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Uncertainty analysis of eddy covariance CO₂ flux measurements for different EC tower distances using an extended two-tower approach

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BGD

11, 11943–11983, 2014

**Uncertainty analysis
of eddy covariance
CO₂ flux
measurements**

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Abstract

The use of eddy covariance CO₂ flux measurements in data assimilation and other applications requires an estimate of the random uncertainty. In previous studies, the two-tower approach has yielded robust uncertainty estimates, but care must be taken to meet the often competing requirements of statistical independence (non-overlapping footprints) and ecosystem homogeneity when choosing an appropriate tower distance. The role of the tower distance was investigated with help of a roving station separated between 8 m and 34 km from a permanent EC grassland station. Random uncertainty was estimated for five separation distances with an extended two-tower approach which removed systematic differences of CO₂ fluxes measured at two EC towers. This analysis was made for a dataset where (i) only similar weather conditions at the two sites were included and (ii) an unfiltered one. The extended approach, applied to weather-filtered data for separation distances of 95 m and 173 m gave uncertainty estimates in best correspondence with the independent reference method. The introduced correction for systematic flux differences considerably reduced the overestimation of the two-tower based uncertainty of net CO₂ flux measurements, e.g. caused by different environmental conditions at both EC towers. It is concluded that the extension of the two-tower approach can help to receive more reliable uncertainty estimates because systematic differences of measured CO₂ fluxes which are not part of random error are filtered out.

1 Introduction

Eddy covariance (EC) measurements of the CO₂ flux are commonly used to analyze the interactions between terrestrial ecosystems and the atmosphere. This is crucial for the understanding of climate-ecosystem feedbacks as well as for an improved representation of vegetation and related processes (photosynthesis, respiration, transpiration, etc.) in land surface models. EC fluxes are used to evaluate and to improve

BGD

11, 11943–11983, 2014

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



the underestimation of turbulent energy fluxes and/or an overestimation of the available energy (Wilson et al., 2002). The latter is closely linked to (c) an omission of low or high frequency turbulent fluxes (Foken, 2008; Wilson et al., 2002) and the situation that (d) land surface heterogeneity can even on flat terrain induce advection (Finnigan, 2008; Foken et al., 2006; Liu et al., 2006; Panin et al., 1998).

Sometimes, measured energy fluxes are corrected for EBD (e.g. Todd et al., 2000; Twine et al., 2000; Hendricks Franssen et al., 2010). Because atmospheric CO₂ transport processes are very similar to those of latent and sensible heat and because their calculation with the eddy covariance method is based on the same physical assumptions, the energy balance closure problem might also result in a systematic underestimation of errors of the CO₂ fluxes (Mauder et al., 2010; Foken, 2008; Wilson et al., 2002). However, the correction of measured CO₂ fluxes with the EBD is not widely accepted, because the connection between energy- and CO₂ deficits has not been firmly proven and depends on the actual reason for the imbalance (Barr et al., 2006; Foken et al., 2006; Wilson et al., 2002). In a comparison of EC and chamber measurements, Graf et al. (2013) found different biases for CO₂ flux and latent heat flux, and only the latter showed some relation to the EBD of the EC systems. Oren et al. (2006) also pointed out that errors related to the EBD do not necessarily translate to errors in measured CO₂ which is supported by findings of Scanlon and Albertson (2001).

After a possible correction of the EC flux data for systematic errors a random error will remain which originates e.g. from instrumentation errors, flux footprint heterogeneity or turbulence sampling errors (Flanagan and Johnson, 2005). The uncertainty cannot be corrected or predicted like systematic errors due to its random character but can be quantified by statistical analysis and characterized by probability distribution functions (Richardson et al., 2012). Errors due to flux footprint heterogeneity are related to the simplifying assumption that the flux footprint originates from one (constant) footprint area within the measurement interval. However, temporal variability of e.g. wind direction, wind speed and atmospheric stability cause temporal variations of the the footprint area. Turbulence sampling errors are related to the fact that turbulence

BGD

11, 11943–11983, 2014

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



uncertainty is no longer required. Hence, the raw-data based uncertainty estimate is not affected by not fulfilled underlying assumptions such as similar environmental conditions or a correct simulation model. However, because many data users do not have access to the raw-data but to processed EC data only, random error estimates by the raw-data based approach are not commonly available. Therefore a two-tower based approach is still of great potential. Important advantages of the two-tower approach are (1) its simplicity and user friendliness, (2) its usability for relatively short non gap-filled time series of several months, and (3) the independence of a model. Given the fact that site specific, adequate uncertainty estimates for eddy covariance data are very important but still often neglected due to a lack of resources, we are aiming to advance the two-tower approach so that it can also be applied if environmental conditions at both eddy covariance towers are not very similar.

The main objectives of this study were (1) to analyze the effect of the EC tower distance on the two-tower based CO₂ flux measurement uncertainty estimate and (2) to extend the two-tower approach with a simple correction term that corrects for systematic differences in CO₂ fluxes measured at the two sites. This extension follows the idea of the extended two-tower approach for the uncertainty estimation of energy fluxes presented in Kessomkiat et al. (2013). The correction step is important for providing a more reliable random error estimate. In correspondence with these objectives we analyzed the following questions: what is an appropriate EC tower distance to get a reliable two-tower based uncertainty estimate? Can the random error be quantified in reasonable manner with the extended two-tower approach, even though environmental conditions at both EC towers are clearly not identical? The total random error estimated with the raw-data based method (Mauder et al., 2013) was used as a reference to evaluate our extended two-tower approach based results.

EC conversions and corrections such as e.g. correction of spectral loss and correction for density fluctuations (Webb et al., 1980). It includes tests on high frequency data (site specific plausibility limits, statistical spike detection) as well as on processed half hourly fluxes such as stationarity and integral turbulence tests, footprint analysis (Kormann and Meixner, 2001) and uncertainty estimates for final fluxes. All tests lead to a standardized quality flagging with data flagged as high, moderate or low quality data. For this analysis only high and moderate quality data were used, while low quality data were treated as missing values. To avoid introduction of additional uncertainty no gap filling was performed.

3.3 Uncertainty estimation based on the two-tower approach

The two-tower approach (Hollinger and Richardson, 2005; Hollinger et al., 2004; Richardson et al., 2006) defines the random error of NEE eddy covariance measurements as the standard deviation $\sigma(\delta)$ of the difference between the CO₂ fluxes [$\mu\text{mol m}^{-2} \text{s}^{-1}$] simultaneously measured at two different EC towers (NEE₁, NEE₂):

$$\sigma(\delta) = \frac{\sigma(\text{NEE}_1 - \text{NEE}_2)}{\sqrt{2}} \quad (3)$$

Based on Eq. (3) we calculated the two-tower based uncertainty estimates using the NEE₁ data measured at the permanent EC tower in Rollesbroich (EC1) and the NEE₂ data of a second tower which was either the rowing station (EC2) or – in case of the 32 km EC tower distance – another permanent EC tower (EC3, Table 1). For comparison, the measurement uncertainty $\sigma(\delta)$ was calculated separately for each EC tower distance (Table 1) and independently for each of the following schemes:

1. the classical two-tower approach (Hollinger and Richardson, 2005; Hollinger et al., 2004; Richardson et al., 2006)

BGD

11, 11943–11983, 2014

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

2. the classical two-tower approach including a weather-filter previously applied to the actual uncertainty estimation procedure (conditions of weather filter summarized in Sect. 3.5)
3. the extended two-tower approach with an added correction for systematic flux differences (sfd-correction; Sect. 3.4), without weather-filter
4. the extended two-tower approach with weather-filter

The uncertainty estimate of the two-tower approach is obtained by dividing the NEE data series into several groups (“bins”) according to the flux magnitude and then using Eq. (3) to calculate the standard deviation $\sigma(\delta)$ for each group (Richardson et al., 2006). Finally, a linear regression function between the flux magnitude and the standard deviation can be derived. The linear correlation of the uncertainty and the flux magnitude can be explained by the fact that the flux magnitude is a main driving factor for the random error and can explain about 63 % of the variance in the CO₂ flux error as shown in a case study by Richardson et al. (2006). Accordingly, we calculated the standard deviation $\sigma(\delta)$ [$\mu\text{mol m}^{-2} \text{s}^{-1}$] based on 12 groups of the CO₂ flux magnitude; six groups for positive and six groups for negative fluxes. Fixed class limits for the flux magnitude would have led to a different number of samples in each group. Separately for positive and negative NEE values, the data were sorted and divided into 6 groups with an equal amount of half hourly data. For each single group the standard deviation $\sigma(\delta)$ was calculated using the single half-hourly flux differences of NEE₁ and NEE₂. The corresponding mean NEE magnitude for each group member was determined by averaging all half-hourly means of NEE₁ and NEE₂ in the respective group. Then, the linear regression equation was derived separately for negative and positive NEE values using the 6 calculated standard deviations $\sigma(\delta)$ and the 6 mean NEE values. This procedure was carried out for each dataset of the five EC tower distances and again for each of the four uncertainty estimation methods so that altogether 20 × 2 linear regression equations were derived. The significance of the correlation between the NEE magnitudes and the standard deviations $\sigma(\delta)$ was tested with the p value determined

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



statistically be separated quite easily from random differences of the EC flux measurements is their fundamentally different behavior in time: random differences fluctuate highly in time whereas systematic differences tend to be constant over time or show slow variations. The sfd-correction introduced is similar to the second correction step in Kessomkiat et al. (2013, Eq. 6 therein), but adapted to the measured NEE instead of latent and sensible heat fluxes. To define the correction term it was necessary to find a moving averaging interval that is long enough to exclude most of the random error part but short enough to consider daily changes of these systematic flux differences. Twelve hours (including 24 half hourly time steps) were found to be a suitable time interval to calculate the running mean for the sfd-correction term. This period also corresponds well with the coefficient of spatial variation (CV) which Oren et al. (2006) found to be stable after ~ 7 daytime and ~ 12 nighttime hours in case of a uniform pine plantation.

For each moving averaging interval, the mean NEE_{12h} of one EC tower (separately for EC1 and EC2) [$\mu\text{mol m}^{-2} \text{s}^{-1}$] and the mean CO₂ flux averaged over both EC towers $NEE_{2T_{12h}}$ [$\mu\text{mol m}^{-2} \text{s}^{-1}$] were calculated to define the sfdcorrection term which was used to calculate the corrected NEE_{corr} [$\mu\text{mol m}^{-2} \text{s}^{-1}$]:

$$NEE_{\text{corr}} = \frac{NEE_{2T_{12h}}}{NEE_{12h}} \times NEE \quad (4)$$

NEE is the single half-hourly, processed NEE value [$\mu\text{mol m}^{-2} \text{s}^{-1}$] of one EC tower. Only if both NEE data, NEE_{EC1} for the permanent EC1 tower and NEE_{EC2} for the second tower, were available at a particular half hourly time step and if both values were either positive or negative the respective data were included to calculate the sfd-correction term. The correction was done separately for positive and negative fluxes, due to the different sources, properties and magnitudes of the CO₂ flux measurements and different errors for daytime (negative) and nighttime (positive) fluxes (e.g. Goulden et al., 1996; Oren et al., 2006; Wilson et al., 2002). NEE_{corr} was calculated only if at

ing measurement period (Table 1) was calculated by dividing the number of NEE data with overlapping footprints ($\times 100$) by the total number of NEE data available for the same measurement period. This implies that the calculated average footprint overlap [%] for a particular EC tower distance is not the total percentage area of footprint overlap but the percentage of time steps CO_2 fluxes originate from nearly the same area (defined by target 1 and target 2).

3.7 Comparison measures

To compare and evaluate the two-tower based uncertainty estimates, we calculated random error estimates based on Mauder et al. (2013) as a reference. This reference method is independent of the two-tower based approach, because data of only one EC tower are used to quantify the random error of the measured fluxes and raw data instead of the processed fluxes are used. The raw-data based random error estimates – the instrumental noise $\sigma_{\text{COV}}^{\text{noise}}$ and the stochastic error $\sigma_{\text{COV}}^{\text{stoch}}$ – were calculated independently. Generally, the instrument noise $\sigma_{\text{COV}}^{\text{noise}}$ was considerably lower than the stochastic error $\sigma_{\text{COV}}^{\text{stoch}}$. The total raw-data based random error σ_{COV} was calculated by adding $\sigma_{\text{COV}}^{\text{noise}}$ and $\sigma_{\text{COV}}^{\text{stoch}}$. The absolute random error σ_{COV} [$\mu\text{mol m}^{-2} \text{s}^{-1}$] used for the evaluation of the two-tower based random error estimates was calculated by averaging the single raw-data based NEE uncertainty values measured at the permanent EC1 tower in Rollesbroich. In order to be consistent with the two-tower based calculations, exactly the same half hourly time steps of the EC1 data series used for the two-tower based uncertainty estimation were used to calculate the corresponding mean reference values σ_{COV} . As indicator for the performance of the two-tower based uncertainty estimation schemes applied for the five different EC tower distances, the relative difference $\Delta\sigma_{\text{COV}}$ [%] of a two-tower based uncertainty value [$\mu\text{mol m}^{-2} \text{s}^{-1}$] and the reference value σ_{COV} [$\mu\text{mol m}^{-2} \text{s}^{-1}$] was calculated:

$$\Delta\sigma_{\text{COV}}[\%] = \frac{\sigma(\delta) - \sigma_{\text{COV}}}{\sigma_{\text{COV}}} \times 100 \quad (5)$$

the weather filter applied. The effect of the weather-filter on the uncertainty estimates of the shorter EC tower distances was very minor (Table 2). As shown in Table 2 the uncertainty estimates $\sigma(\delta)_{\text{corr, f}}$ determined with the extended two-tower approach are nearly identical to the independent reference values σ_{cov} for the EC tower distances 95 m and 173 m suggesting that those distances were most suitable for the application of the extended two-tower approach. The NEE uncertainty $\sigma(\delta)_{\text{corr, f}}$ estimated for the grassland site Rollesbroich agree well with the NEE uncertainty values for grassland sites by Richardson et al. (2006), ranging between $\sim 0.2 \mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$ in winter months and $\sim 1 \mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$ in summer months.

4.3 Discussion

The results show that the two-tower based uncertainty estimates (both classical and extended two-tower approach) were smallest for the 8 m distance. This can be explained with the results of the footprint analysis: while the percentage footprint overlap is 20.4% for the 95 m EC tower distance and only 0.9% for the 173 m EC tower distance, it is 61.2% for the 8 m EC tower distance. The more frequent overlapping of the 8 m distance footprint areas is associated with a more frequent sampling of the same eddies. As a consequence part of the random error was not captured with the two-tower approach. If EC towers are located very close to each other ($< 10 \text{ m}$) and the footprint overlap approaches 100%, only instrumental errors and stochasticity related sampling of small eddies will be captured with the two-tower based uncertainty estimate. Because the EC measurements are statistically not independent if the footprints are overlapping, the classical EC tower method is not expected to give reliable uncertainty estimates for very short EC tower distances (Hollinger and Richardson, 2005; Hollinger et al., 2004). However, without applying the sfd-correction, the mean uncertainty estimate $\sigma(\delta)$ was still higher than the raw-data based reference value which includes both the instrumental noise $\sigma_{\text{cov}}^{\text{noise}}$ and the stochastic error $\sigma_{\text{cov}}^{\text{stoch}}$. The raw-data based instrumental noise $\sigma_{\text{cov}}^{\text{noise}}$ itself was only $0.04 \mu\text{mol m}^{-2} \text{ s}^{-1}$

sensor network (“SoilNet”; Bogena et al., 2009), calibrated for the Rollesbroich site by Qu et al. (2013). This data shows that both soil moisture and soil temperature are heterogeneous within the site (Qu et al., 2014). The effect of soil moisture, soil temperature and soil properties on CO₂ fluxes (respiration mainly) is well known (e.g. Herbst et al., 2009; Flanagan and Johnson, 2005; Xu et al., 2004; Lloyd and Taylor, 1994; Orchard and Cook, 1983) as well as the role of grassland management (e.g. Allard et al., 2007). It is expected that systematic differences in measured NEE caused by those spatial variable land surface properties are stronger during night than during day since they affect respiration more directly than photosynthesis which also agrees with the findings in Oren et al. (2006). However, since our focus was on estimating the total uncertainty of measured NEE and since it is expected that the sfd-correction also captures systematic differences in weather conditions (e.g. temperature, solar radiation) that strongly determine the magnitude of carbon uptake during day, we did not distinguish between the uncertainty of daytime and nighttime data. At very large EC tower distances (20.5 km, 34 km) footprints were not overlapping and the environmental conditions were considerably different; in particular for the EC tower setup Rollesbroich/Merzenhausen with different land use (grassland/crop) and climate conditions (Sect. 2). For those distances, the relative difference $\Delta\sigma_{\text{cov}}$ between the reference value σ_{cov} and $\sigma(\delta)$ (classical two-tower approach) was much larger than for the relative difference $\Delta\sigma_{\text{cov}}$ between σ_{cov} and $\sigma(\delta)_{\text{corr, f}}$ (extended two-tower approach). The uncertainty estimate improved by 80 % for the 20.5 km distance and 82 % for the 34 km if both sfd-correction and weather filter were used. However, after applying the sfd-correction and the weather-filtering, the mean uncertainty estimate for the large EC tower distances was still 33.2 % and 49.6 % higher than the raw-data based reference value (Table 2) suggesting that these large EC tower distances were less suitable for estimating the NEE uncertainty on the basis of the extended two-tower approach compared to the 95 m and 173 m distance. The absolute corrected and weather-filtered uncertainty value $\sigma(\delta)_{\text{corr, f}}$ [$\mu\text{mol m}^{-2} \text{s}^{-1}$] was slightly lower for the 34 km EC tower distance than for the 20.5 km EC tower distance (Table 2), which is counterintuitive.

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

they still contain the random error part that cannot be corrected or filtered out. Therefore, completely correcting the difference in mean NEE slightly overcorrects systematic differences in NEE.

In general, the weather-filter did not improve the uncertainty estimates as much as the *sfd*-correction. However, this does not imply that differences in weather conditions are negligible when applying the extended two-tower approach for larger EC tower distances. In fact the systematic part of measured EC flux differences between both towers caused by (steady, systematic) among-site differences in weather conditions were already partly captured with the *sfd*-correction. In contrast such systematic differences were difficult to capture with the weather-filter because it was not possible to define weather-filter criteria that allow the assumption of data similarity without reducing the dataset too much for further meaningful analysis.

5 Conclusions

When estimating the uncertainty of eddy covariance net CO₂ flux (NEE) measurements with a two-tower based approach it is important to consider that the basic assumptions of identical environmental conditions (including weather conditions and land surface properties) on the one hand and non-overlapping footprints on the other hand are contradicting and impossible to fulfill. If the two EC towers are located in a distance large enough to ensure non overlapping footprints, different environmental conditions at both EC towers can cause systematic differences of the simultaneously measured fluxes that should not be included in the uncertainty estimate. This study for the grassland site Rollesbroich in Germany showed that the extended two-tower approach which includes a correction for systematic flux differences (*sfd*-correction) can be used to derive more reliable (less overestimated) uncertainty estimates compared to the classical two-tower approach. An advantage of this extended two-tower approach is its simplicity and the fact that there is no need to quantify the differences in environmental conditions (which is usually not possible due to a lack of data). Comparing the uncertainty estimates for

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



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Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



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BGD

11, 11943–11983, 2014

**Uncertainty analysis
of eddy covariance
CO₂ flux
measurements**

H. Post et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



BGD

11, 11943–11983, 2014

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Table 1. Measurement periods and locations of the permanent EC towers in Rollesbroich (EC1) and Merzenhausen (EC3) and the roving station (EC2).

	Coordinates	Sitename	Distance to EC1	Measurement period	alt. (m)
EC1	50.6219142° N/6.3041256° E	Rollesbroich	–	13 May 2011–15 Jul 2013	514.7
EC2	50.6219012° N/6.3040107° E	Rollesbroich	8 m	29 Jul 2011–6 Oct 2011	514.8
	50.6219012° N/6.3040107° E			5 Mar 2013–15 May 2013	
	50.6217990° N/6.3027962° E	Rollesbroich	95 m	7 Oct 2011–15 May 2012	516.3
	50.6210472° N/6.3042120° E			1 Jul 2013–15 Jul 2013	517.3
	50.6217290° N/6.3016925° E	Rollesbroich	173 m	24 May 2012–14 Aug 2012	517.1
	50.5027500° N/6.5254170° E	Kall-Sistig	20.5 km	14 Aug 2012–1 Nov 2012	498.0
	15 May 2013–1 Jul 2013				
EC3	50.9297879° N/6.2969924° E	Merzenhausen	34 km	10 May 2011–16 Jul 2013	93.3

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Table 2. Mean NEE uncertainty [$\mu\text{mol m}^{-2} \text{s}^{-1}$] for five EC tower distances estimated with the classical two-tower approach, with and without including a weather-filter ($\sigma(\delta)$, $\sigma(\delta)_f$), and with the extended two-tower approach (sfd-correction), also with and without including a weather-filter ($\sigma(\delta)_{\text{corr}}$, $\sigma(\delta)_{\text{corr},f}$). The table also provides the random error σ_{cov} [$\mu\text{mol m}^{-2} \text{s}^{-1}$] estimated with the raw-data based reference method (Mauder et al., 2013).

EC tower distance	N	$\sigma(\delta)$ ($\Delta\sigma_{\text{cov}}$)	$\sigma(\delta)_f$ ($\Delta\sigma_{\text{cov}}$)	$\sigma(\delta)_{\text{corr}}$ ($\Delta\sigma_{\text{cov}}$)	$\sigma(\delta)_{\text{corr},f}$ ($\Delta\sigma_{\text{cov}}$)	σ_{cov}
8 m	3167	0.76 (10.9)	0.77 (12.4)	0.48 (−29.8)	0.49 (−28.1)	0.69
95 m	3620	1.30 (101.4)	1.50 (131.8)	0.67 (3.9)	0.63 (−2.6)	0.65
173 m	2410	2.04 (87.7)	1.82 (67.4)	1.05 (−3.7)	1.07 (−1.7)	1.09
20.5 km	2574	2.72 (182.4)	2.35 (144.1)	1.44 (49.6)	1.28 (33.2)	0.96
34 km	15 571	2.73 (249.1)	2.86 (265.5)	1.25 (59.8)	1.17 (49.6)	0.78
mean		1.91	1.86	0.98	0.93	0.83

($\Delta\sigma_{\text{cov}}$): relative differences [%] between two-tower based uncertainty estimates and the references value σ_{cov} (Eq. 5).

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

Table A1. Summary of the 95% confidence intervals for the linear regression coefficients between the 6 average NEE magnitudes and the 6 corresponding standard errors determined with Eq. (3) as described in Sect. 3.3 for the 4 two two-tower based correction schemes and the 5 EC tower distances.

Variables:	Two towers:	m	m_{lower}	m_{upper}	b	b_{lower}	b_{upper}
NEE _{negative} /σ(δ)	EC1/EC2 (8 m)	-0.012	-0.041	0.017	0.691	0.442	0.940
	EC1/EC2 (95 m)	-0.045	-0.099	0.010	1.163	0.680	1.647
	EC1/EC2 (173 m)	-0.052	-0.067	-0.036	1.747	1.537	1.957
	EC1/EC2 (20.5 km)	-0.088	-0.272	0.097	2.544	0.696	4.392
	EC1/EC3 (34 km)	-0.130	-0.330	0.069	2.849	0.772	4.926
NEE _{negative} /σ(δ) _t	EC1/EC2 (8 m)	-0.008	-0.043	0.026	0.746	0.497	0.995
	EC1/EC2 (95 m)	-0.005	-0.036	0.026	1.569	1.286	1.853
	EC1/EC2 (173 m)	-0.055	-0.088	-0.021	1.416	1.009	1.824
	EC1/EC2 (20.5 km)	-0.011	-0.087	0.066	2.606	1.929	3.284
	EC1/EC3 (34 km)	-0.039	-0.190	0.113	3.527	1.737	5.317
NEE _{negative} /σ(δ) _{corr}	EC1/EC2 (8 m)	-0.039	-0.054	-0.025	0.237	0.102	0.372
	EC1/EC2 (95 m)	-0.045	-0.080	-0.010	0.663	0.305	1.021
	EC1/EC2 (173 m)	-0.053	-0.078	-0.028	0.484	0.108	0.860
	EC1/EC2 (20.5 km)	-0.098	-0.130	-0.066	0.867	0.501	1.233
	EC1/EC3 (34 km)	-0.097	-0.140	-0.054	1.000	0.399	1.602
NEE _{negative} /σ(δ) _{corr,t}	EC1/EC2 (8 m)	-0.039	-0.061	-0.017	0.254	0.082	0.427
	EC1/EC2 (95 m)	-0.040	-0.067	-0.014	0.617	0.350	0.883
	EC1/EC2 (173 m)	-0.064	-0.118	-0.009	0.391	-0.343	1.125
	EC1/EC2 (20.5 km)	-0.096	-0.138	-0.055	0.722	0.287	1.157
	EC1/EC3 (34 km)	-0.073	-0.120	-0.026	0.927	0.206	1.647
NEE _{positive} /σ(δ)	EC1/EC2 (8 m)	0.101	0.027	0.174	0.346	-0.024	0.715
	EC1/EC2 (95 m)	0.161	0.028	0.294	0.734	0.285	1.183
	EC1/EC2 (173 m)	0.061	-0.284	0.406	1.340	-0.775	3.455
	EC1/EC2 (20.5 km)	0.118	-0.272	0.507	1.332	-0.500	3.164
	EC1/EC3 (34 km)	0.235	0.113	0.356	0.731	0.323	1.140
NEE _{positive} /σ(δ) _t	EC1/EC2 (8 m)	0.101	0.020	0.182	0.340	-0.080	0.760
	EC1/EC2 (95 m)	0.029	-0.299	0.357	1.333	-0.114	2.780
	EC1/EC2 (173 m)	0.179	-0.122	0.480	0.535	-1.316	2.385
	EC1/EC2 (20.5 km)	0.145	-0.174	0.464	1.134	-0.365	2.632
	EC1/EC3 (34 km)	0.320	0.059	0.580	0.763	-0.330	1.857
NEE _{positive} /σ(δ) _{corr}	EC1/EC2 (8 m)	0.085	0.048	0.122	0.123	-0.072	0.317
	EC1/EC2 (95 m)	0.103	0.090	0.116	0.149	0.105	0.193
	EC1/EC2 (173 m)	0.178	-0.061	0.418	-0.037	-1.619	1.545
	EC1/EC2 (20.5 km)	0.222	0.061	0.382	-0.168	-0.985	0.650
	EC1/EC3 (34 km)	0.164	0.135	0.193	0.145	0.045	0.245
NEE _{positive} /σ(δ) _{corr,t}	EC1/EC2 (8 m)	0.080	0.046	0.114	0.153	-0.027	0.333
	EC1/EC2 (95 m)	0.100	0.064	0.135	0.143	-0.019	0.305
	EC1/EC2 (173 m)	0.182	-0.068	0.431	-0.057	-1.698	1.585
	EC1/EC2 (20.5 km)	0.175	-0.035	0.384	0.074	-0.997	1.145
	EC1/EC3 (34 km)	0.218	0.126	0.309	0.072	-0.277	0.421

^a m_{lower} , m_{upper} : lower and upper 95% confidence interval for slope m

^b b_{lower} , b_{upper} : lower and upper 95% confidence interval for intercept b

$\sigma(\delta)$, $\sigma(\delta)_t$: uncertainty estimated with classical two-tower approach without and with weather filter (f)

$\sigma(\delta)_{\text{corr}}$, $\sigma(\delta)_{\text{corr},t}$: uncertainty estimated with extended two-tower approach

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

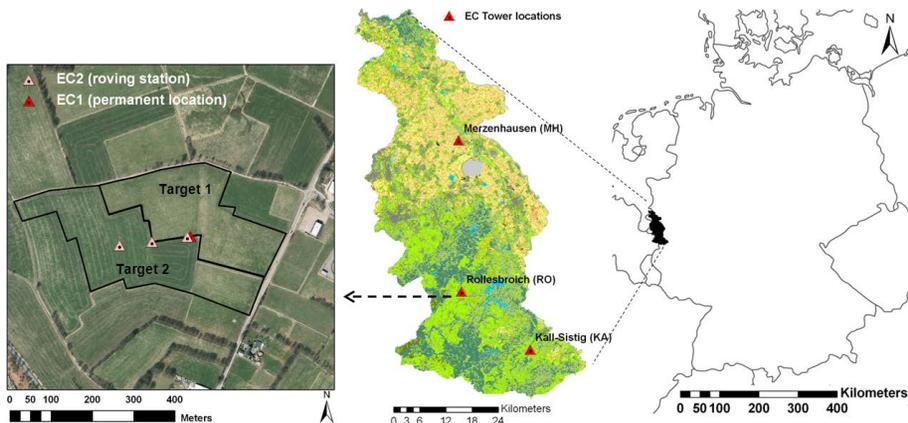
[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Figure 1. Eddy covariance (EC) tower locations in the Rur-Catchment (center) including the Rollesbroich test site (left), with the target areas defined for the footprint analysis.

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

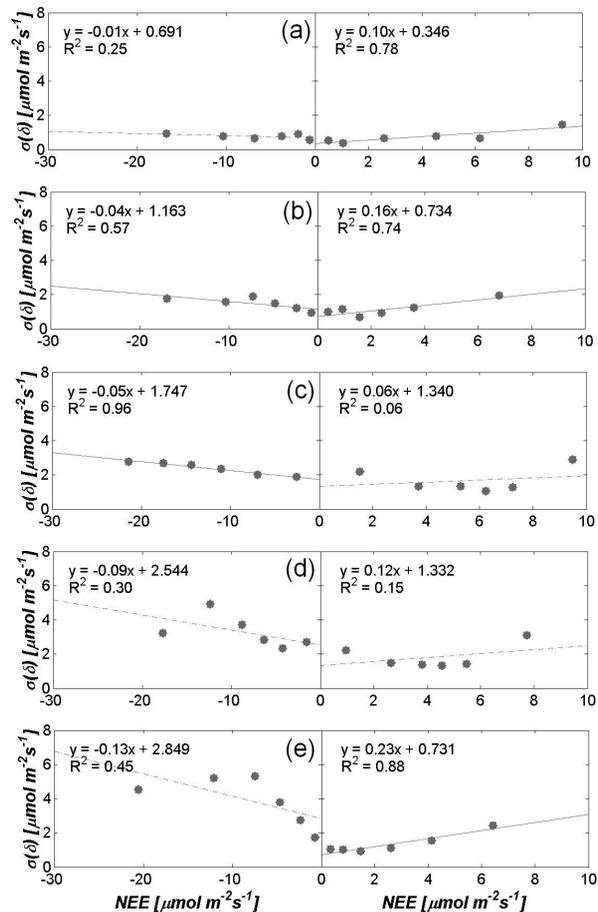
[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Figure 2. NEE uncertainty $\sigma(\delta)$ determined with the classical two-tower approach as function of the NEE flux magnitude for the EC tower distances 8 m (a), 95 m (b), 173 m (c), 20.5 km (d) and 34 km (e). (Dashed line: regression slope not significantly different from zero ($p > 0.1$).)

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

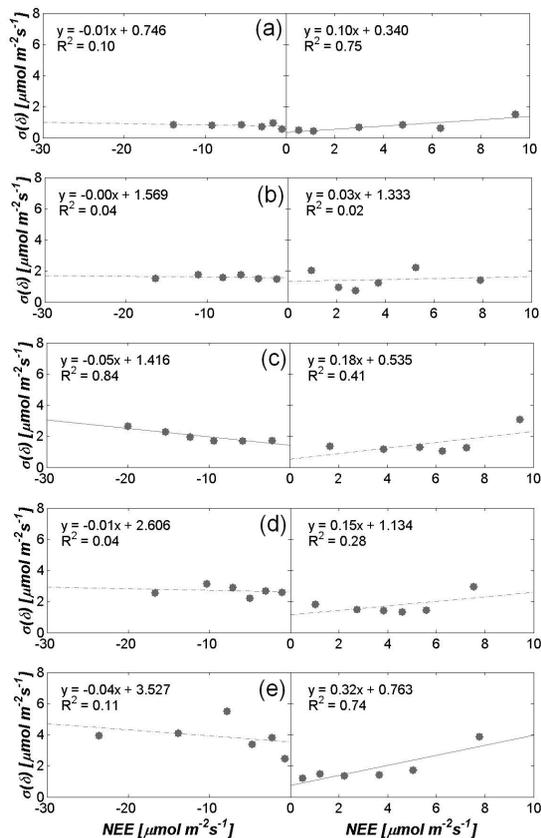


Figure 3. NEE uncertainty $\sigma(\delta)$ determined with the classical two-tower approach as function of the NEE flux magnitude including the application of the weather-filter for the EC tower distances 8 m (a), 95 m (b), 173 m (c), 20.5 km (d) and 34 km (e). (Dashed line: regression slope not significantly different from zero ($p > 0.1$).)

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

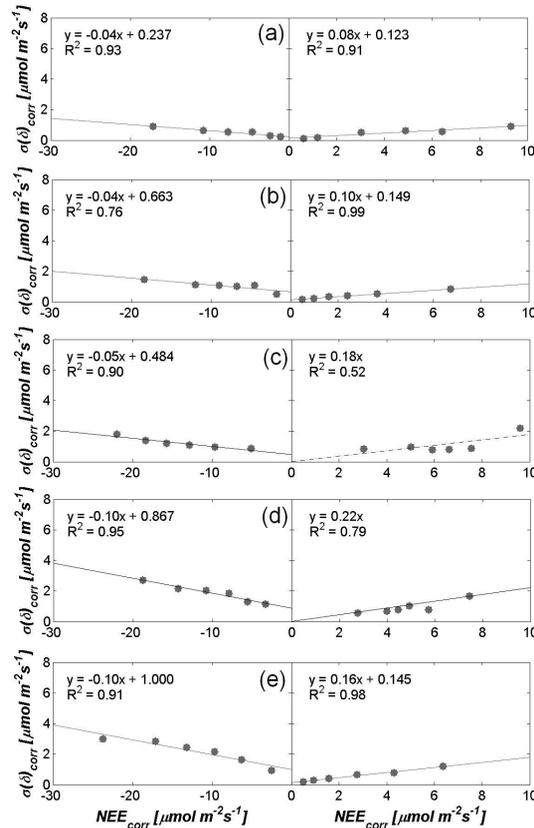


Figure 4. NEE uncertainty $\sigma(\delta)_{\text{corr}}$ determined with the extended two-tower approach as function of sfcd-corrected NEE_{corr} magnitude (Eq. 3) for the EC tower distances 8 m (a), 95 m (b), 173 m (c), 20.5 km (d) and 34 km (e). (Dashed line: regression slope not significantly different from zero ($p > 0.1$).)

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

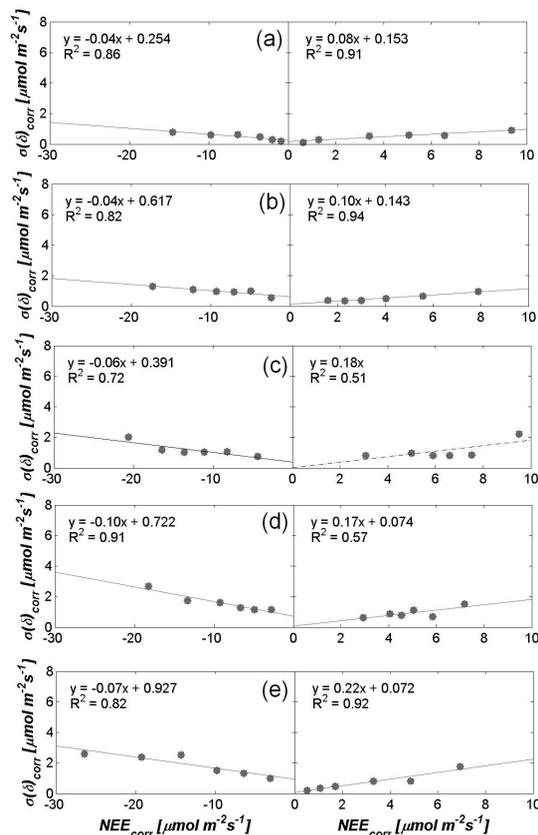


Figure 5. NEE uncertainty $\sigma(\delta)_{\text{corr}}$ determined with the extended two-tower approach as function of sfcd-corrected NEE_{corr} magnitude (Eq. 3) including application of the weather-filter for the EC tower distances 8 m (a), 95 m (b), 173 m (c), 20.5 km (d) and 34 km (e). (Dashed line: regression slope not significantly different from zero ($p > 0.1$)).

Uncertainty analysis of eddy covariance CO₂ flux measurements

H. Post et al.

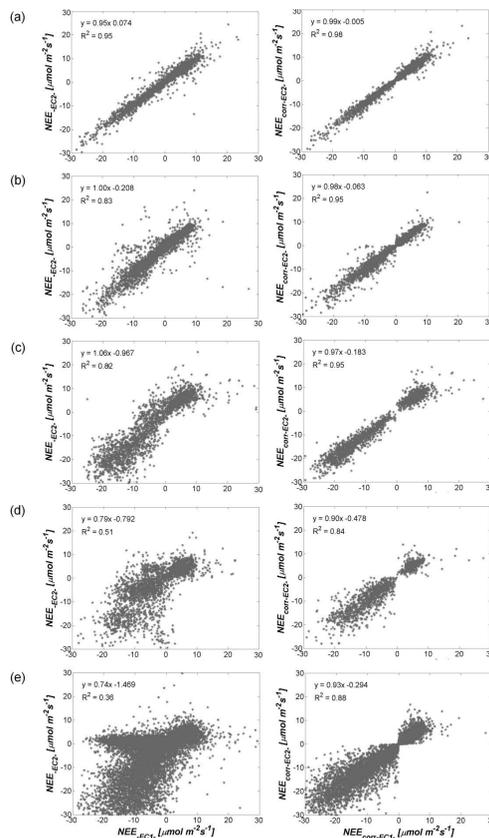


Figure 6. Scatter of the NEE measured at EC1 (NEE_{EC1}) and NEE measured at a second tower EC2/EC3 (NEE_{EC2}) for the uncorrected NEE (left) and the sf-d-corrected NEE_{corr} (right) for the EC tower distances 8 m (a), 95 m (b), 173 m (c), 20.5 km (d) and 34 km.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)
