Intercomparison of fast response commercial gas analysers for nitrous oxide flux measurements under field conditions

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Abstract

Four gas analysers capable of measuring nitrous oxide (N₂O) concentration at a response time necessary for eddy covariance flux measurements were operated from spring till winter 2011 over a field cultivated with reed canary grass (RCG, Phalaris arundinaceae, L.), a perennial bioenergy crop in Eastern Finland. The instruments were TGA100A (Campbell Scientific Inc.), CW-TILDAS-CS (Aerodyne Research Inc.), N2O/CO-23d (Los Gatos Research Inc.) and QC-TILDAS-76-CS (Aerodyne Research Inc.). The period with high emission, lasting for about two weeks after fertilization in late May, was characterised by an up to two orders of magnitude higher emission, whereas during the rest of the campaign the N₂O fluxes were small, from 0.01 to 1 nmol m⁻² s⁻¹. Two instruments, CW-TILDAS-CS and N2O/CO-23d, determined the N₂O exchange with minor systematic difference throughout the campaign, when operated simultaneously. TGA100A produced cumulatively highest N₂O estimates (with 29% higher value during the period when all instruments were operational). QC-TILDAS-76-CS obtained 36% lower fluxes than CW-TILDAS-CS during the first period, including the emission episode, whereas the correspondence with other instruments during the rest of the campaign was good. The reasons for systematic differences were not identified, suggesting further need for detailed evaluation of instrument performance under field conditions with emphasis on stability, calibration and any other factors that can affect systematically the accuracy of flux measurements. The instrument CW-TILDAS-CS was characterised by the lowest noise level (with a standard deviation of around 0.12 ppb at 10 Hz
sampling rate), as compared to N2O/CO-23d and QC-TILDAS-76-CS (around 0.50 ppb) and TGA100A (around 2 ppb). We identified that for all instruments except CW-TILDAS-CS the random error due to instrumental noise was an important source of uncertainty at 30 min averaging level and the total stochastic error was frequently of the same magnitude as the fluxes when N2O exchange was small at the measurement site. Both instruments based on Continuous-Wave Quantum Cascade Lasers, CW-TILDAS-CS and N2O/CO-23d, were able to determine the same sample of low N2O fluxes with high mutual coefficient of determination at 30 min averaging level and with minor systematic difference over the observation period of several months. This enables us to conclude that the new generation instrumentation is capable of measuring small N2O exchange with high precision and accuracy at sites with low fluxes.

**Keywords:** nitrous oxide, fast response instruments, eddy covariance, system performance.

1 Introduction

During the last years there has been a rapid development in the application of laser spectroscopy for greenhouse gas measurements. In particular, development of fast response N2O analyzers based on spectroscopic techniques (e.g. tunable diode laser (TDL) and quantum cascade laser (QCL) spectrometers) has facilitated the eddy covariance (EC) measurements of N2O exchange in different ecosystems. Such measurements have been reported in literature and they have been carried out in different ecosystems such as agricultural (Smith et al., 1994; Wienhold et al., 1994; Christensen et al., 1996; Laville et al., 1997; Scanlon and Kiely, 2003; Neftel et al., 2007; Kroon et al., 2007), forest (Pihlatie et al., 2005; Eugster et al., 2007) as well over urban canopies (Famulari et al. 2010; Järvi et al., 2014).

The observed N2O emissions are episodic in nature, showing high spatial and temporal variability. Emission bursts of short duration, typically occurring after fertilizer application, or associated with thawing and rain events (Kroon et al., 2007; Pihlatie et al., 2010), are followed by long periods of small fluxes, when also uptake of N2O has been observed (Flechard et al., 2005). Overall, N2O fluxes reported by previous studies are characterised by large uncertainty and temporal variability, which are related to biogeochemical soil processes and several systematic and random error sources of the EC measurements. One of the sources
of uncertainty for the $\text{N}_2\text{O}$ fluxes measured by the EC technique is the performance and stability of fast response gas analyzers. Some studies performed under field conditions (Eugster et al., 2007; Kroon et al., 2007; Neftel et al., 2009) have reported that the laser drift can cause occasional over- or under-estimation of EC flux. The instrumental drift typically characterizes TDL as well as QCL spectrometers (Werle et al., 1993; Nelson et al., 2002). Mammarella et al. (2010) thoroughly investigated the performance of TDL instruments in measurements of $\text{N}_2\text{O}$ fluxes by the EC technique. They suggested that high pass filtering could be used to remove the low-frequency signal drifting, which could otherwise contaminate the detected concentration time series and significantly increase the flux uncertainty.

Apart from the episodic emissions, $\text{N}_2\text{O}$ fluxes are typically small in magnitude (in the order of one to one hundred $\mu$g N m$^{-2}$ h$^{-1}$, which corresponds to $\text{N}_2\text{O}$ flux range from $10^{-2}$ to 1 nmol m$^{-2}$ s$^{-1}$ as presented in the units used in the current study), being on the detection limit of the EC systems (e.g. Pihlatie et al., 2005; Wang et al., 2013). Small fluxes imply small turbulent fluctuations of the concentration, requiring high precision of the instruments to be able to resolve those fluctuations. In other words, the signal (turbulent fluctuations) to instrumental noise ratio has to be high enough to achieve sufficiently low flux error arising due to the noise present in measured signals (Lenschow and Kristensen, 1985).

The goals of this study are to compare the available equipment for $\text{N}_2\text{O}$ flux measurements employing the EC technique and to evaluate their performance, ability to detect small fluxes and long-term stability in determining the $\text{N}_2\text{O}$ exchange. The instruments used were TGA100A (Campbell Scientific Inc.), CW-TILDAS-CS (Aerodyne Research Inc.), N2O/CO-23d (Los Gatos Research Inc.) and QC-TILDAS-76-CS (Aerodyne Research Inc.), which shall be further referred to as CS-TDL, AR-CW-QCL, LGR-CW-QCL and AR-P-QCL, respectively, throughout this study by using the combinations of acronyms for manufacturer and the laser type (see Table 1). In addition, the methods for flux calculation using the laser spectrometer data are evaluated and the magnitude and dynamics of $\text{N}_2\text{O}$ fluxes during the RCG growing season are determined.
2 Materials and methods

2.1 Site

The measurement site was a 6.9 ha field cultivated with RCG, a perennial bioenergy crop. The site was located on the rural area of Maaninka, Eastern Finland (63° 9' 48.69" N, 27° 14' 3.29" E). Long-term (reference period 1981-2010; Pirinen et al., 2012) annual air temperature in the region is 3.2°C, the coldest month of the year is February and the warmest is July, with monthly mean air temperature being -9.4°C and 17.0°C, respectively. The annual precipitation in the region is 612 mm. Part of this precipitation amount falls as snow. Snow cover season starts in October and lasts until the end of April with a maximum snow cover of approximately 50 cm. The RCG crop at the Maaninka site was fertilized in the beginning of the growing season (late May), resulting in a large emission pulse of N₂O. The site was applied with an N-P-K-S fertilizer containing 76 kg N ha⁻¹, based on ammonium nitrate (NO₃-N : NH₄-N = 47:53). The canopy height developed throughout the growing season from about 10 cm in mid-May to 1.7 m by late June. The increase in plant height was almost linear in time between these periods and starting from July changed slowly up to 1.9 m.

The soil at the study site is classified as fine sand to coarse silt (particle size 0.03 – 0.06 mm). According to the World Reference Base for Soil Resources (WRB) system (FAO, 2006), the soil is classified as Regosol. The soil pH varies from 5.4 to 6.1 within the ploughing depth from the surface to about 30 cm, electrical conductivity between 960 to 3060 µS cm⁻¹ and soil organic matter content between 3 and 11%. The average C/N ratio in the ploughing depth is 14.9 (ranging from 14.1 to 15.7). The soil particle density is about 2.65 g cm⁻³ within the soil depth from the surface to about 20 cm.

2.2 Measurements

Measurements were conducted by the University of Helsinki (UH) and by the University of Eastern Finland (UEF), operating separate EC systems based on two different sonic anemometers. The UH measurement setup included a 3-D ultrasonic anemometer (USA-1, METEK GmbH, Elmshorn, Germany) to acquire the wind components. The anemometer was installed on top of a pole, the measurement height being 2.2 m. The measurement height was raised to 2.4 m on 30.6.2011 due to the RCG growth. Gas analyzers were situated in an air conditioned cabin located about 15 m east from the anemometer pole. This wind direction (50-110° sector) was therefore discarded from further analysis due to possible disturbances to flux measurements. Sample inlets for gas analyzers were located 10 cm below the
anemometer. The N$_2$O instruments operated by the UH were the instrument based on tunable
diode laser CS-TDL (model TGA100A, Campbell Scientific Inc.), and two instruments based
on continuous wave quantum cascade lasers, AR-CW-QCL (models CW-TILDAS-CS,
Aerodyne Research Inc., see e.g. Zahniser et al., 2009; Lee et al., 2011) and LGR-CW-QCL
(model N2O/CO-23d, Los Gatos Research Inc., see e.g. Provencal et al., 2005). Sampling
lines of AR-CW-QCL and LGR-CW-QCL were heated slightly above ambient temperature in
order to avoid water from condensing to the lines. CS-TDL had a dryer just before the
instrument and no sampling line heating was used. The flow rates and tube dimensions were
chosen to correspond to turbulent flow regime except that the larger diameter of the sampling
line of the LGR-CW-QCL analyser resulted in laminar tube flow for that instrument (see
Section 3.1 below). Further details of the involved instruments are given in Table 1 and
details of the different setups are given in Table 2.

The maintenance of CS-TDL was the most demanding of the compared instruments. It uses
liquid nitrogen to keep the laser source at the operating temperature, and the Dewar was filled
up twice a week. The instrument CS-TDL was calibrated in the beginning of the campaign.
Further the operating parameters of the analyser, such as laser current and laser, housing and
detector temperatures were checked once a week and after power failures. In addition, the
shape and intensity of the absorption line were checked at the same time. These checks were
assumed to guarantee calibration stability of the instrument to a reasonable degree. In
addition, the inlet filter of CS-TDL was changed once a month.

The instrument AR-CW-QCL was calibrated and its operating parameters were fine-tuned at
the site after instrument installation. The instrument manufacturer provided a software
upgrade during the campaign to conduct the real-time water vapour correction to the trace gas
concentration data analysed by the instrument. In addition, the operating parameters were
fine-tuned a few times on-line by the instrument manufacturer during the campaign.

LGR-CW-QCL arrived in the campaign later (see Section 2.6 for details). The factory
 calibration of LGR-CW-QCL was checked but no deviation was observed within the
uncertainty range of the calibration gases. After about two weeks of operation, the laser
drifted out of the tuning range and the laser offset current was tuned manually to enable
correct operation again. No calibration of the instruments based on CW-QCL-s was
performed during the campaign as these analysers were expected to be very stable according
to manufacturers’ information.
The UEF set up included a pulsed quantum cascade laser spectrometer AR-P-QCL (Model QC-TILDAS-76-CS, Aerodyne Research Inc., Billerica, MS, USA, see McManus et al., 2005), an infrared gas analyser (IRGA, Model Li-6262) and a 3-D sonic anemometer (Model R3-50, Gill Instruments, Ltd., Hampshire, UK) for fast response gas concentration and wind component measurements (Tables 1 and 2). The heated intake tubes for the laser spectrometer and IRGA were installed on either sides of the sonic anemometer, all mounted on a boom on an adjustable instrument mast. The mast height was set at 2.0 m above the soil surface in the beginning of the campaign. To adjust to the increasing plant height, the mast was raised to 2.5 m during mid-June. AR-P-QCL was set up to measure simultaneously the \( \text{N}_2\text{O} \), \( \text{CO}_2 \) and water vapour mixing ratios, while the IRGA was used to monitor the \( \text{CO}_2 \) and water vapour mixing ratios. Both trace gas analysers were calibrated against standard gases minimum once a month during the campaign, in particular AR-P-QCL was calibrated every 2-3 weeks with two standard gases 299 and 342 ppb. The calibration slope of AR-P-QCL did not change by more than 7.6% throughout the campaign and maximum 6.1% between consecutive calibrations. Thus 6.1% can be considered as the maximum flux systematic error arising from calibration accuracy of this instrument.

A weather station set up on another mast close to the EC mast monitored the supporting meteorological variables. The weather station mast height was also adjusted according to the changes in the EC mast height. Supporting measurements included air temperature and relative humidity (Model: HMP45C, Vaisala Inc.) using radiation shield, atmospheric pressure (Model CS106 Vaisala PTB110 Barometer), wind speed and direction (Model 03002-5, R.M. Young Company) and several other variables not used in current study. Data was collected using a datalogger (model CR 3000, Campbell Scientific Inc.). Except air pressure (stored as hourly averages), meteorological data was stored as 30 minute averages. Short gaps in the data were filled using linear interpolation, but when air temperature, relative humidity, pressure or rainfall data were missing for longer periods, data from Maaninka weather station operated by the Finnish Meteorological Institute located about 6 km to South-East from the site, was used.

2.3 Flux processing

Measurements were sampled at 10 Hz frequency. Filtering to eliminate spikes was performed according to standard approach (Vickers and Mahrt, 1997), where the high frequency EC data were despiked by comparing two adjacent measurements. If the difference between two
adjacent concentration measurements of N$_2$O was greater than 20 ppb, the following point was replaced with the same value as the previous point.

The spectroscopic correction due to water vapour impact on the absorption line shape was applied along with the Webb-Pearman-Leuning (WPL) dilution correction due to water vapour on high-frequency raw concentration output $X_C$ (mixing ratio with respect to moist air, uncorrected for spectroscopic effect) according to $\chi_c = \frac{X_c}{1 - (1 + b)X_v}$, where $\chi_c$ and $\chi_v$ are the instantaneous mixing ratios of N$_2$O and water vapour with respect to dry air and $b$ is the spectroscopic correction coefficient determined experimentally for each instrument (Table 1) by measuring the response of instrument (output $X_c$) on sample air of standard gas (constant $X_c$) with varying water content $X_v$. The correction was not necessary for CS-TDL as a dryer installed after the air intake point on the sampling line dried the air sample before the optical cell. LGR-CW-QCL corrected for the water vapour effect by a built-in module in the LGR data acquisition software; the same applied to AR-CW-QCL after software update in July 2011.

Prior to calculating the turbulent fluxes, a 2-D rotation (mean lateral and vertical wind equal to zero) of sonic anemometer wind components was done according to Kaimal and Finnigan (1994) and all variables were linearly detrended. The EC fluxes were calculated as 30 min co-variances between the scalars and vertical wind velocity following commonly accepted procedures (e.g. Aubinet et al, 2000). Time lag between the concentration and wind measurements induced by the sampling lines was determined by maximizing the covariance. For CS-TDL the lag was determined by maximizing the covariance for high flux period only (day of year (DOY) 144-146) because in other periods the lag was not well defined by using this method. The final processing (instruments CS-TDL, AR-CW-QCL and LGR-CW-QCL) was done by fixing the time lag to avoid unphysical variation of lag occurring due to random flux errors. For AR-P-QCL system the lag was determined by maximising the covariance for CO$_2$ and the same lag was assigned to N$_2$O. This was to use the advantage that the instrument measured also CO$_2$ and therefore enabled to use much better signal-to-noise ratio in determination of the lag time. Spectral corrections were applied to account for the low and high frequency attenuation of the co-variances (Sect. 2.4). Then, the humidity effect on temperature flux was accounted for after Schotanus et al. (1983). All data processing was
performed with post-processing software EddyUH (http://www.atm.helsinki.fi/Eddy_Covariance/EddyUHsoftware.php).

2.4 Spectral corrections

Low and high frequency variations in the measured signal are attenuated due to data acquisition and processing, and by a non-ideal measurement system (e.g. Moore, 1986; Moncrieff et al., 1997; Rannik and Vesala, 1999; Massman, 2000). Block averaging and detrending of data acts as a high pass filter, thus damping low frequency fluctuations (Rannik and Vesala, 1999; Finnigan et al., 2003). Turbulent fluctuations occurring at high frequencies are attenuated due to the measurement system’s limitations. Gas analyzer’s finite frequency response, attenuation of fluctuations in the sampling line, spatial separation between the anemometer measurement head and sampling line inlet affect the attenuation of high frequency fluctuations in the signal.

The observed flux ($F_m$) can be formally presented as the integral over the convolution of the true co-spectrum ($Co$, unaffected by frequency attenuation) with the co-spectral transfer function as

$$F_m = \int_0^\infty T(f)Co(f) df,$$

where the co-spectral transfer function can be presented as the convolution of respective low-frequency $T_L(f)$ and high-frequency $T_H(f)$ transfer functions. For the low-frequency transfer function due to high-pass filtering and/or finite averaging period see Rannik and Vesala (1999).

For evaluation of the instrument frequency performance and subsequent high-frequency flux corrections during post-processing, the high-frequency transfer function of the EC-system was estimated (Aubinet et al., 2000) as the ratio of the observed and not-attenuated flux (Horst, 1997). The co-spectral transfer function $T_H(f)$ for a system behaving as a first order response sensor can be described by

$$T_H(f) = \frac{1}{1 + (2\pi f \tau)^2},$$

where $f$ is the natural frequency and $\tau$ the (first order) response time of the attenuator (sensor or the system in total) (Horst, 1997). The effective transfer function of the EC system for
different instruments was estimated as the ratio of co-spectral density of scalar flux relative to co-spectrum of sensible heat flux (Aubinet et al. 2000). Such a procedure assumed that temperature measurements were not affected by attenuation (true for the sonic anemometer) and includes normalisation with integral over frequencies not affected by attenuation.

### 2.5 Estimation of random errors

Turbulent fluxes averaged over a limited time period have random errors because of the stochastic nature of turbulence (Lenschow et al. 1994; Rannik et al., 2006) as well as due to noise presented in measured signals (Lenschow and Kristensen, 1985).

The random error of the flux was evaluated as one standard deviation of the co-variance error, hereafter in the manuscript denoted by \( \delta_F \). It was defined through the variance of the distribution of the individual flux realization around the ensemble mean (e.g. Lenschow et al., 1994). Theoretically, there are several approaches to approximate the same error estimate, see e.g. Rannik et al. (2009). Currently, the flux random error was calculated according to the method implemented in EddyUH, the method proposed by Finkelstein and Sims (2001). The method evaluates the error in time domain through integration of the auto-covariance and cross-covariance functions of the vertical wind speed and the scalar concentration according to

\[
\delta_F \approx \sqrt{\frac{1}{n} \sum_{p=m}^{m} \sum_{p=m}^{m} \overline{w'(p)c'(p)} + \frac{m}{p-m} \sum_{p=m}^{m} \overline{w'(p)c'(p)}},
\]

where \( \overline{w'(p)} = \frac{1}{n} \sum_{i=1}^{n-p} (w(t_i) - \overline{w})(w(t_{i+p}) - \overline{w}) \). In calculations we used \( m = 200 \) (corresponding to 20 sec) to ensure that integration of the covariance functions was performed over times exceeding the integral time scale of turbulence. This mathematically rigorous method provides estimates for the random uncertainty of the flux measurements for every flux averaging period.

Random uncertainty of the observed co-variance due to presence of noise in instruments signal, giving essentially the lowest limit of the flux that the system is able to measure, was expressed in its simplest form as

\[
\delta_{F,\text{noise}} = \frac{\sigma_w \sigma_{\text{noise}}}{\sqrt{JT}},
\]
where $\sigma_w$ and $\sigma_{\text{noise}}$ denote the standard deviation of the turbulent record of vertical wind speed and the standard deviation of instrumental noise as observed at frequency $f$, $T$ denotes the flux averaging period. The expression above assumes that the noise component of the vertical wind speed measurement is negligible. In this study we use the method developed by Lenschow et al. (2000) and applied to EC fluxes by Mauder et al. (2013) to estimate the flux error due to instrumental noise. Lenschow et al. (2000) derived the method to estimate the instrumental random noise variance $(\sigma_{\text{noise}})^2$ from the auto-covariance function of the measured turbulent record close to zero-shift, enabling to determine the error for each half-hour flux averaging period.

The random flux error $\delta_F$ is the result of limited sampling in time and/or in space of a stochastic turbulence realization. Its expression includes the covariance and cross-covariance functions of turbulent records, therefore in addition to variances and co-variances accounting for respective integral time scales of turbulent records. The error $\delta_F$ incorporates also the contribution due to instrumental noise and is therefore larger from the latter.

The error $\delta_{F,\text{noise}}$ instead does not depend on the integral time scale of turbulence, being therefore mainly determined by the instrumental noise characteristics and less on the observation conditions (only via $\sigma_w$). Assuming no true turbulent variation of concentration and thus zero flux, the calculated flux will be generally non-zero due to noise in instrumental signal. Evidently the system will not be able to detect the fluxes smaller than the ones obtained from the expression for $\delta_{F,\text{noise}}$. Therefore this is the minimum flux that the EC system can detect and $\delta_{F,\text{noise}}$ serves useful in characterising the instrumental limitation to detect small fluxes.

If an average over fluxes $F_i \ (i = 1..N)$ is calculated, each of these representing a flux value observed over averaging period $T$ and being characterised by an error $\delta_{F,i}$, then the error of the average flux $\langle F \rangle = \frac{1}{N} \sum_{i=1}^{N} F_i$ was expressed as

$$\Delta_{\langle F \rangle} = \sqrt{\frac{\sum_{i=1}^{N} (\delta_{F,i})^2}{N^2}}.$$  

(5)

This expression will be used to estimate the random errors of the average fluxes in Sect. 3.4.
2.6 Periods of analysis and quality screening

The intercomparison measurements were performed from the beginning of the growing season in April till November 2011. According to instrumental data coverage, the period was divided into three sub-periods for the instrument evaluation and flux analysis purposes. During the period I, DOY 110-181 (20.04-30.06.2011), the measurements of CS-TDL, AR-CW-QCL and AR-P-QCL were available, during the period II, DOY 206-271 (25.07-28.09.2011), all instruments were measuring and during period III, DOY 272 – 324 (29.09-20.11.2011), all other except CS-TDL were operational. Prior to analysis data quality screening was performed. The measurements corresponding to wind direction interval 50-110° were excluded as possibly affected by instrumental cabin. In addition, quality screening was performed according to Vickers and Mahrt (1997) by applying the following statistics and selection thresholds: data with N₂O concentration skewness outside (-2, 2), or kurtosis outside (1, 8), or Haar mean and Haar variance exceeding 3 were rejected. Applying the same statistics and thresholds as for N₂O, additional quality screening of N₂O fluxes was performed according to H₂O concentration statistics for AR-CW-QCL and AR-P-QCL due to the impact of the spectroscopic and dilution corrections on fluxes and according to CO₂ concentration statistics for AR-P-QCL because the lag obtained for CO₂ was assigned to N₂O in case of this instrument.

The applied quality criteria were used to ensure exclusion of the system malfunctioning as well as unphysical and/or unusual occasions. No quality screening for stationarity was performed as the focus of the study was the instrumental intercomparison, which was not affected by occasional non-stationary conditions included in the analysed data set.

3 Results

The fluxes obtained for three periods are presented in Fig. 1, being averaged over daily period for the clarity of presentation. No gap-filling was used and for each day only the existing measurements, after applying data quality screening described above, were averaged. In May the fluxes increased significantly after the fertilization and then decreased back to low, although clearly positive level after a few weeks. This was the only occasion of high N₂O emission followed by continuous decrease of fluxes towards the autumn. The soil temperature had increasing trend until about DOY 205 (24 July, 2011) and since August declining
seasonal trend (Fig. 2). SWC increased with occasional rain events. During the high emission, starting from DOY 144 (24 July, 2011) and lasting until approximately DOY 155 (4 June, 2011), the SWC was approximately 0.3 m$^3$ m$^{-3}$, being relatively high.

The high fluxes observed during that period enabled to evaluate the frequency performance of three systems including CS-TDL, AR-CW-QCL and AR-P-QCL. The LGR-CW-QCL instrument was not operational then and the frequency response analysis for this instrument was performed based on the concurrently measured H$_2$O and CO signal analysis.

### 3.1 Spectral characteristics of instruments

Spectral analysis was performed to study the frequency performance of the instruments. In general, averaging over long periods should lead to better spectral statistics. However, aggregating over different periods might lead to biased results as the spectra do not necessarily follow the idealised normalizations in frequency scale, considering also that spectral scaling depends on stability. Therefore we aimed to use optimal averaging period over several hours for similar conditions in terms of wind speed and stability. For the period May 26$^{th}$, from 7:00 to 13:00 EET (Eastern European Time) when the conditions corresponded to moderately unstable (average wind speed of the period 3.2 m s$^{-1}$ and sensible heat flux 50 W m$^{-2}$), the calculated spectra exhibited very clear and systematic patterns for temperature as well as N$_2$O concentration records measured by three instruments (Fig. 3). In spite of high fluxes registered by the instruments during this period, CS-TDL N$_2$O signal was dominated by noise almost over the whole frequency range presented. For AR-CW-QCL, almost no evidence of noise could be observed in the power spectral plot (multiplied with frequency). The older version by Aerodyne, the AR-P-QCL instrument, revealed increase of the spectral density only at the high-frequency end of the power spectrum, being characteristic to some noise contribution. The co-spectra of all three instruments showed smooth patterns, the shape being consistent with the co-spectral model by Kaimal et al. (1972) but slightly shifted in frequency scale. At the high frequency ends of the presented co-spectra the N$_2$O signal curves deviate from the theoretical as well as from temperature co-spectra, indicating attenuation of signals at high frequencies by the measurement systems.

The same time period was used to estimate the frequency response of the N$_2$O eddy covariance systems according to the method described in Sect. 2.4 (Fig. 4). The time constants estimated by making use of the co-spectra presented in Fig. 3 and eq. (2) for CS-
TDL, AR-CW-QCL and AR-P-QCL were 0.12, 0.07 and 0.08 seconds, respectively. Note that these time constants characterise the frequency response of the systems in total.

Although the response time obtained for AR-P-QCL system from high flux period was 0.08 sec, the analysis of the response time from measured CO\textsubscript{2} signal for several other periods yielded the average response time 0.15 sec. The N\textsubscript{2}O signal was synchronised with CO\textsubscript{2} by using the lag determined for CO\textsubscript{2} and theoretically the N\textsubscript{2}O response time does not differ from that of CO\textsubscript{2} under turbulent tube flow regime, hence we choose the constant value 0.15 sec for co-spectral corrections throughout the campaign for this instrument.

Spectral analysis was performed also for the period when LGR-CW-QCL measurements were available. For the comparison purpose, the results for a time period in August 4\textsuperscript{th} from 00:30 to 4:00 EET are presented for AR-CW-QCL and LGR-CW-QCL instruments (Fig. 5). The period was chosen with relatively high fluxes (with LGR-CW-QCL measurements available) and similar stability and wind conditions (average wind speed of the period 0.94 m s\textsuperscript{-1} and sensible heat flux -37.5 W m\textsuperscript{-2}). The power spectra of both instruments revealed contribution of noise at high frequency ends of the spectra, being more pronounced for LGR-CW-QCL. The co-spectra were more scattered when compared to high flux period (Fig. 3). Estimation of the frequency response of the systems based on this period was uncertain due to scatter and could not be used as the basis for co-spectral corrections for LGR-CW-QCL.

The main difference in the flow setups of the systems concerned LGR-CW-QCL. With larger tube diameter and slightly lower flow rate the flow regime was likely laminar (Re \approx 2 000), whereas for other instruments it was clearly turbulent (Re \geq 4 600). It is well established that under laminar flow regime tube flow attenuates turbulent fluctuations of concentration much more than under turbulent flow. According to the expression for tube attenuation in laminar flow regime (Foken et al., 2012) the first order response time for LGR-CW-QCL flow setup would be 0.37 sec (estimated for N\textsubscript{2}O). For turbulent flow (ARI-CW-QCL setup) the theoretical response time for tube damping is much smaller (0.01 sec) than the response time obtained from the co-spectra (0.07 sec), suggesting that the system’s response was dominated by the instrumental response.

The frequency response of the LGR-CW-QCL system was further determined from the co-spectral analysis of the CO signal and we obtained the value 0.26 sec. We determined also the
experimental response time for water vapour from several periods corresponding to low humidity conditions (RH<40%) and we consistently found the value around 0.35 sec (for LGR-CW-QCL system). For comparison, the response time for H$_2$O measured by ARI-CW-QCL system was determined to be 0.10 sec. Damping of water fluctuations in sampling lines is stronger than for other scalars as evidenced by experimental studies (e.g. Mammarella et al., 2009). This is due to adsorption/desorption of water molecules on tube walls. This explains the difference between the response times obtained from CO and H$_2$O. Thus we believe that a value of 0.26 sec characterises well the first order response time of LGR-CW-QCL setup for N$_2$O and we use this value in co-spectral corrections. Note, however, that a higher response time of the LGR-CW-QCL system does not mean a slower instrument performance because the system has more damping primarily in the sampling line due to lower flow rate and larger tube diameter (Table 2).

The frequency response times determined in this section were used in performing the co-spectral corrections (Table 2) as described in Sect. 2.4, typical magnitudes of these corrections are presented in Table 3.

### 3.2 Random uncertainty of fluxes and instrumental noise

The method by Lenschow et al. (2000) described in Sect. 2.5 enabled to calculate the instrumental noise for each 30 min period and the resulting flux uncertainty due to instrumental noise. Fig. 6a shows the estimated signal noise statistics with upper and lower percentiles and quantiles (boxes) with a median value in the middle. For all instruments except LGR-CW-QCL the distributions are very narrow and different percentiles cannot be separated from the plot (for values see Table 1). This tells us that the noise levels of the three instruments are very stable, but the noise level of LGR-CW-QCL somewhat varies. In comparison of the instruments, AR-CW-QCL has by far the lowest noise level of around 0.12 ppb (standard deviation of the signal noise at 10 Hz frequency). The two instruments, LGR-CW-QCL and AR-P-QCL, are characterised by a similar noise level (around 0.5 ppb), while CS-TDL signals show the highest noise level (2 ppb). Consequently, these instrumental noise levels are reflected in the random errors of fluxes, determining essentially the minimum flux level that each instrument is able to measure at a given flux averaging interval (30 min period). For AR-CW-QCL the respective lowest flux is around $10^2$ nmol m$^{-2}$ s$^{-1}$ (as given by median in Fig. 6b), for LGR-CW-QCL and AR-P-QCL around $4x10^2$ nmol m$^{-2}$ s$^{-1}$ and for CS-TDL 0.15 nmol m$^{-2}$ s$^{-1}$. 


The frequency distributions of the total flux random errors, calculated according to Eq. (3), are naturally higher than the flux error due to instrumental noise only. It can be observed that in case of full flux random error the difference between different instruments is reduced (Fig. 6b) because in addition to instrumental noise impact this error statistic also incorporates the flux uncertainty due to stochastic nature of turbulence. The relative random errors (Fig. 6c) are the largest for CS-TDL (being in the order of 100% and in most cases less than ±300%) and the smallest for AR-CW-QCL (median around 30% and mostly the error being less than 100%) instruments. It is the signal noise of the instrument that contributes to the random error of the flux, determining which instrument is able to detect lowest fluxes. In case of CS-TDL the low-frequency signal drifting can also enlarge the total random error of the calculated flux.

3.3 Intercomparison of fluxes averaged over turbulent spectrum

It was observed that the fluxes calculated from CS-TDL measurements during the low flux period were dominated by stochastic uncertainty, being frequently in the order of the random uncertainties of fluxes (Sect. 3.2). Therefore, the fluxes averaged over 30 min period were compared for this instrument with AR-CW-QCL results over the period DOY 110-182, which included the high emission episode starting from DOY 144 and exhibiting elevated fluxes until approximately DOY 155. In general the fluxes with high magnitude obtained by CS-TDL compared well with those of obtained by AR-CW-QCL (Fig. 7a). The AR-P-QCL system, as compared with AR-CW-QCL, showed systematically lower fluxes during the given period of high fluxes (slope 0.70). In spite of lower noise level of this instrument, the coefficient of determination for this instrument (0.63) was lower than that for CS-TDL (0.77) in comparison to the fluxes as measured by AR-CW-QCL.

During the second observation period, when fluxes were much lower, CS-TDL was not able to determine fluxes with sufficiently small error and the correlation with AR-CW-QCL at 30 min averaging level was very low (Fig. 7c). At around zero fluxes as measured by AR-CW-QCL, the results by CS-TDL showed scattered values visually between ±2 nmol m\(^{-2}\) s\(^{-1}\). The noise level of CS-TDL around 2 ppb translates into flux uncertainty due to instrumental noise of about 0.05 to 0.3 nmol m\(^{-2}\) s\(^{-1}\). The total flux error \(\delta_f\) was within the range from 0.1 to 0.45 nmol m\(^{-2}\)s\(^{-1}\) (upper and lower quantiles of the distribution in Fig. 6b). We analysed the range of variation of CS-TDL fluxes during the given period DOY 206-272, conditionally selecting...
the observations when the observed fluxes by AR-CW-QCL were absolutely smaller than 0.15 nmol m\(^{-2}\) s\(^{-1}\) (90% of N\(_2\)O flux random errors for AR-CW-QCL less than this value during the given period). The respective N\(_2\)O fluxes as determined by CS-TDL were characterised by the upper and lower quantiles of -0.27 and 0.52 nmol m\(^{-2}\) s\(^{-1}\). This is consistent with the upper quantile of the flux error distribution for CS-TDL. Therefore the fluxes of CS-TDL, corresponding to close-to-zero fluxes as determined by AR-CW-QCL, were consistent with the flux error estimates.

The comparison of the 30 min average fluxes calculated from two instruments, AR-CW-QCL and LGR-CW-QCL, revealed very good correspondence and high correlation \((R^2 = 0.90)\) even though those measurements corresponded to very low N\(_2\)O fluxes. The slope close to unity and negligible intercept indicates no systematic bias between the measurements of these systems (Fig. 7d).

### 3.4 Long-term averages and systematic differences

In order to evaluate the possible systematic differences, cumulative curves of the flux observations were calculated. No gap-filling of missing data was done but instead only the half-hour periods were used when the results for all instruments were available. Thus the cumulative sums do not assume representing the total emissions over the given periods, although rough estimates could be calculated by accounting in total sums with the data coverage percentage presented in Table 4. The summation of fluxes over the first and second periods reveals that CS-TDL gives the highest flux sums and AR-P-QCL the lowest, in particular during the first period (Fig. 8). The cumulative sums for fluxes obtained from AR-CW-QCL and LGR-CW-QCL measurements converge over 2\(^{nd}\) and 3\(^{rd}\) periods and show only small differences. Also the cumulative fluxes measured by AR-P-QCL during these periods are very close to fluxes measured by the two other instruments. In order to assess the magnitude of the random errors in these differences, the random errors of the fluxes averaged over three periods were calculated according to Eq. (5). The analysis revealed that the average fluxes for period II, obtained from the measurements of AR-CW-QCL and LGR-CW-QCL instruments did not differ within calculated error limits, and were very close during the period III with the result for AR-P-QCL (Table 4).

However, CS-TDL produced a 7% higher total sum for the period of high fluxes (DOY 110-181 with an average flux of 0.87 nmol m\(^{-2}\) s\(^{-1}\) as determined by AR-CW-QCL) and a 29%
higher sum for the second period (DOY 206-271) compared to an average flux 0.142 nmol m$^{-2}$ s$^{-1}$ (average of AR-CW-QCL and LGR-CW-QCL results). The AR-P-QCL instrument determined for these two periods 36% and 13% lower average fluxes, respectively. The possible reasons for this will be discussed in the next section. For the third period, the results for AR-P-QCL did not differ much from the results of the other two instruments.

4 Discussion

Performance of four instruments (see Tables 1 and 2) capable of fast response measurement of N$_2$O was studied throughout the 2011 growing season over a field cultivated with RCG in Eastern Finland. The N$_2$O fluxes were small in the beginning of the season, increased significantly after the fertilization (late May) and then decreased back to low, positive values after a few weeks. Three instruments, CS-TDL, AR-CW-QCL and AR-P-QCL were operational during this high emission period. During this period, all instruments detected the same flux dynamics, whereas the fluxes obtained by AR-P-QCL, the previous instrument version by Aerodyne, were lower compared to the other two instruments.

For many applications the systematic errors of micrometeorological flux measurements of atmospheric trace gases are more important than the random errors. For example, for determination of annual balances (e.g. Kroon et al., 2010b) or for the comparison of exchange of different ecosystems (e.g. Nicolini et al., 2013) the systematic errors become very important. The two CW-QCL instruments compared very well on half-hour basis as well as produced statistically close cumulative fluxes over the period when the two instruments were simultaneously operational (25.07.2011-20.11.2011). The cumulative emission estimate obtained by CS-TDL for the same period was 29% higher than the average result for instruments based on the continuous wave quantum cascade lasers, AR-CW-QCL and LGR-CW-QCL. AR-P-QCL obtained 36% lower fluxes than AR-CW-QCL during the first period including the emission episode, whereas the correspondence with other instruments during the rest of the campaign was relatively good.

The systematic differences in fluxes could be the result of calibration and/or limited stability of the system over time. The impact of the instruments calibration (sensitivity shift) impact on flux systematic differences can be assessed by using calibration information (Section 2.2) as well as comparison of average concentrations measured by different instruments. The two analysers based on CW-QCL-s are expected to be very stable, which was confirmed by the
measurements: The concentrations measured by these two instruments were very consistent and the slope (characterising sensitivity) of the 30 min average concentration comparison did not deviate from unity by more than 5% (with the coefficient of determination of linear regression $R^2 = 0.86$).

The sensitivity of AR-P-QCL did not change more than 6.1% between consecutive calibrations and this can be considered as the maximum flux error arising from calibration accuracy of this instrument (Section 2.2). Nevertheless, the correlation of the 30 min average concentration measured by this instrument as compared to AR-CW-QCL was not as good (for the period DOY 206-272 slope 1.05 was determined with $R^2 = 0.63$). The concentration comparison presented here does not reveal that the calibration bias was the reason for the observed flux systematic difference for the instrument AR-P-QCL.

The analyser CS-TDL is known for its signal drifting as illustrated and discussed by Mammarella et al. (2010) and the absolute concentrations were not well determined during our campaign. Therefore accurate measurement of absolute concentration by this instrument over a long period of time cannot be expected and the concentration comparison was not used as the method for evaluation of the instrument’s calibration impact on flux systematic bias. Note that signal drifting makes the time series produced by the instrument essentially non-stationary and therefore enhances the random variability of the flux estimate around the true value. However, such enhanced random uncertainty does not affect systematically the cumulative sums over longer periods.

In case of low fluxes the water vapour dilution and spectral line broadening effects are the primary suspects for the reasons in systematic differences in fluxes (e.g. Peltola et al., 2014). Close correspondence of the concentrations and fluxes as measured by AR-CW-QCL and LGR-CW-QCL let us conclude that the spectroscopic and water vapour dilution corrections for these instruments were adequate. Note that those corrections were done by built in functionality in case of LGR-CW-QCL. For AR-CW-QCL the respective corrections were done in post processing phase for the period I and by built-in software for the rest of the campaign.

The only evident systematic flux error source that could affect performance of CS-TDL would be incomplete drying of sample air. If that was the case, then the calculated fluxes had
suffered from missing partial density and spectroscopic corrections. Since the water fluxes are
dominantly upward, a respective correction would tend to increase the flux values, therefore
increasing even more the systematic difference relative to other instruments.

The instrument ARI-P-QCL is based on the pulsed quantum cascade laser. For this instrument
the experimentally determined spectroscopic correction coefficient was much lower than the
coefficient for AR-CW-QCL (Table 1). The reason for systematically lower values of fluxes
determined by AR-P-QCL from the beginning of the experiment in April till June 2011, but
subsequent relatively good comparison with other instruments till the end of the experiment in
November 2011, is not known. Two types of corrections were applied to N₂O fluxes: the
spectroscopic correction to account for the impact of water vapour on the absorption line
shape, and the co-spectral correction. The latter correction was comparable to all instruments
(Table 3) and does not introduce significant difference between instruments. The
spectroscopic correction was applied together with the water vapour dilution correction (Sect.
2.3) and can constitute a major correction depending on the value of the coefficient b. The
correction is related to the water vapour flux, which was during the day time on the average
around 100 W m⁻² (periods I and II, Table 5), with mid-day averages around 150 to 200 W m⁻².
Considering the average concentration of N₂O around 330 ppb and the spectroscopic
correction value b=0.39 (the value for AR-CW-QCL), the spectroscopic correction can be a
few tenths of nmol m⁻² s⁻¹ during mid-day, which is of the order of the flux magnitude. We
used all auxiliary data available to investigate the possible reasons for the systematic
differences, but found no explaining variable or reason. In particular, no systematic variation
of the residual between AR-P-QCL and AR-CW-QCL fluxes was found over wide range of
latent heat fluxes from -20 to 250 W m⁻². This proves that the dilution and spectroscopic
corrections were properly accounted for. In addition, larger spectroscopic correction would
not explain systematic difference observed during the first period only.

Thus the reasons for flux underestimation by AR-P-QCL during the period I are not known
and we suggest that extreme care should be exercised during the long-term measurement
campaigns both with N₂O and H₂O calibrations due to the strong impact of the latter on the
N₂O flux through spectroscopic and dilution corrections.

A comment should be made regarding the observation level used in the study. When RCG
was grown high, the measurement level was only about 0.5 m above the canopy top. The
measurements within the roughness sublayer can be disturbed in terms of several statistics, but the impact can be expected revealed more in spectral shapes than in integral statistics. The spectra obtained for N$_2$O (Fig. 3 and 5) were dominated by white noise over wider (CS-TDL) or narrow (AR-CW-QCL) frequency ranges depending on the instrument in question. The temperature spectra were similarly affected by the noise but only at the high frequency end of spectra and we believe that not evidencing the canopy impact on spectral shapes. We checked also the spectra for vertical wind speed (not shown). The spectra exhibited smooth and consistent shapes, without the particular impact of the canopy foliage on spectral forms usually observed inside canopy. Launiainen et al. (2007) studied the turbulence statistics and spectral shapes within pine forest canopy. They did not observe deviation of spectral shapes above canopy at height z/h = 1.47 (h being the canopy height) from the atmospheric surface layer forms, within the crown space (z/h = 0.78) the spectra deviated only slightly from the above-canopy forms. Within the trunk space (z/h = 0.4) the spectra were distorted due to the drag imposed by the canopy elements. This supports that the spectra measured close to but above canopy are weakly affected by the canopy presence. Thus we do not expect that the relatively low observation level biases the overall N$_2$O flux level and that the comparison of instrumentation is affected. Also the effect on the instrumental noise and flux random uncertainty analysis is expected to be very limited through the influence on the co-variance functions. The positive impact of the close positioning of the system could be its higher sensitivity in detecting the low fluxes through higher concentration fluctuations expected (more) close to the source level.

Important characteristics of the instruments for performing the EC measurements are the response time and the noise level. The response times for CS-TDL, AR-CW-QCL and AR-PQCL flux measurements systems were determined to be 0.12 and 0.07 and 0.08 seconds, respectively. The main factors affecting the response time of the closed-path EC system are the damping of fluctuations in the sampling line and the instrumental response. Since the flow rate of CS-TDL system was higher, it can be concluded that the response characteristics of other two instruments are superior. The response time of the EC system including LGR-CW-QCL was larger due to the laminar tube flow regime, but the instrumental response was not determined based on the current field measurements.

In order to understand drivers of exchange and inferring the broad average fluxes such as seasonal or annual sums by using some gap-filling methodologies it is important that the
exchange at shorter time scale can be distinguished from random variation. Therefore understanding of the random errors is important when working with low fluxes as is frequently the case with $\text{N}_2\text{O}$. At half-hour averaging time scale the flux estimates for AR-CW-QCL and LGR-CW-QCL instruments were very well correlated and showed good correspondence. Apart from high $\text{N}_2\text{O}$ fluxes exceeding a few nmol m$^{-2}$ s$^{-1}$ during the high emission period, CS-TDL was not able to resolve the emission fluxes at half-hourly time scale. Therefore one can conclude that CS-TDL is not suitable for measuring such low fluxes if the aim is to resolve fluxes at hourly time scale and not the daily or longer averages.

Aerodyne AR-CW-QCL had the lowest noise level (around 0.12 ppb at 10 Hz sampling rate) compared to Los Gatos LGR-CW-QCL instrument (std of noise 0.60 ppb) and has therefore advantage in resolving low fluxes over short averaging periods. The noise level of AR-P-QCL was comparable to LGR-CW-QCL instrument but the old generation instrument Campbell CS-TDL suffered clearly from higher noise level (around 2 ppb). Huang et al. (2014) reported for the instrument similar to AR-CW-QCL the precision 0.066 ppb for 10 Hz. The value obtained by us was higher roughly by a factor of two. According to manufacturer the precision of LGR-CW-QCL is 0.1 ppb at 1 Hz averaging; at 10 Hz this would correspond to 0.32 ppb. We have determined again a median value roughly twice higher than this. Kroon et al. (2007) reported for the instrument similar to AR-P-QCL the precision value 0.5 ppb Hz$^{-1/2}$ (equivalent to 1.6 ppb at 10 Hz), whereas Neftel et al. (2007) and Eugster et al. (2007) report 0.3 ppb Hz$^{-1/2}$ (equivalent to 0.95 ppb at 10 Hz). Pihlatie et al. (2005) and Wang et al. (2013) report as the noise of instrument CS-TDL 1 ppb and 1.5 ppb (at 10 Hz), respectively. Under field conditions the instrumental noise can be somewhat higher compared to laboratory conditions where the instrumental characteristics are typically studied. Also the estimation method from the field records where the turbulent variation is superimposed by the instrumental noise can introduce some uncertainty. In summary, the observed instrumental noise characteristics for instruments compare well with the results reported by others and are useful in characterising instrumental performance.

The flux errors due to instrumental noise for the observation conditions prevailing at the site were determined to be around $10^2$ nmol m$^{-2}$ s$^{-1}$ for AR-CW-QCL, $4 \times 10^2$ nmol m$^{-2}$ s$^{-1}$ for LGR-CW-QCL and AR-P-QCL and 0.15 nmol m$^{-2}$ s$^{-1}$ for CS-TDL. Based on half-hour as well as long-term flux comparison, the best correspondence was observed between the systems with new generation instruments AR-CW-QCL and LGR-CW-QCL, of which the
former has the advantage in detecting lower fluxes at half-hourly averaging basis (lower noise level).

The signal noise of the anemometer used by the UH (USA1 by METEK) was determined to be 0.037 m s\(^{-1}\) at 10 Hz sampling frequency for vertical wind speed component. The noise level of the anemometer employed by the UEF was similar. The flux error due to anemometer’s noise for the observation conditions prevailing at the site during the period DOY 206-271 (the period for the statistics presented in Fig. 6) were determined to be around 2\times10^{-3} \text{ nmol m}^{-2} \text{s}^{-1} (the median value). This was much less than the respective flux error around 10^{-2} \text{ nmol m}^{-2} \text{s}^{-1} for the instrument AR-CW-QCL, which had the lowest noise level 0.012 ppb (median value) of all instruments compared. Therefore the assumption that the anemometer’s noise affects flux detection much less than the gas analysers was well justified.

The chamber techniques are widely used to measure the soil \(N_2O\) exchange. The traditional way to perform chamber measurements is to determine the gas concentration at several time moments during the chamber operation (called deployment time DT). In such data collection the sources of uncertainty are the imprecision related to gas sampling (either manual or automatic) as well as instrumental uncertainty (e.g. Venterea et al., 2009), leading to a measurement precision which is called a detection limit of chamber based flux measurement system. Neftel et al. (2007) report a flux detection limit of about 0.23 nmol m\(^{-2}\) s\(^{-1}\) for their chamber system with DT of 10 min and the concentration sampling interval of 1 min. The measurement cycle of the system was however two hours. Wang et al. (2013) found for their automatic and manual chamber systems detection limits of about 5 \(\mu g\) m\(^{-2}\) h\(^{-1}\) (0.05 nmol m\(^{-2}\) s\(^{-1}\)) for hourly DT. Their instrument precision was high, around 0.4\% relative to ambient \(N_2O\) concentration. By using the methodology and scaled results presented by Parkin et al. (2012), we estimated the flux detection limit of a chamber system with assumed chamber height of 0.5 m, the area of 0.25 m\(^2\), deployment time 30 min and instrumental precision as high as 0.1\% to be 0.03 nmol m\(^{-2}\) s\(^{-1}\). It has to be noted that the flux detection limit of the chamber systems depends on several factors such as the type of the chamber and respective sampling method, the precision of the instrument, chamber dimensions and operation time (DT). Nevertheless, the obtained result is well comparable with the EC systems. The random error of \(N_2O\) fluxes for 30 min averaging time for the instrument with lowest noise, the AR-CW-QCL instrument, was found to be 0.036 nmol m\(^{-2}\) s\(^{-1}\) (the median value). Note that here we compare the flux detection limit of the chamber based systems (which accounts for all
possible sources of uncertainty) with the total stochastic error of the EC fluxes. The results are of the same magnitude.

In this study we followed the methodology proposed by Mauder et al. (2013) in quantification of the random errors in EC fluxes, i.e. the stochastic error and the error due to instrumental noise in flux. The relative random errors obtained in our study were much larger than the respective errors reported by Mauder et al. (2013) for CO₂ measurements, evidencing that the importance of random errors depends on the trace gas of interest via instrumental precision and the flux magnitude ratio. Kroon et al. (2010a) focus on the evaluation of the EC flux measurements of CH₄ and N₂O specifically. They observed over a dairy farm site the fluxes in the range of 15 to 110 ng N m⁻² s⁻¹ (0.5 to 4 nmol m⁻² s⁻¹), which they classified from low to high flux classes. They performed calibration of the instrument similar to our AR-P-QCL weekly and considered the respective uncertainty random over longer periods of time. Kroon et al. (2010a) reported the average daily and monthly flux relative uncertainties of 31 and 7%, respectively. In our study the N₂O fluxes were typically much smaller (excluding the fertilisation episode), around 0.1 to 0.3 nmol m⁻² s⁻¹. We measured with the similar instrument 36% lower fluxes than obtained by AR-CW-QCL over the period DOY 110-181 and 13% lower fluxes than obtained by two new generation instruments over the period DOY 206-271. Evidently our measurements performance was affected by unidentified error source being systematic in nature. In evaluation of the annual balances of CH₄ and N₂O fluxes over managed fen meadow Kroon et al. (2010b) made an assumption that the uncertainty in EC fluxes was random and was neglected in evaluation of long term averages. In our results this assumption was violated and we suggest that all possible systematic error sources should be considered very carefully in planning, implementing and evaluating the flux measurements of trace gases.

In analysing the random errors of the fluxes Kroon et al. (2010a) assumed that the flux error due to instrumental precision in concentration measurement was negligible. We observed that this was not necessarily the case for N₂O when low flux levels were measured and demonstrated that the method originally proposed by Lenchow et al. (2000) to determine instrumental noise variance worked well in the field conditions over a long period of time.
5 Conclusions

The new instruments based on continuous wave quantum cascade lasers, AR-CW-QCL and LGR-CW-QCL, were stable throughout the campaign in terms of determination of absolute concentrations as well as obtaining very close cumulative fluxes.

The older instruments CS-TDL and AR-P-QCL measured systematically different fluxes over subperiods of the campaign up to 29% and -36%, respectively, compared to the new instruments based on CW-QCL-s, whereas the systematic differences did not prevail throughout the campaign. The reasons for the systematic differences were not identified. We suggest that special emphasis should be on the instrumental stability and correcting procedures that can affect systematically the accuracy of measured fluxes when conducting long-term measurements of prevalingly low fluxes.

The lowest noise level was determined for AR-CW-QCL (0.12 ppb at 10 Hz sampling rate) and the highest for the old generation instrument CS-TDL (precision 2 ppb at 10 Hz sampling rate). During the period DOY 206-272, when all instruments were operational, the lower quantile/median/upper quantile statistics of the fluxes measured by AR-CW-QCL instrument were 0.008/0.11/0.31 nmol m⁻² s⁻¹.

The random errors of fluxes originate from the stochastic nature of turbulence (one-point sampling over limited time interval). Additionally, the instrumental noise contributes to the random flux error. The median values for flux errors during the period DOY 206-272 (error due to instrumental noise / the total error) were detected for the instruments as follows: for CS-TDL 0.155/0.255, AR-CW-QCL 0.010/0.036, LGR-CW-QCL 0.046/0.065, and AR-P-QCL 0.031/0.068 nmol m² s⁻¹. These error statistics indicate that (i) the major component of the flux random error source is the instrumental noise, and (ii) the flux errors for CS-TDL are dominantly larger than the flux magnitude and only in case of AR-CW-QCL the flux error due to instrumental noise can be said to be much smaller than the typical flux value.

The following fractions of fluxes were smaller than the stochastic flux error: in case of CS-TDL 47%, AR-CW-QCL 15%, LGR-CW-QCL 28%, and AR-P-QCL 30%. We conclude that apart from AR-CW-QCL large fraction of the fluxes were within the error magnitude of single half-hour observations.
With the new generation analyzers based on continuous-wave QCL-s N\textsubscript{2}O fluxes can be measured with the EC at locations where the fluxes are small, well below the detection limit of older instruments (CS-TDL for instance). According to our analysis the new instruments enable to attain the flux precision as good as the precision of the modern chamber systems. Thus the new instruments open up the possibility to study N\textsubscript{2}O exchange at new ecosystems, broadening the scientific perspectives.

Acknowledgements

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References


Table 1. Instrumental characteristics. Experimental precision values are based on flux measurements during the period DOY 206-271 (period II). TDL – Tunable Diode Laser; CW-QCL - Continuous-Wave Quantum Cascade Laser; P-QCL – Pulsed QCL.

<table>
<thead>
<tr>
<th>Instrument model</th>
<th>TGA100A</th>
<th>CW-TILDAS-CS</th>
<th>N2O/CO-23d</th>
<th>QC-TILDAS-76-CS</th>
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</thead>
<tbody>
<tr>
<td>Manufacturer</td>
<td>Campbell Scientific Inc.</td>
<td>Aerodyne Research Inc.</td>
<td>Los Gatos Research Inc.</td>
<td>Aerodyne Research Inc.</td>
</tr>
<tr>
<td>Acronym used in current study</td>
<td>CS-TDL</td>
<td>AR-CW-QCL</td>
<td>LGR-CW-QCL</td>
<td>AR-P-QCL</td>
</tr>
<tr>
<td>Measured species</td>
<td>N$_2$O</td>
<td>N$_2$O, H$_2$O, CO</td>
<td>N$_2$O, H$_2$O, CO</td>
<td>N$_2$O, CO$_2$, H$_2$O</td>
</tr>
<tr>
<td>Sample cell volume (ml)</td>
<td>480</td>
<td>500</td>
<td>500 (76 m path length)</td>
<td></td>
</tr>
<tr>
<td>Sample cell pressure (hPa)</td>
<td>50</td>
<td>53</td>
<td>117</td>
<td>53</td>
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<tr>
<td>Spectroscopic correction coefficient b</td>
<td>0.00 (drier used in sampling line)</td>
<td>0.39</td>
<td>0.00 (built-in correction by the instrument)</td>
<td>0.0235</td>
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<tr>
<td>Precision, 10 Hz noise std, $P_{10}/P_{50}/P_{90}$ this study (ppb)</td>
<td>1.89/1.98/2.1</td>
<td>0.12/0.12/0.14</td>
<td>0.46/0.60/0.78</td>
<td>0.43/0.46/0.51</td>
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</table>
Table 2. Eddy covariance measurements setup, flux calculation and quality screening parameters

<table>
<thead>
<tr>
<th>Instrument</th>
<th>CS-TDL</th>
<th>AR-CW-QCL</th>
<th>LGR-CW-QCL</th>
<th>AR-P-QCL</th>
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<td>Sampling height (m)</td>
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<td>2.2/2.4</td>
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<td>2.0/2.5</td>
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<td>Horizontal separation(^1) (m)</td>
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<td>0.05</td>
<td>0.07</td>
<td>0.1</td>
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<td>Tube inner diameter (mm)</td>
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<td>4</td>
<td>8</td>
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<td>Tube length (m)</td>
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<td>16</td>
<td>8.5</td>
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<tr>
<td>Flow rate (LPM)</td>
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<td>13.2</td>
<td>11.6</td>
<td>13.5</td>
</tr>
<tr>
<td>Lag time from tube flow (s)</td>
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<td>0.91</td>
<td>4.2</td>
<td>0.48</td>
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<tr>
<td>Lag time window used in flux calculation (s)</td>
<td>1.0+0.0</td>
<td>1.0+0.0</td>
<td>1.0+0.0(^2)</td>
<td>1.0+0.8(^3)</td>
</tr>
<tr>
<td>Time constant used in spectral corrections (s)</td>
<td>0.12</td>
<td>0.07</td>
<td>0.26</td>
<td>0.15</td>
</tr>
</tbody>
</table>

\(^1\)Refers to separation of the sampling inlet from the center position of the sonic anemometer.

Vertical separation was 0.1 m for all instruments.

\(^2\)Prior to flux calculation concentration records of LGR-CW-QCL were synchronised with AR-CW-QCL outputs.

\(^3\)The lag time window was used to determine the lag time for CO\(_2\), which was assigned as the lag time for N\(_2\)O.
Table 3. Statistics of spectral corrections of fluxes as % of raw uncorrected fluxes: lower percentile/median/upper percentile. Based on flux measurements during the period DOY 206-271 (period II) and data classified as qualified (Table 4). Day time was defined by the elevation of sun higher than zero and night time lower than zero, respectively. Statistics were derived for data when measurements were available for all four instruments.

<table>
<thead>
<tr>
<th></th>
<th>CS-TDL</th>
<th>AR-CW-QCL</th>
<th>LGR-CW-QCL</th>
<th>AR-P-QCL</th>
</tr>
</thead>
<tbody>
<tr>
<td>All data</td>
<td>4.0/6.2/10.2</td>
<td>2.4/3.6/6.0</td>
<td>6.9/12.3/20.0</td>
<td>4.5/7.3/14.8</td>
</tr>
<tr>
<td>Daytime data</td>
<td>4.0/6.1/9.8</td>
<td>2.6/3.6/5.8</td>
<td>6.9/12.0/18.5</td>
<td>4.5/6.9/10.5</td>
</tr>
<tr>
<td>Night data</td>
<td>3.6/6.3/11.3</td>
<td>2.2/3.6/6.4</td>
<td>6.7/12.9/22.3</td>
<td>4.5/7.7/20.2</td>
</tr>
</tbody>
</table>

Table 4. Average fluxes (nmol m\(^{-2}\) s\(^{-1}\)) ± random error of the average. Period I DOY 110-181 (20.04-30.06.2011), Period II DOY 206-271 (25.07-28.09.2011), Period III DOY 272 – 324 (29.09-20.11.2011). % data available represents the fraction of half-hour periods when data from all 3 (or 4) instruments was available (data from wind direction interval 50-110\(^{\circ}\) excluded), relative to full time period length. Averaging of fluxes for each instrument was performed only for data if measurements were available for all instruments used in respective period. No gap filling was used.

<table>
<thead>
<tr>
<th></th>
<th>% data available</th>
<th>% data qualified (out of available)</th>
<th># 30 min periods averaged</th>
<th>CS-TDL</th>
<th>AR-CW-QCL</th>
<th>LGR-CW-QCL</th>
<th>AR-P-QCL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Period I</td>
<td>69.2</td>
<td>75.2</td>
<td>1797</td>
<td>0.931 ±0.018</td>
<td>0.870 ±0.009</td>
<td>0.560 ±0.011</td>
<td></td>
</tr>
<tr>
<td>Period II</td>
<td>55.0</td>
<td>79.4</td>
<td>1383</td>
<td>0.183 ±0.010</td>
<td>0.146 ±0.006</td>
<td>0.138 ±0.007</td>
<td>0.124 ±0.003</td>
</tr>
<tr>
<td>Period III</td>
<td>61.4</td>
<td>78.2</td>
<td>1220</td>
<td>0.067 ±0.002</td>
<td>0.057 ±0.002</td>
<td>0.058 ±0.003</td>
<td></td>
</tr>
</tbody>
</table>

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Table 5. Average micrometeorological conditions during the experimental periods. Period I
DOY 272 – 324 (29.09-20.11.2011). Day time was defined by the elevation of sun higher
than zero and night time lower than zero, respectively. Average latent heat fluxes were
determined from IRGA measurements.

<table>
<thead>
<tr>
<th></th>
<th>Temperature</th>
<th>Air rel. humidity, %</th>
<th>Wind speed, m s⁻¹</th>
<th>Friction velocity, m s⁻¹</th>
<th>Sensible heat flux, W m⁻²</th>
<th>Latent heat flux, W m⁻²</th>
</tr>
</thead>
<tbody>
<tr>
<td>Day, I</td>
<td>11.6</td>
<td>62.9</td>
<td>2.21</td>
<td>0.28</td>
<td>27.5</td>
<td>78.9</td>
</tr>
<tr>
<td>Night, I</td>
<td>6.5</td>
<td>78.3</td>
<td>1.34</td>
<td>0.14</td>
<td>-20.2</td>
<td>8.1</td>
</tr>
<tr>
<td>Day, II</td>
<td>15.3</td>
<td>75.2</td>
<td>1.35</td>
<td>0.26</td>
<td>9.7</td>
<td>109.3</td>
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<tr>
<td>Night, II</td>
<td>11.2</td>
<td>90.3</td>
<td>1.06</td>
<td>0.17</td>
<td>-18.6</td>
<td>10.1</td>
</tr>
<tr>
<td>Day, III</td>
<td>6.1</td>
<td>85.0</td>
<td>1.46</td>
<td>0.29</td>
<td>-10.8</td>
<td>41.5</td>
</tr>
<tr>
<td>Night, III</td>
<td>4.8</td>
<td>90.6</td>
<td>1.21</td>
<td>0.23</td>
<td>-23.5</td>
<td>11.5</td>
</tr>
</tbody>
</table>
Figure 1. Daily average fluxes for four instruments containing period I DOY 110-181 (a), period II DOY 206-271 (b) and period III DOY 272-324 (c). No gap-filling was used in calculation of daily average fluxes.
Figure 2. Soil water content (SWC) at 2.5 cm depth and precipitation (a) and soil temperature at 2.5 cm depth (b) during the measurement campaign.
Figure 3. Normalised co-spectra (left panels) and spectra (right panels) of N₂O measurements by instruments CS-TDL (upper panels a, b), AR-CW-QCL (middle panels c, d) and AR-P-QCL (lower panels e, f) during the high flux period, DOY 146 (26.05.2011) 7:00 to 13:00 EET. The RCG crop was about 0.4 m tall during the given period.
Figure 4. Co-spectral transfer functions derived for CS-TDL (a), AR-CW-QCL (b) and AR-P-QCL (c) from the temperature and N$_2$O co-spectra presented in Fig. 2.
Figure 5. Normalised co-spectra (left panels) and spectra (right panels) of N$_2$O measurements by instruments AR-CW-QCL (upper panels a, b) and LGR-CW-QCL (lower panels c, d) during the period DOY 216 (04.08.2011) 00:30 to 4:00 EET. The RCG crop was about 1.8 m tall during the given period.
Figure 6. (a) Instrumental noise, presented as one standard deviation of the noise at 10 Hz frequency, (b) N₂O flux random error (blue) and flux random error due to instrumental noise (green) statistics; (c) the same as (b) but for relative fluxes. The boxplots present the lower and upper percentiles, quartiles and median values of the distributions. Based on flux measurements during the period DOY 206-271 (period II).
Figure 7. Correlation scatter plots of 30 min average N₂O fluxes (in nmol m⁻² s⁻¹), as measured by CS-TDL and AR-P-QCL vs. AR-CW-QCL during the period I DOY 110-181 (upper panels a, b), and CS-TDL and LGR-CW-QCL vs. AR-CW-QCL during the period II DOY 206-271 (lower panels c, d). The lines present the linear fit with coefficients presented on the plots.
Figure 8. Cumulative sums of available flux data for three periods: upper panel (a) period I DOY 110-181 (20.04-30.06.2011), middle panel (b) period II DOY 206-271 (25.07-28.09.2011), lower panel (c) period III DOY 272 – 324 (29.09-20.11.2011). Accumulation of fluxes for each instrument was performed only for data if measurements were available for all instruments used in respective period. No gap filling was used.