al. (2008)</td>
</tr>
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<td>activation energy for electron transport</td>
<td>$E(J)$</td>
<td>$88.0 \times 10^3$</td>
<td>J mol$^{-1}$</td>
<td>Thum et al. (2008)</td>
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<td>activation energy for Rubisco activity</td>
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<td>$73.6 \times 10^3$</td>
<td>J mol$^{-1}$</td>
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<td>empirical curvature factor</td>
<td>$\theta$</td>
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<td>Von Caemmerer (2000)</td>
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<td>slope in stomatal conductance equation</td>
<td>$k$</td>
<td>9.0</td>
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<td>intercept in stomatal conductance equation</td>
<td>$b$</td>
<td>0.01</td>
<td>mol m$^{-2}$ s$^{-1}$</td>
<td>Collatz et al. (1991)</td>
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Table 2. Overview of the simulations performed for this study.

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
<th>PAR</th>
<th>CO₂</th>
<th>temperature</th>
<th>humidity</th>
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<td>profile</td>
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<td>Profile, but homogeneous PAR within layer</td>
<td>layer-averaged profile</td>
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<td>profile</td>
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<td>profile</td>
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<td>canopy average</td>
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<td>canopy average</td>
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<td>profile</td>
<td>diurnally-averaged profile</td>
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<tr>
<td>DHET_CO2</td>
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<tr>
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<tr>
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<tr>
<td>Annually-averaged conditions for all parameters except one</td>
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<tr>
<td>AHET_PAR</td>
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<td>profile</td>
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<td>annually-averaged profile</td>
</tr>
<tr>
<td>AHET_CO2</td>
<td>Homogeneous in annual cycle except for CO₂</td>
<td>annually-averaged profile</td>
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<tr>
<td>AHET_TEM</td>
<td>Homogeneous in annual cycle except for temperature</td>
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<td>AHET_HUM</td>
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Figure 1. Relationship between relative amount of incoming radiation at surface (as fraction of top-of-atmosphere radiation) $f_{\text{trans}}$ and diffuse fraction $f_{\text{dif}}$. Shown are data between June 2004 and December 2010. Data points with surface fractions $\leq 0$ or $> 1$, as well as data points with diffuse fractions $< 0.1$ or $> 1.25$, were omitted. The original relationship by Spitters et al. (1986) (dashed, $R^2 = 0.61$) as well as the reparameterized relationship (full line, $R^2 = 0.66$) are displayed.
Figure 2. Annual cycle of simulated and observed daily mean (a) CO₂ assimilation and (b) transpiration for the years 1999–2002. Note that the photosynthesis parameterization was based on observations from 2001 (Thum et al., 2008). Days with less than 45 (out of 48) half-hourly observations were omitted. (c) 10 day running mean of simulated and observed daily mean transpiration for 1999.
Figure 3. Diurnal cycle of simulated and observed (a) CO$_2$ assimilation and (b) transpiration, averaged for four seasons with data from 1999, 2000 and 2002.
Figure 4. Overview of vertical gradients in the canopy for three periods: 18–22 May 1999 (case 1), 24–28 August 1999 (case 2) and 8–12 September 1999 (case 3). Shown are gradients of (a) leaf-level photosynthetically absorbed radiation (PAR), averaged per canopy layer; (b) atmospheric CO₂ concentration; (c) air temperature; (d) relative humidity; (e) simulated CO₂ assimilation and (f) simulated transpiration, as well as the canopy-integrated (g) CO₂ assimilation and (h) transpiration, compared with observed fluxes (the canopy-integrated fluxes in (g) and (h) are expressed per ground area). The gradient in PAR originates from detailed simulation of the light transfer in the canopy. Gradients in CO₂, air temperature and relative humidity were obtained from linear interpolation of measurements at 5–6 levels in and directly above the canopy.
Figure 5. Effect of temperature and humidity conditions on transpiration for the case period 18 to 22 May 1999: (a) Above-canopy (28.0 m) and within-canopy (8.5 m) relative humidity; (b) above-canopy and within-canopy temperature; (c) Simulated profile of stomatal conductance, averaged per layer; (d) Simulated transpiration, as well as observed H₂O flux; (e) Relative deviation in simulated transpiration when applying above-canopy humidity (simulation HOM_HUM_AC); (f) Relative deviation in simulated transpiration when applying within-canopy humidity (simulation HOM_HUM_IC).
**Figure 6.** Light conditions and its distribution in the canopy for the case period 24 to 28 August 1999:

(a) Above-canopy photosynthetically active radiation (PAR, separated in direct and diffuse components);
(b) Light use efficiency (LUE, CO₂ assimilation per unit of absorbed PAR) for the full heterogeneity case (simulation HET);
(c) Light use efficiency for a setup that does not separate sunlit and shaded leaves (simulation HOM_PAR_LAYER);
(d) Light use efficiency for a setup that separates neither sunlit and shaded leaves, nor layers (simulation HOM_PAR);
(e) Canopy-scale light use efficiency (CO₂ assimilation per unit of incoming PAR).
Figure 7. Vertical distribution of (a) light absorption and (b) CO$_2$ assimilation in the canopy (expressed per area leaf), separated for clear time steps ($f_{\text{dif}} < 0.5$) with a solar angle $\beta > 30^\circ$ ($n = 1418$), clear time steps with a solar angle $\beta < 30^\circ$ ($n = 1382$), and cloudy time steps ($f_{\text{dif}} \geq 0.5$, $n = 4888$) for 1999. The average distribution within a layer in (b) is represented by the median, 25–75% percentile, and 5–95% percentile.
**Figure 8.** Daily integrated flux of CO₂ assimilation as a function of the daily integrated photosynthetically active radiation (PAR) separated for clear days ($f_{\text{dif}} < 0.5$) and cloudy days ($f_{\text{dif}} \geq 0.5$). Shown are results from the full heterogeneity simulation and the simulation without heterogeneity in light, as well as the observation-derived CO₂ assimilation flux. Days with less than 45 (out of 48) half-hourly observations were omitted. Regression lines (obtained with least-squares linear regression through the origin) are shown for the three data sets as well (full lines corresponding to the clear days, dashed lines to the cloudy days).
Figure 9. Changes of the within-canopy CO₂ profile, and its impact on CO₂ assimilation, illustrated for 12 September 1999: (a) observed changes in PAR and above-canopy (28 m) CO₂ concentration; (b) Simulated and observation-derived CO₂ assimilation; (c) within-canopy CO₂ profile for 9 selected times; (d) relative deviations from simulated CO₂ assimilation when applying average (simulation HOM_CO2) or above-canopy (simulation HOM_CO2_AC) CO₂ concentration instead of the distribution displayed in (c); (e) simulated CO₂ assimilation for simulations applying the CO₂ distribution as well as canopy-average or above-canopy CO₂ concentration. For (d) and (e), only daytime panels were shown.
Figure 10. Explanation of variability of simulated (a) CO$_2$ assimilation and (b) transpiration for (1) vertical variability ($n = 25$), (2) annual variability ($n = 277$) and (3) diurnal variability ($n = 48$). Shown are the distributions (box indicates median and 25–75 % percentile, whiskers indicate full distribution) obtained from the full simulation, and from simulations that exhibit variability only for one parameter (see text for details).